

# EE-464 STATIC POWER CONVERSION-II

## Three Phase Inverters

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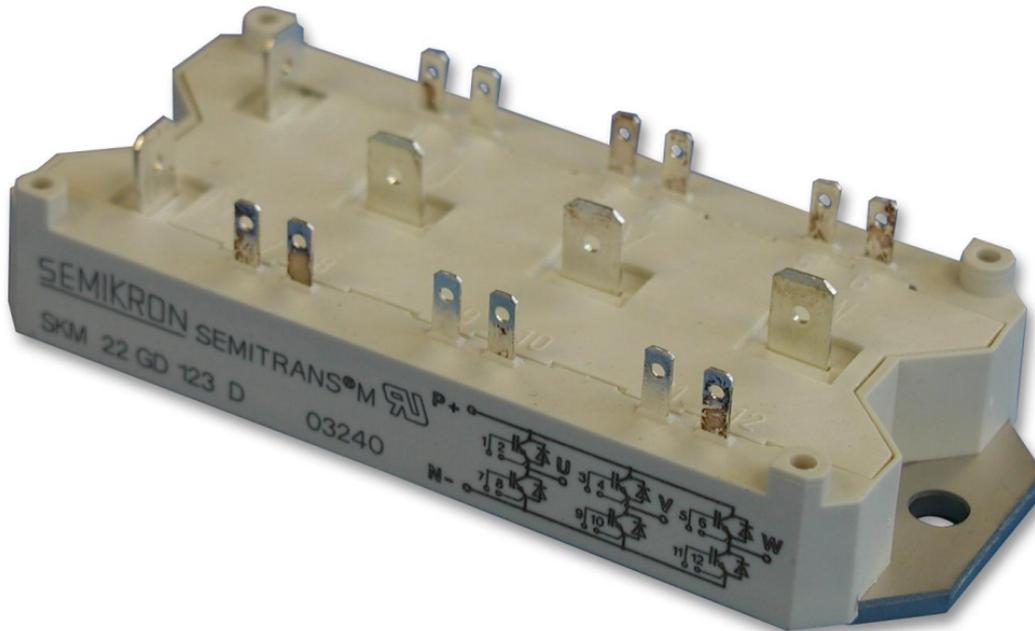
# Three Phase Inverters

**ABB**

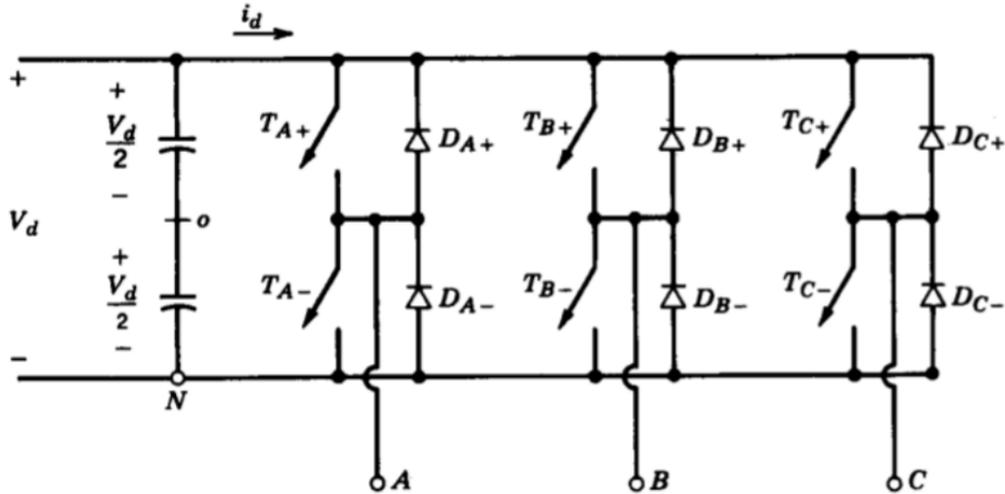


Different Sized Variable Frequency Drives (VFD)

# Three Phase Inverters



# Three Phase Voltage-Source Inverters



Three inverter legs are connected in parallel

# Three Phase Voltage-Source Inverters

- . Do not close top and bottom switches at the same time
- . Point (o) is not needed but shown for simplicity in calculations
- . Current can flow through the switch or anti-parallel diodes.

