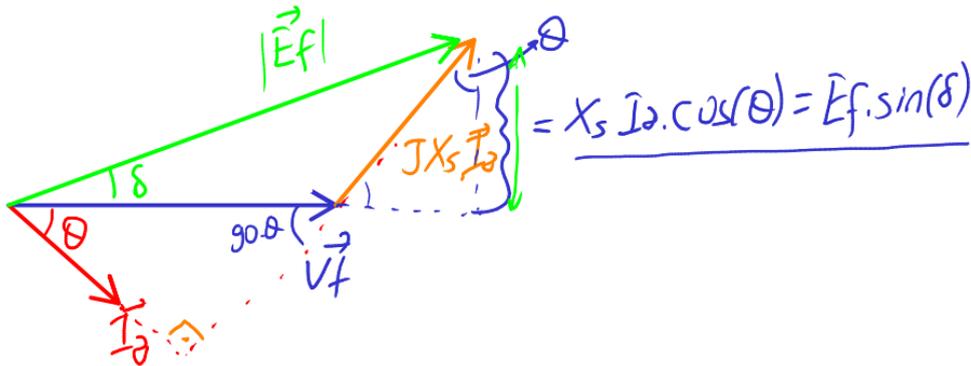


# Power of a Synchronous Machine

We already showed:

$$E_f \sin(\delta) = X_s I_a \cos(\theta)$$

Note: We neglected  $R_a$



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Write Power equation in terms of  $E_f$

$$P = 3 V_t \underbrace{I_a \cos(\theta)}_{= \frac{E_f \sin(\delta)}{X_s}}$$

# Power of a Synchronous Machine

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Write Power equation in terms of  $E_f$

$$P = \frac{3|V_t||E_f|\sin(\delta)}{X_s} \checkmark$$

# Power of a Synchronous Machine

$$P = \frac{3V_t E_f \sin(\delta)}{X_s}$$

What about Torque?

Neglect losses (core, copper etc)

$$P = T \omega_s$$

↳ rad/s  
+ Mechanical speed

# Torque of a Synchronous Machine

$$T = \frac{P}{\omega_s}$$

$$T = \frac{3V_t E_f \sin(\delta)}{X_s \omega_s}$$

*mechanical speed*

# Torque of a Synchronous Machine

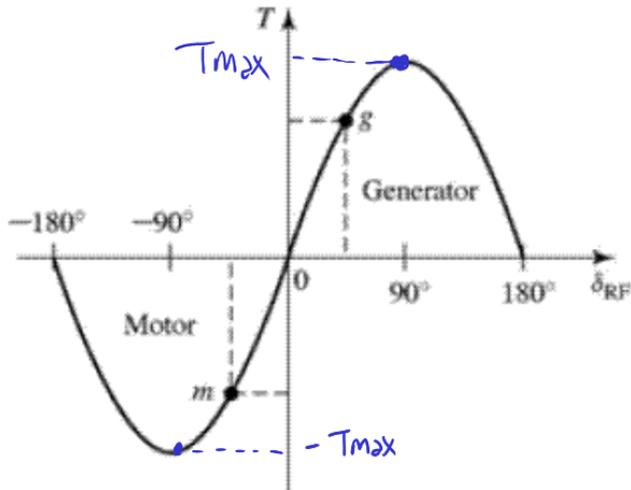
Remember the previous weeks:

