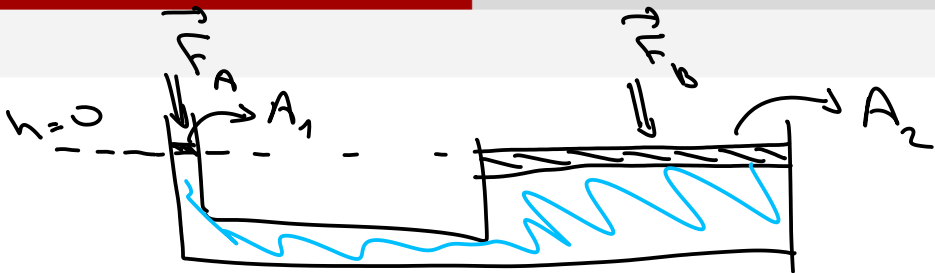


Hydraulics

$$P = P_0 + \rho g h$$



$$\left. \begin{aligned} P_A - P_B &= P_C - P_D \\ P_B &= P_D \end{aligned} \right\} P_A = P_C$$



$$P = P_0 + \rho g h$$

$$\frac{F_A}{A_1} = \frac{F_B}{A_2}$$

$$F_A = \frac{A_1}{A_2} F_B$$

$$m_1 = 1 \text{ kg}$$



$$A_2 \quad m_2 = 100 \text{ kg}$$



$$\frac{A_1}{A_2} = \frac{1}{100}$$

Laminar Flow X Turbulant flow

$l_2 = v_1 dt$ $l_1 = v_1 dt$



$$P_1 A_1 l_1 = P_2 A_2 l_2$$

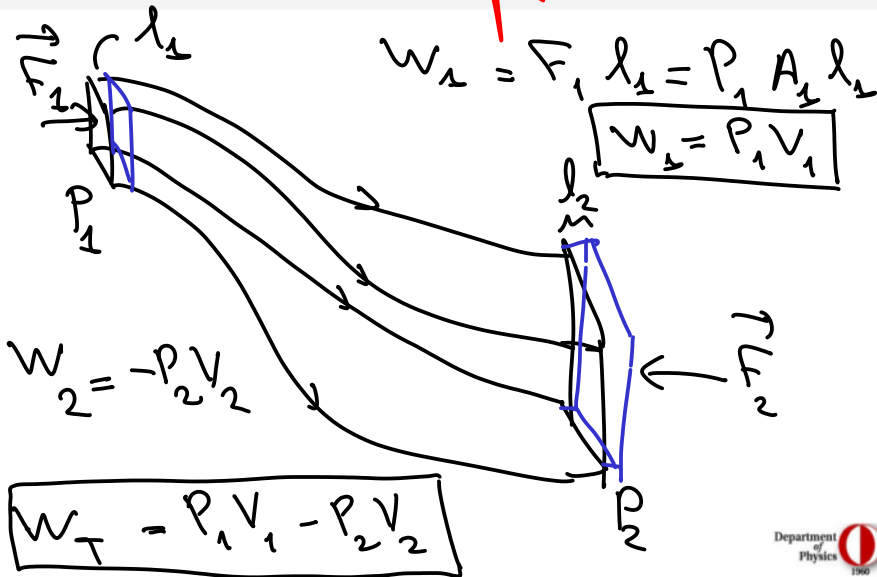
$$\Rightarrow P_1 A_1 v_1 = P_2 A_2 v_2$$

$$\rho_1 A_1 v_1 = \rho_2 A_2 v_2$$

^{i.f.} $\rho_1 = \rho_2$ incompressible liquid

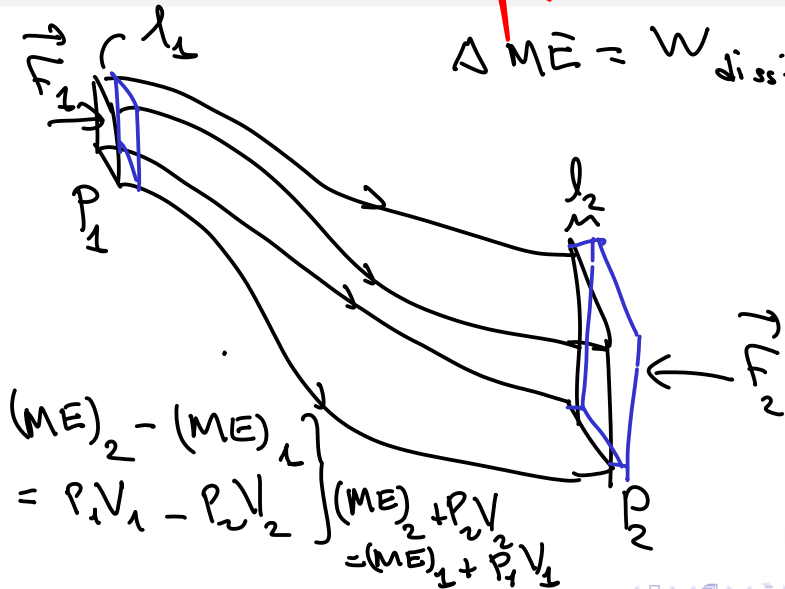
$$\Rightarrow \boxed{A_1 v_1 = A_2 v_2}$$