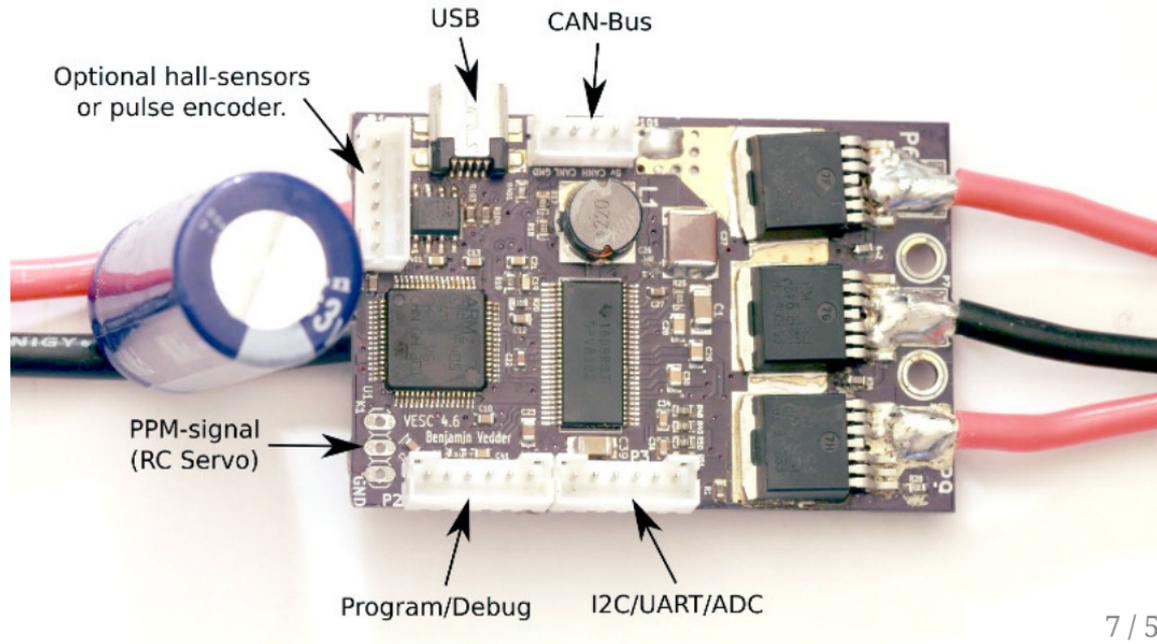
# PWM Techniques

There are many different PWM techniques that will be covered:

- Square-wave (Six-step) PWM
- Sinusoidal PWM (SPWM)
- Hysteresis (Bang-Bang) Control
- Space-Vector PWM (SVPWM)
- Third harmonic injection