$$T = T_{max} \sin(\delta)$$

$$T_{max} = \frac{3V_t E_f}{X_s \omega_s}$$

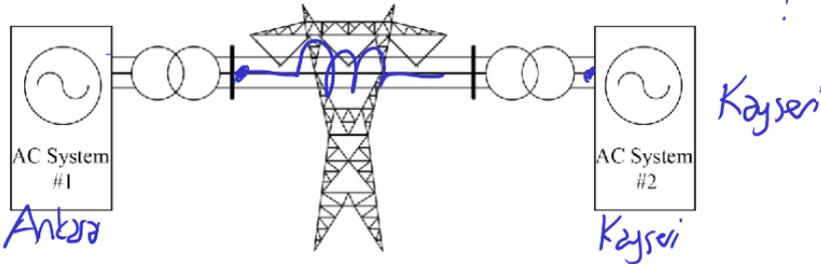
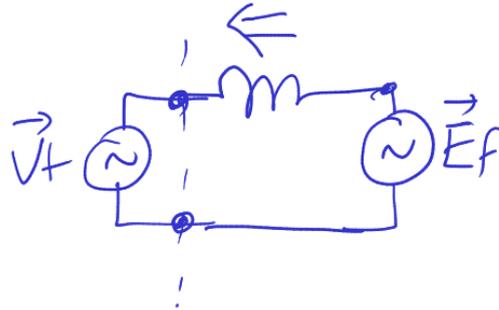
# Torque of a Synchronous Machine

$$T_{max} = \frac{3V_t E_f}{X_s \omega_s} \quad \checkmark$$



# Generalized Power Transfer in AC Systems

$$P = \frac{3|V_t||E_f|\sin(\delta)}{|X_s|}$$



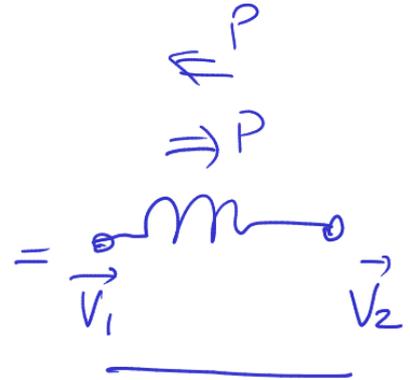
direction of power  $\propto \sin(\delta)$

$$\delta > 0 \Rightarrow P > 0$$

$$\delta < 0 \Rightarrow \underline{\underline{P < 0}}$$

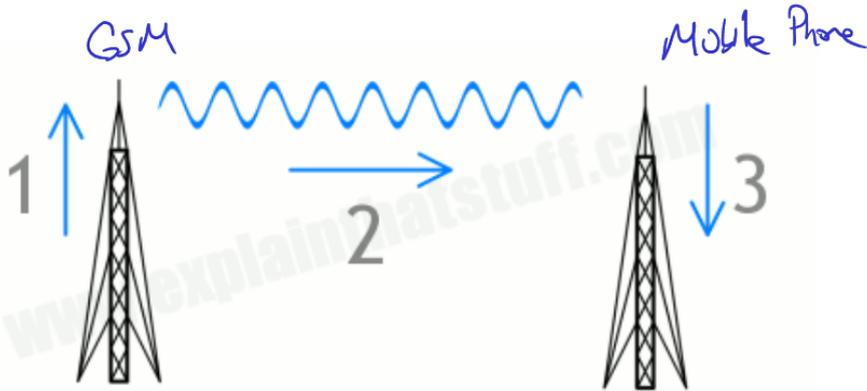
# Generalized Power Transfer in AC Systems

## In Transmission Systems



# Generalized Power Transfer in AC Systems

## In Wireless Communication



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# Generalized Power Transfer in AC Systems

## In Wave Energy Converters

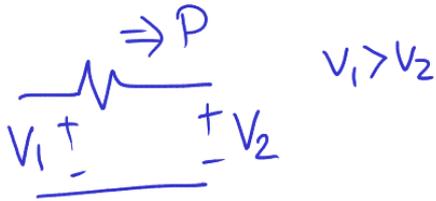


[Pelamis WEC Operation, Full Story.](#)

# Power Flow

## DC Systems:

Power flows from high potential to low potential

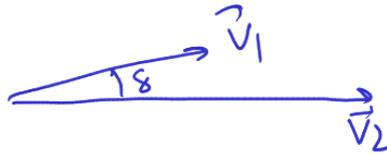


# Power Flow

## DC Systems:

Power flows from high potential to low potential

## AC Systems:



Power flows from leading voltage source to lagging voltage source (sign of load angle,  $\delta$  determines the direction of power flow)