Bernoulli's Principle



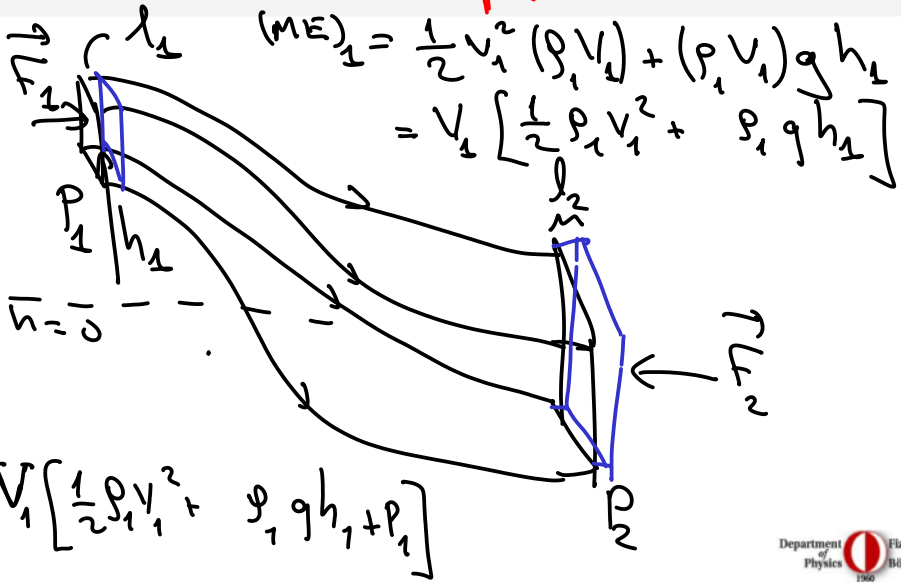
Bernoulli's Principle

$$\Delta ME = W_{\text{dissip}} = P_1 V_1 - P_2 V_2$$



$$\begin{aligned} (ME)_2 - (ME)_1 &= P_1 V_1 - P_2 V_2 \\ (ME)_2 + P_2 V_2 &= (ME)_1 + P_1 V_1 \end{aligned}$$

Bernoulli's Principle

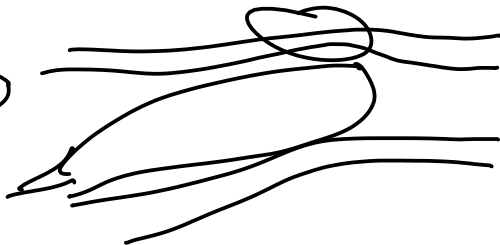
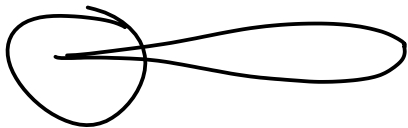


$$V_1 \left[\frac{1}{2} \rho v_1^2 + \rho g h_1 + P_1 \right] = (1 \rightarrow 2)$$

+ incompressibility $\Rightarrow V_1 = V_2$

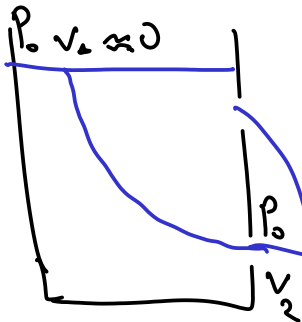
$$\Rightarrow \boxed{\frac{1}{2} \rho v^2 + \rho g h + P = \text{const}}$$

Bernoulli's eqn



$$A_1 v_1 = A_2 v_2$$

11 x



$$\frac{1}{2} \rho v^2 + \rho g h + P = \text{const}$$
$$\frac{1}{2} \rho v_1^2 + \rho g h_1 + P$$
$$= \frac{1}{2} \rho v_2^2 + \rho g h_2 + P$$

$$\frac{1}{2} \rho v_2^2 = \rho g (h_1 - h_2)$$

$$v_2 = \sqrt{2g \Delta h}$$