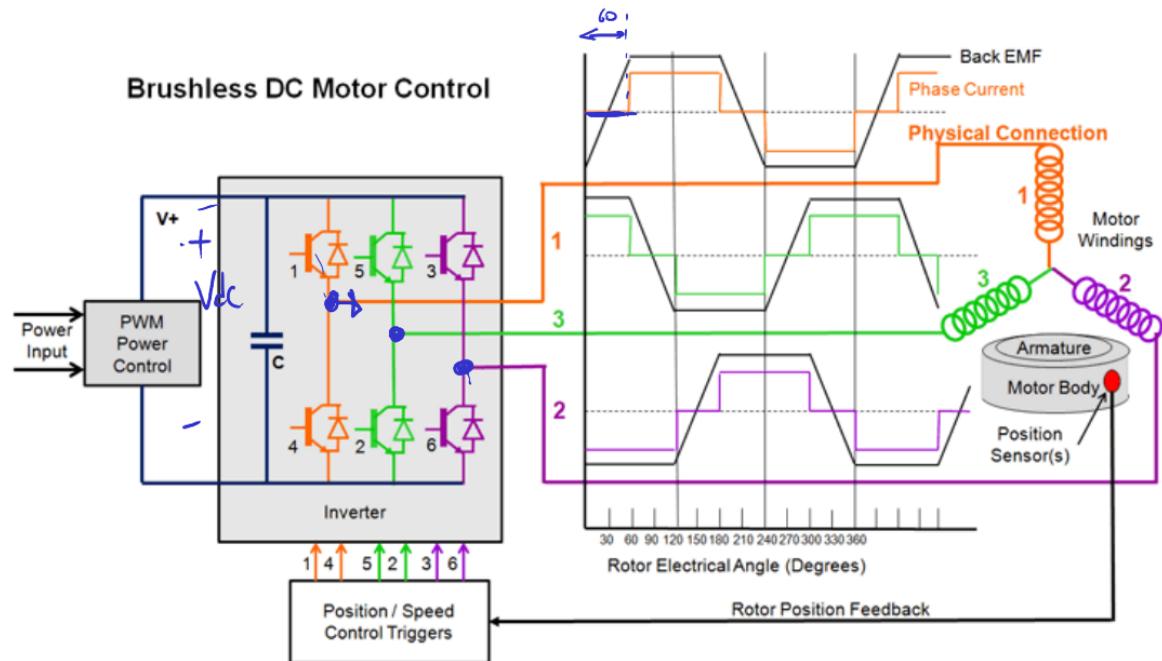
# Six-Step Inverter

Commonly used in BLDC motor Drives



# Six-Step Inverter

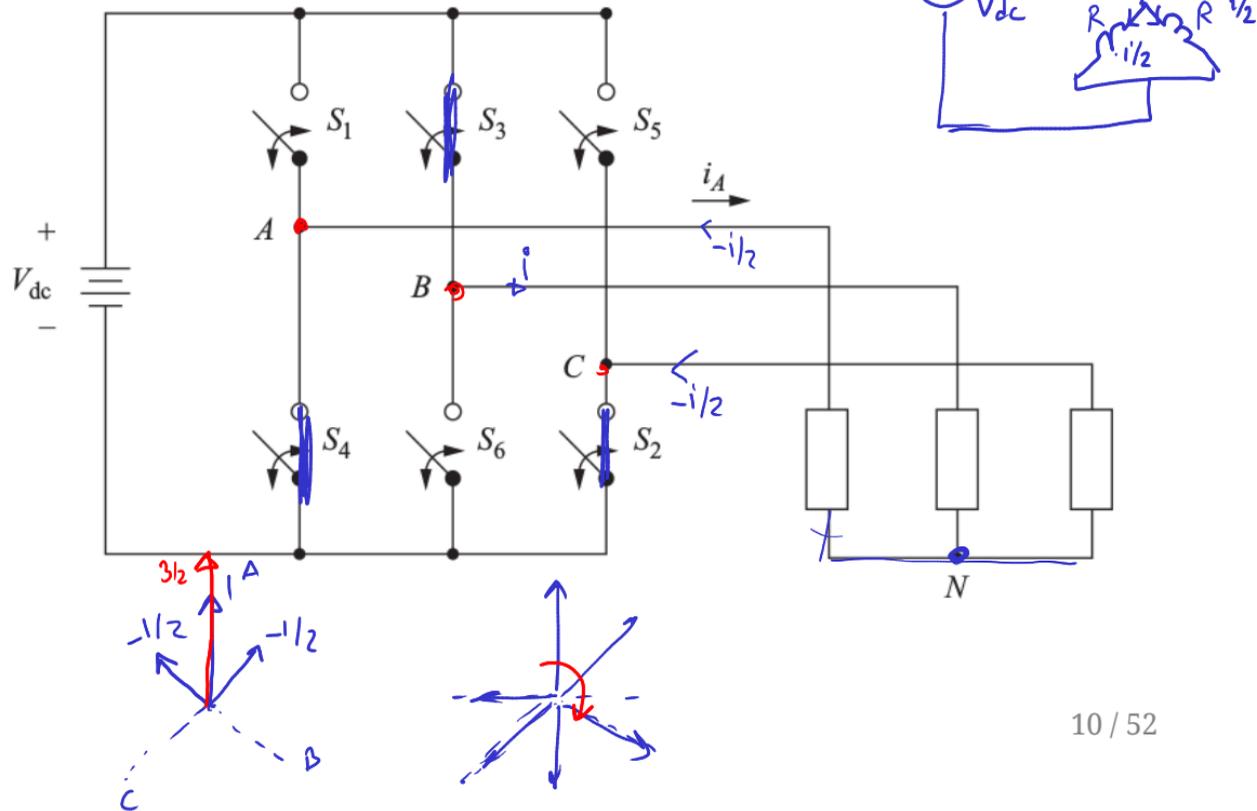
Commonly used in BLDC motor Drives



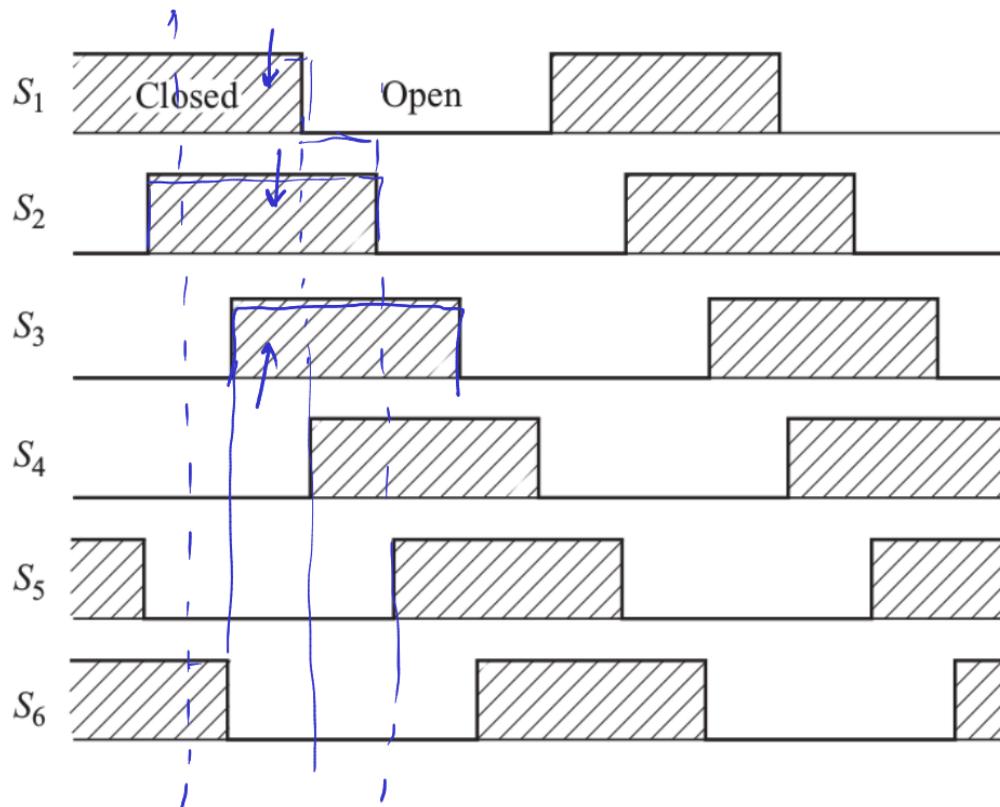
# Six-Step Inverter

- Each switch has 50% duty ratio.
- Each leg has a phase difference of 120 degrees
- One switching action takes place at every 60 degrees

