

Temperature

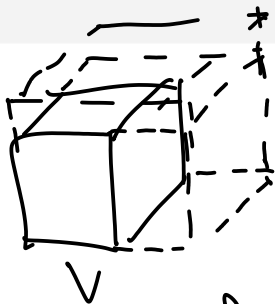
Temperature
Heat (Energy)



$$\Delta L \propto L \Delta T$$

$$\Delta T = \frac{\Delta L}{L}$$



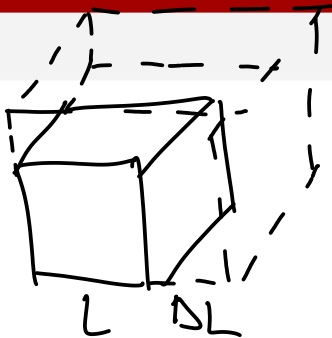


$$\begin{aligned} \gamma &= 3\alpha \\ \beta &= 2\alpha \end{aligned}$$



$$\frac{\Delta V}{V} \propto \Delta T$$

$$\begin{aligned} \Delta L &= \alpha L \Delta T \\ \Delta A &= \beta A \Delta T \\ \Delta V &= \gamma V \Delta T \end{aligned}$$



$$V = L^3$$

$$\Delta L = \alpha L \Delta T$$

$$\Delta V = \gamma V \Delta T$$

$$\begin{aligned} \Delta V &= V_f - V_i = (L + \Delta L)^3 - (L)^3 \\ &= \cancel{L^3} + 3\Delta L L^2 + 3(\Delta L)^2 L + \cancel{(\Delta L)^3} \\ &= \gamma V \Delta T \end{aligned}$$



$$100^{\circ}\text{C} \quad 212^{\circ}\text{F} \quad 112^{\circ}\text{E} \quad \Delta V = \gamma V \Delta T$$

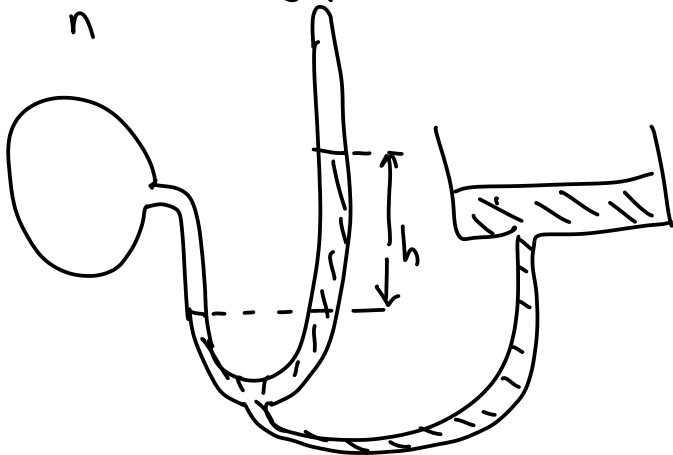
$$\Delta h \propto \Delta T$$

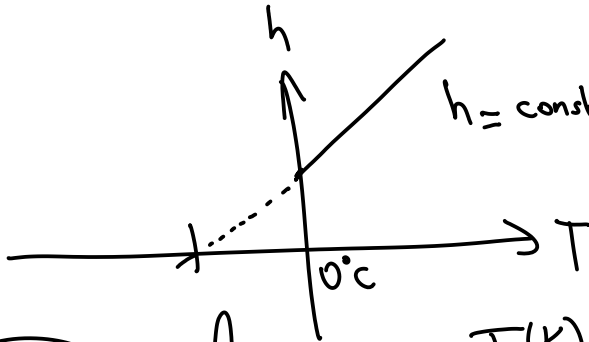
$$32^{\circ}\text{F} \quad 13^{\circ}\text{E}$$