# Six-Step Inverter

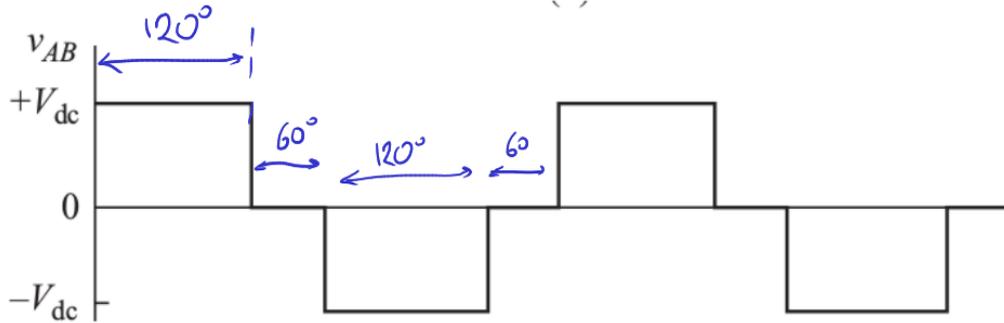


# Six-Step Inverter

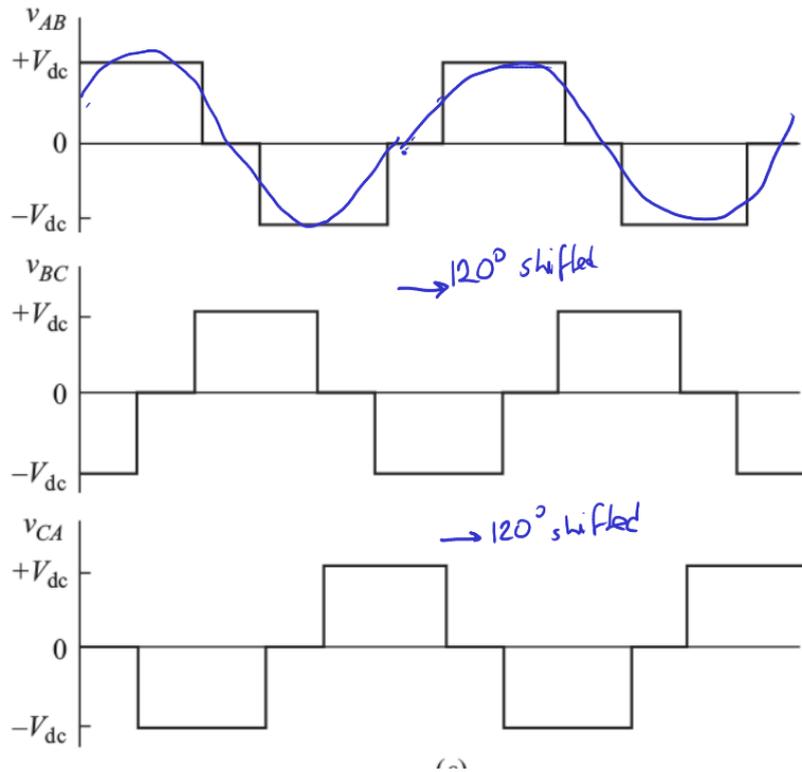


# Six-Step Inverter

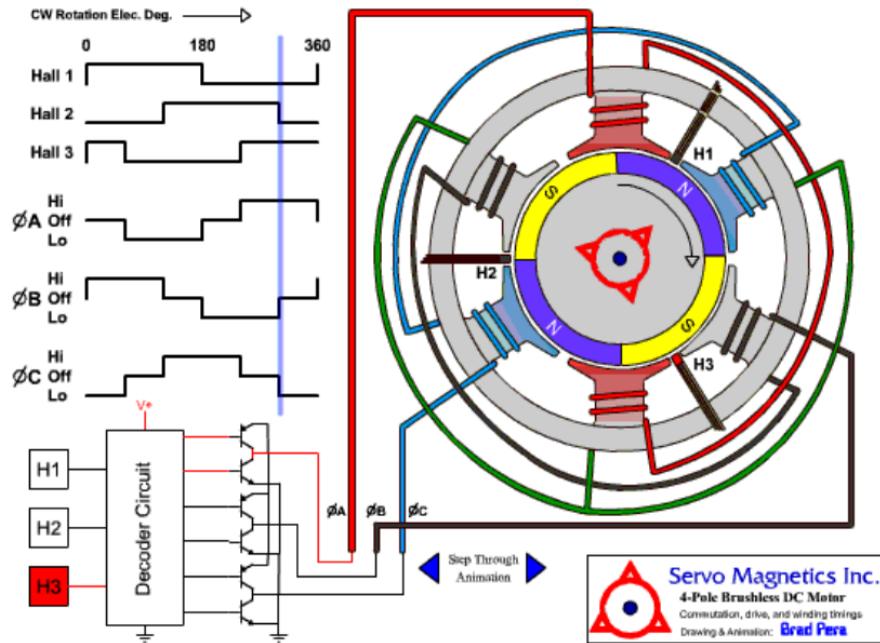
Line-to-line voltage:  $V_{AB} = V_{A0} - V_{B0}$



# Line-to-line voltages:

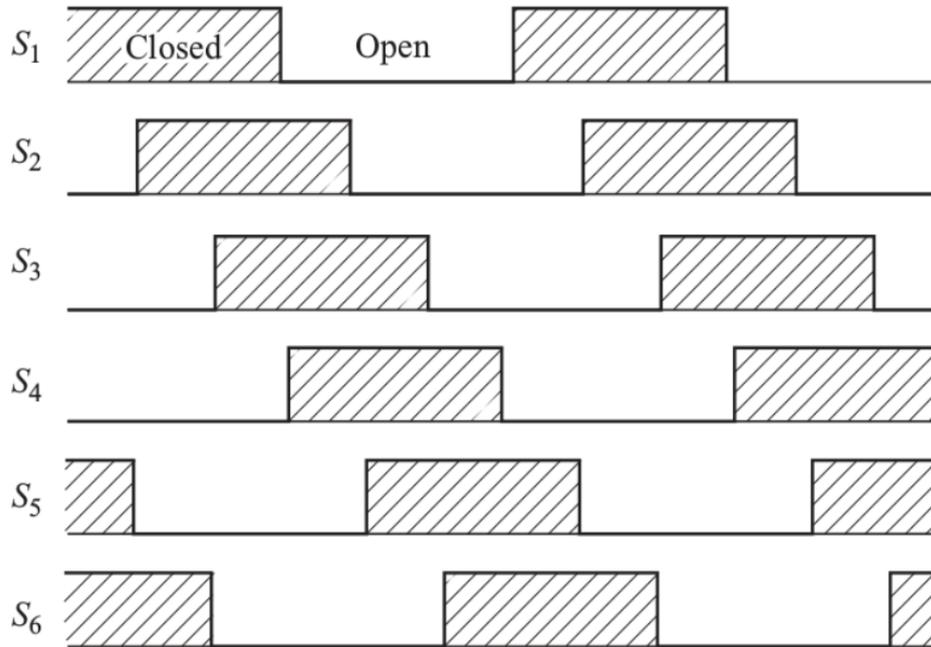


# Square Wave Operation

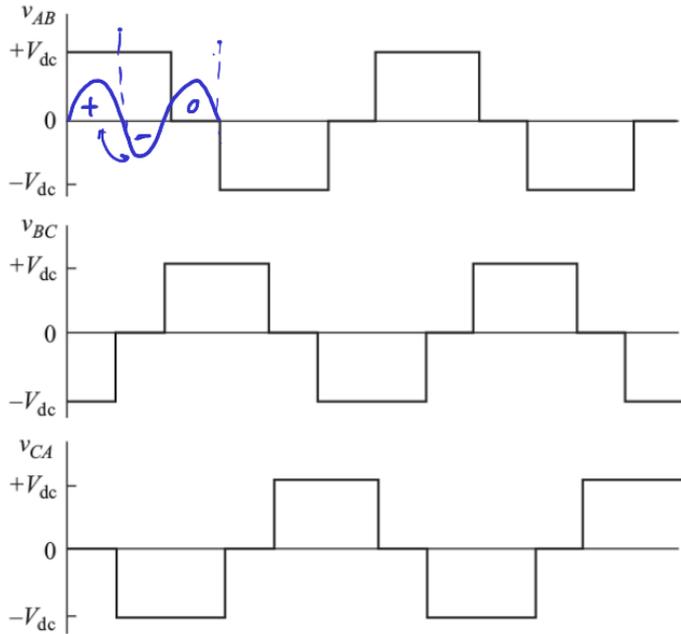


[BLDC Drive with square wave](#)

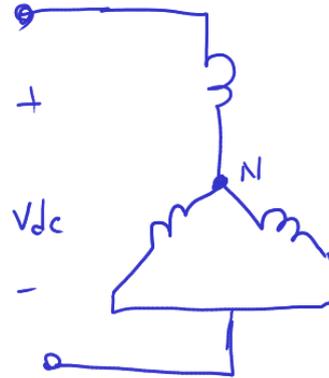
# Switching Sequence



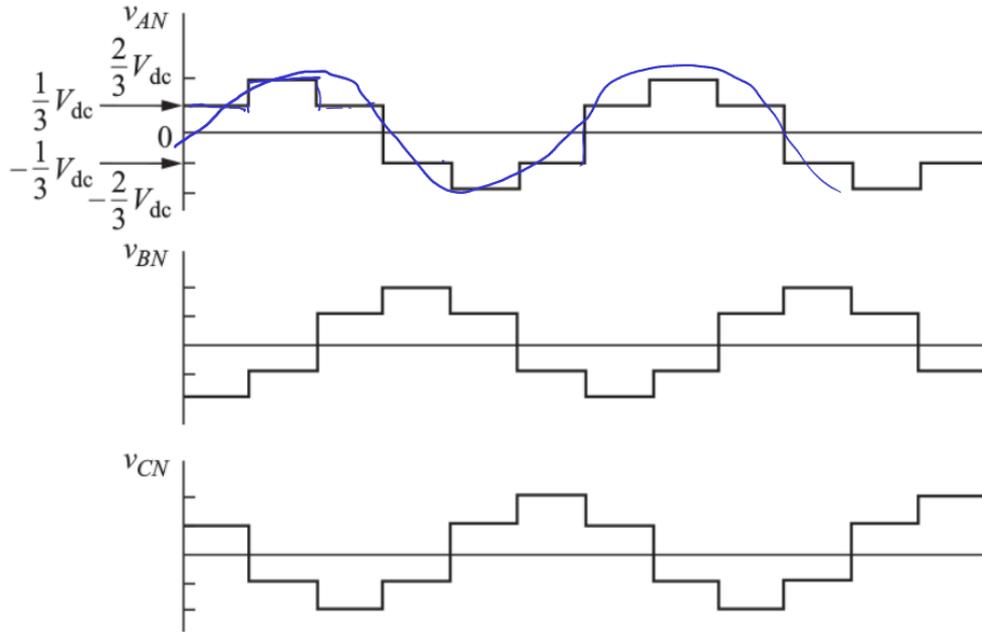
# Line-to-Line Voltages



(c)



# Equivalent Phase Voltages



# Line-to-Line Harmonics

## Fourier Coefficients

$$\hat{V}_{n,l-l} = \frac{1}{n} \frac{4}{\pi} \underbrace{V_{dc}} \cos\left(n \frac{\pi}{6}\right)$$

$$\text{For: } n = \underline{6k \pm 1} = \underbrace{1}, \underbrace{5}, \underbrace{7}, \underbrace{11}, \underbrace{13} \dots$$

- No even harmonics ✓
- No third order harmonics ✓

# Line-to-Line Harmonics

RMS of the fundamental component?