$$\frac{C}{100} = \frac{F - 32}{180} = \frac{E - 13}{99}$$

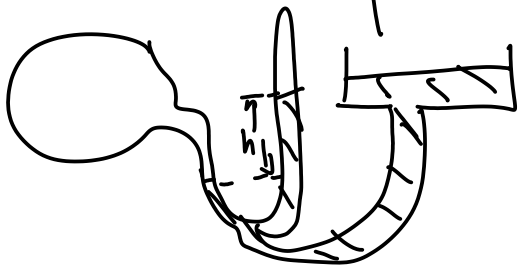
Ideal Gas

$$\frac{PV}{n} = \text{constant at constant } T$$





$$h = \text{const} [T(^{\circ}\text{C}) + 273.15^{\circ}\text{C}]$$

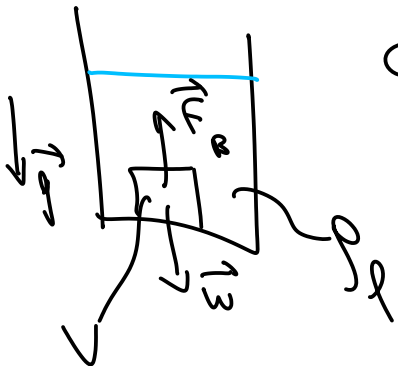


$$T(\text{K}) \leftrightarrow T(^{\circ}\text{C}) + 273.15$$

$$0^{\circ}\text{C} \leftrightarrow 273.15\text{K}$$

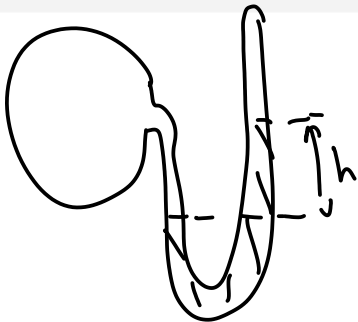
$$100^{\circ}\text{C} \leftrightarrow 373.15\text{K}$$

QUIZ 10



$$Q: |\vec{F}_B| = ?$$

$$\frac{|\vec{g}|}{\sin \theta} = g$$



$$h = \text{const } T$$

$$h \propto P$$

$$\frac{PV}{n} = \text{const } T$$

$$\Rightarrow \frac{PV}{nT} = R$$

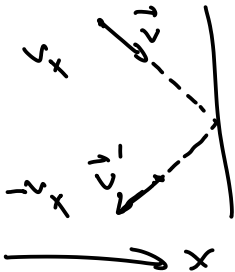
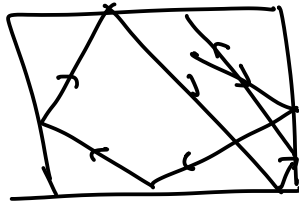
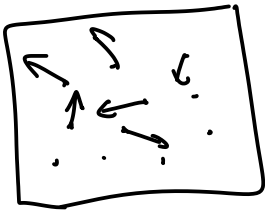
$$PV = nRT$$

$$PV = nRT \quad n = \frac{N}{N_A}$$

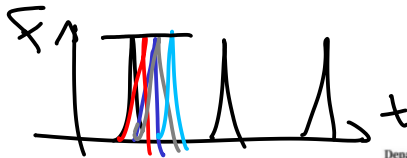
$$N_A = 6.02 \times 10^{23}$$

$$PV = N \left(\frac{R}{N_A} \right) T \equiv N k_B T$$

k_B : Boltzmann's Constant



$$|\vec{p}| = m 2v_x$$



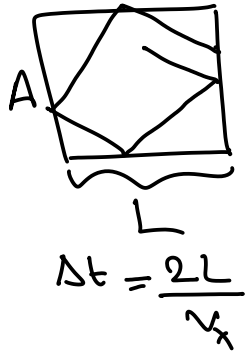
$\langle F \rangle$: average of F

$$\langle F_T \rangle = N \langle F_1 \rangle$$

$$F_1 = \frac{\Delta p}{\Delta t} = \frac{m 2v_x}{\frac{2L}{v_x}}$$

$$F_1 = \frac{mv_x^2}{L}$$

$$\langle F_T \rangle = \frac{Nm v_x^2}{L}$$



$$\langle F_T \rangle = \frac{N m v_x^2}{L}$$

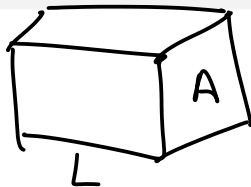
$$P = \frac{F}{A} = \frac{N m v_x^2}{AL} \quad \left. \begin{matrix} AL \\ \end{matrix} \right\} = V$$

$$PV = N m \overline{v_x^2}$$

$$PV = N k_B T$$

$$\overline{v_x^2} = \overline{v_y^2} = \overline{v_z^2} = \frac{1}{3} \overline{v^2}$$