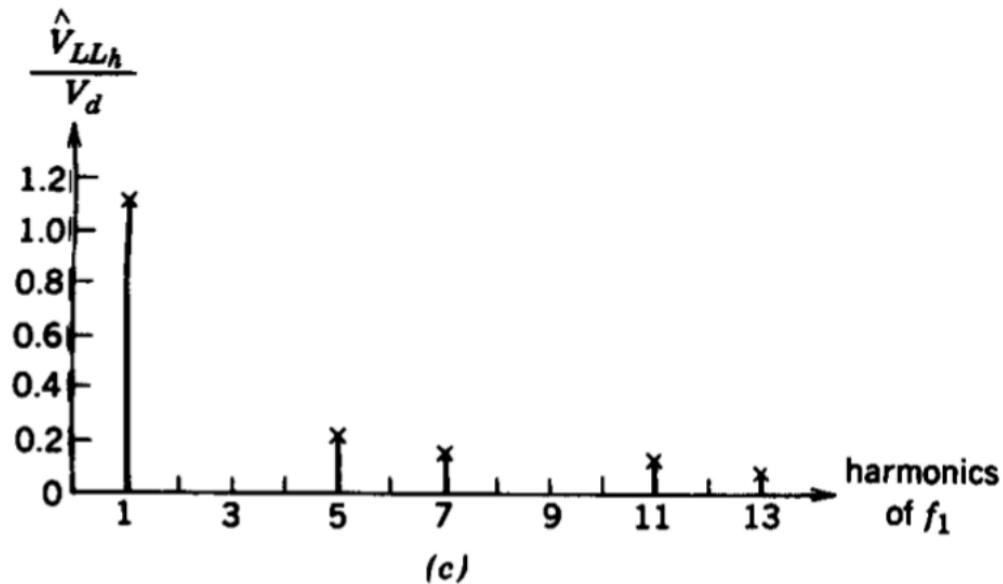
$$V_{1,l-l,rms} = \frac{1}{\sqrt{2}} \frac{4}{\pi} V_{dc} \frac{\sqrt{3}}{2} = 0.78V_{dc}$$

Harmonics RMS:

$$V_{n,l-l,rms} = \frac{1}{n} 0.78V_{dc}$$

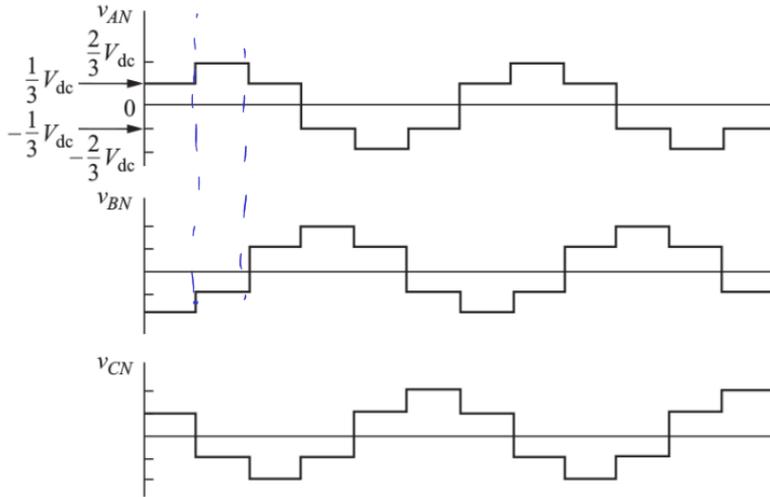
For:  $n = 6k \pm 1 = 1, 5, 7, 11, 13...$

# Line-to-Line Harmonics



# Line-to-Neutral voltages:

Neutral point is floating



Voltage level changes every 60 degrees (that's why it's a six-step inverter!)

# Line-to-Neutral Harmonics

## Fourier Coefficients

$$\hat{V}_{n,l-N} = \frac{1}{n} \frac{2}{3\pi} V_{dc} \left( 2 + \cos\left(\frac{\pi n}{3}\right) - \cos\left(\frac{2\pi n}{3}\right) \right)$$

For:  $n = 6k \pm 1 = \underline{1, 5, 7, 11, 13} \dots$

### Simpler Form

$$\hat{V}_{n,l-N} = \frac{1}{n} \frac{2}{\pi} V_{dc}$$

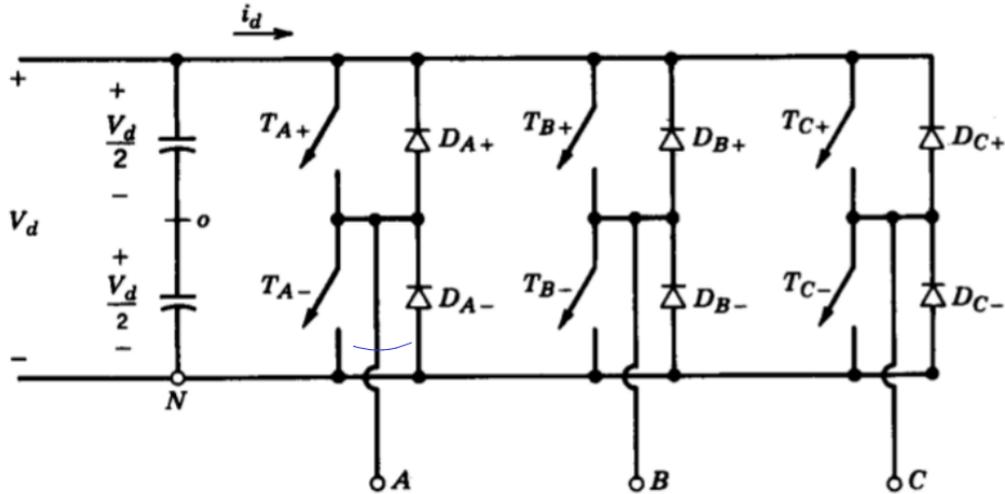
# Line-to-Neutral Harmonics

$$\hat{V}_{n,l-N} = \frac{1}{n} \frac{2}{\pi} V_{dc}$$

For:  $n = 6k \pm 1 = 1, 5, 7, 11, 13\dots$

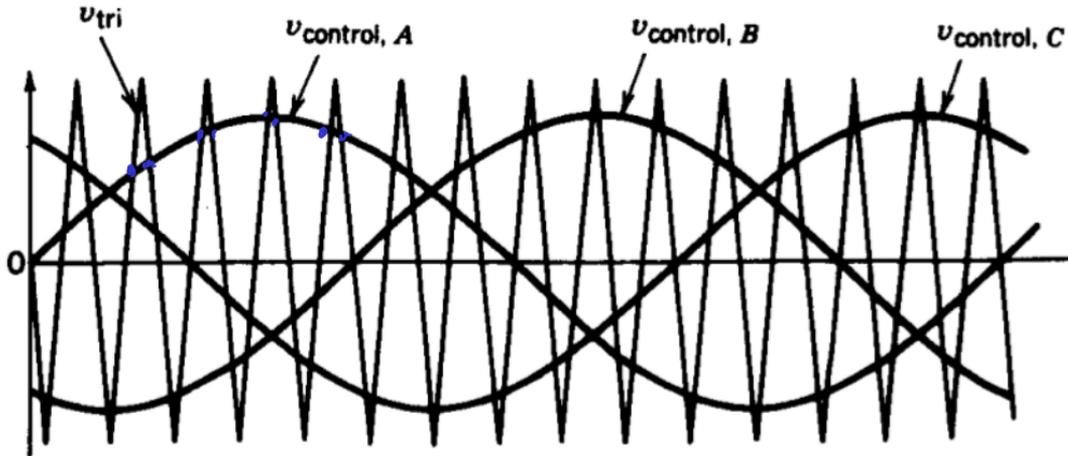
- No even harmonics
- No third order harmonics

# Three Phase Voltage-Source Inverter



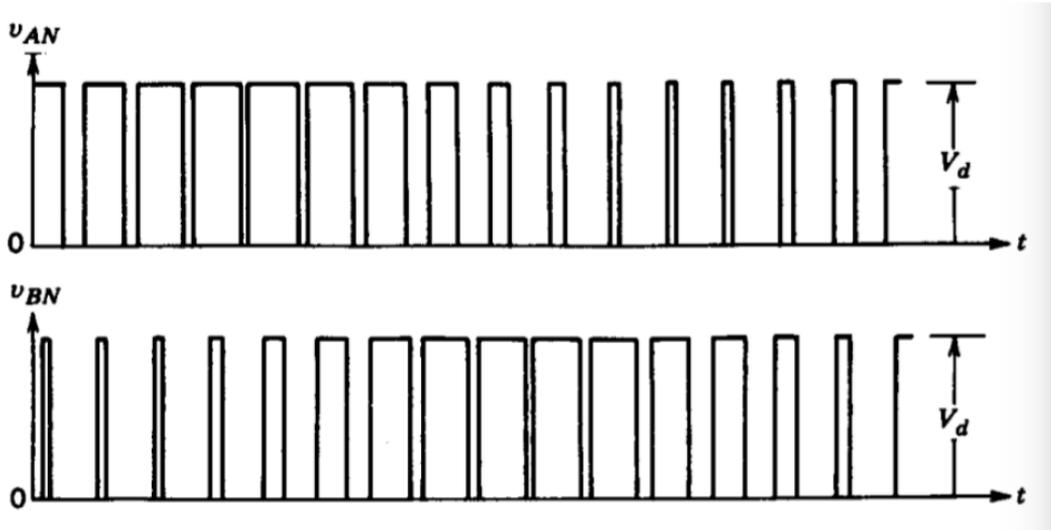
# Sinusoidal PWM (SPWM)

A triangular carrier wave is generated and compared with each phase.



# Sinusoidal PWM (SPWM)

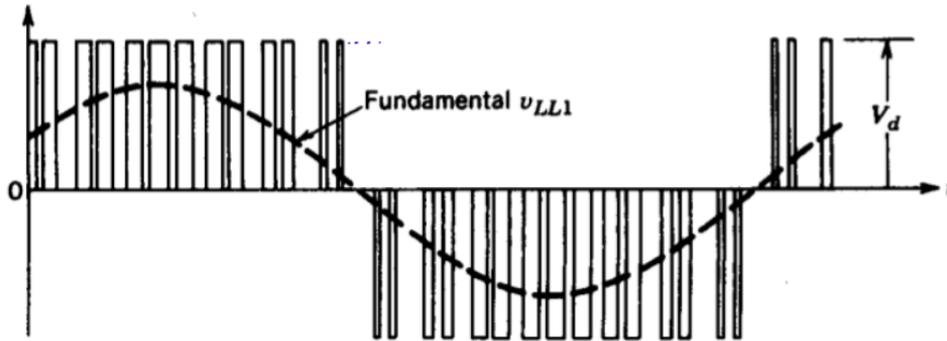
$V_d$  or 0 voltage is generated at  $V_{AN}$  depending on the comparison.