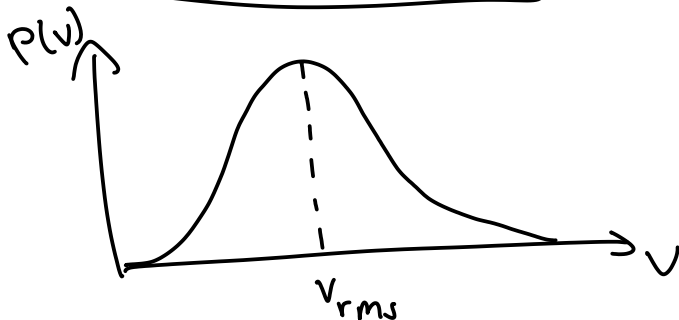
$$PV = N \left(\frac{1}{2} m \overline{v^2} \right) \frac{2}{3}$$



$$PV = N \left(\frac{1}{2} m \overline{v^2} \right) \frac{2}{3} \equiv N k_B T$$

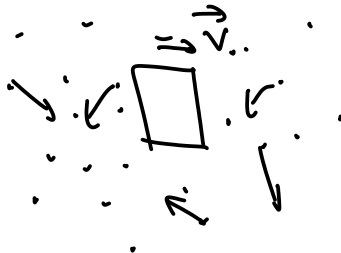
$$\left\langle \frac{1}{2} m v^2 \right\rangle = \frac{3}{2} k_B T$$

$$v_{rms} = \sqrt{\overline{v^2}}$$



$$\vec{F}_D = -bv$$

$\rightarrow x$



$$\vec{v}_2 = v \hat{x}$$

$$|\Delta \vec{p}_2| = 2m(v_2 - v)$$

$$= 2m(v_2 - v)$$



$$\vec{v}_1 = -v_1 \hat{x}$$

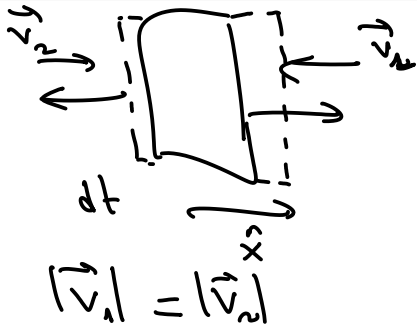
$$= (2v - v_2) \hat{x}$$

$$= (2v + v_1) \hat{x}$$

$$|\Delta \vec{p}_1| = 2m(v - v_1)$$

$$\vec{v}_1 = -v_1 \hat{x}$$

$$|\Delta \vec{p}_1| = 2m(v + v_1)$$



$$\Delta \vec{p}_1 = \sqrt{2} m (v + v_1) \hat{x}$$

$$\Delta \vec{p}_2 = +2m(v_2 - v) \hat{x}$$

$$\Delta \vec{p}_1 + \Delta \vec{p}_2 = 2m(v_2 - v) \hat{x} - 2m(v_1 + v) \hat{x}$$

$$\Delta \vec{p}_1 + \Delta \vec{p}_2 = -4m v \hat{x}$$

$$\Rightarrow \vec{F}_D \propto -\vec{v}$$

Quiz Bonus 1

$$\vec{A} = 3\hat{x} + 4\hat{y}$$

$$\vec{B} = 2\hat{z}$$

i) $\vec{A} \cdot \vec{B} = ?$

ii) $\vec{A} + \vec{B} = ?$

Use one FULL
page for the
Quiz