# Sinusoidal PWM (SPWM)

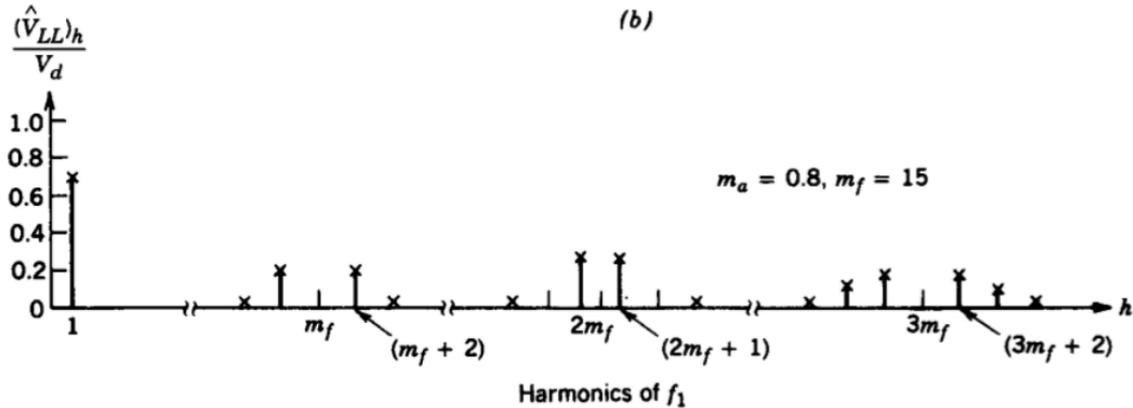
Line to line voltage ( $V_{AB} = V_{AN} - V_{BN}$ )

$$v_{AB} = v_{AN} - v_{BN}$$



# Sinusoidal PWM (SPWM)

## Harmonics in the line voltage

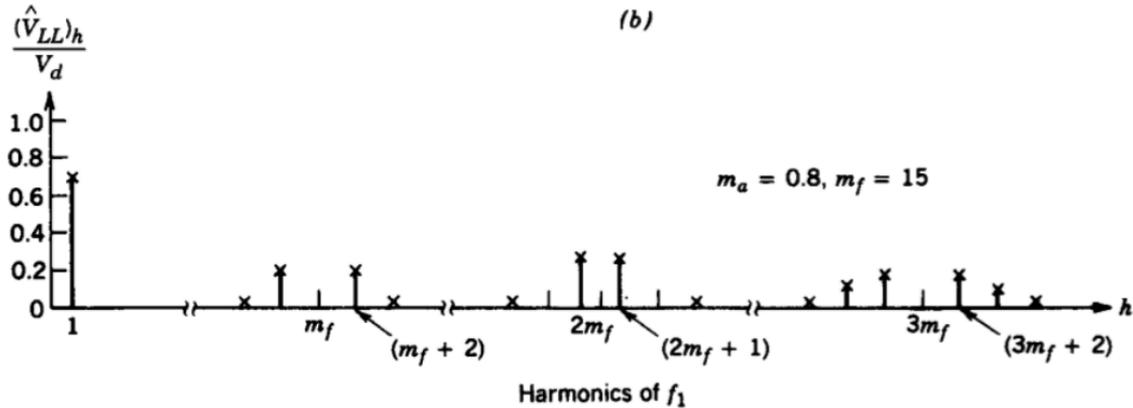


Harmonics at the side bands,

Like the unipolar but starts at  $m_f$ .

# Sinusoidal PWM (SPWM)

## Harmonics in the line voltage



If  $m_f$  is small, it is better to use synchronized PWM, and  $m_f$  should be an odd integer, preferably multiple of 3 to reduce harmonics.

# Sinusoidal PWM (SPWM)

## Harmonics in the line voltage

**Table 8-2** Generalized Harmonics of  $v_{LL}$  for a Large and Odd  $m_f$  That Is a Multiple of 3.

$h \backslash m_a$	0.2	0.4	0.6	0.8	1.0
1	0.122	0.245	0.367	0.490	0.612
$m_f \pm 2$	0.010	0.037	0.080	0.135	0.195
$m_f \pm 4$				0.005	0.011
$2m_f \pm 1$	0.116	0.200	0.227	0.192	0.111
$2m_f \pm 5$				0.008	0.020
$3m_f \pm 2$	0.027	0.085	0.124	0.108	0.038
$3m_f \pm 4$		0.007	0.029	0.064	0.096
$4m_f \pm 1$	0.100	0.096	0.005	0.064	0.042
$4m_f \pm 5$			0.021	0.051	0.073
$4m_f \pm 7$				0.010	0.030

# Voltage Levels?

Linear Region ( $m_a < 1$ )

$$\hat{V}_{AN1} = m_a \frac{V_d}{2}$$

$$V_{l-l,rms} = \frac{\sqrt{3}}{\sqrt{2}} m_a \frac{V_d}{2}$$

$$V_{l-l,rms} = 0.612 V_d \text{ (max in linear region)}$$

# Voltage Levels?

Overmodulation ( $m_a > 1$ )

Square-Wave Operation?

$$V_{l-l,rms} = \frac{\sqrt{3}}{\sqrt{2}} \frac{4}{\pi} m_a \frac{V_d}{2}$$

$$V_{l-l,rms} = 0.78V_d$$

$$V_{l-l,rms,h} = \frac{0.78}{h} V_d \text{ for } h = 6n \pm 1$$

# Voltage Levels?

