

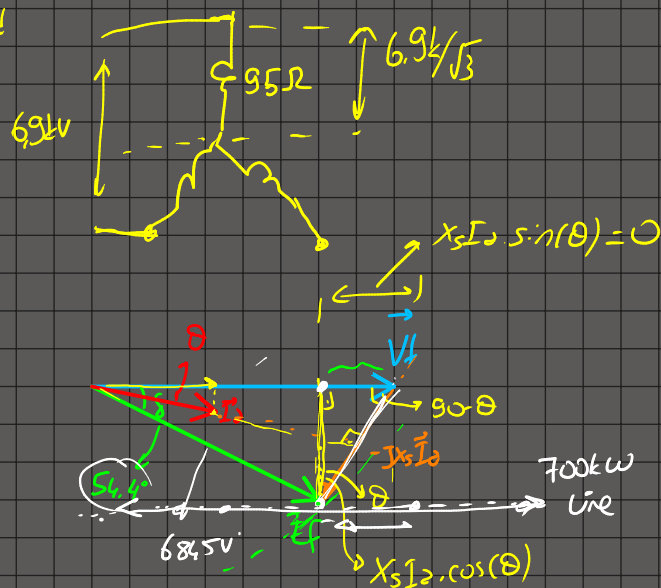
6.9 kV(I-I) 50 Hz synchronous motor has a Δ -connected synchronous reactance of 95 Ohm/phase. For this problem all losses and saturation effect may be neglected.

a) Compute the armature current and pf of the motor when supplying 700kW rated power and the load angle is 54.4 degrees.

b) Compute the maximum power this motor can deliver if its field excitation is kept constant at the value in part a. Compute the power factor and armature current.

c) What should be the minimum percentage increase in the field current for the motor to supply 1 MW power.

d) What should be the excitation voltage for the motor to supply rated power while drawing minimum armature current?



$$a) V_{ph} = \frac{6.9 \text{ kV}}{\sqrt{3}} = 3993 \text{ V}$$

$$P = 3 V_{ph} \cdot I_{ph} \cdot \cos(\theta)$$

$$700 \text{ kW} = 3 \cdot 3993 \cdot I_{ph} \cdot \cos(\theta)$$

$$I_{ph} \cdot \cos(\theta) = 58.6 \text{ A}$$

$$\tan(\delta) = \frac{X_s \cdot I_a \cdot \cos(\theta)}{V_t - X_s \cdot I_a \cdot \sin(\theta)}$$

$$E_f \cdot \sin(\delta) = X_s \cdot I_a \cdot \cos(\theta)$$

$$V_t - X_s \cdot I_a \cdot \sin(\theta) = \frac{95 \cdot 58.6}{\tan(54.4)} = 6845 \text{ V}$$

$$|E_f| = 6845 \text{ V}$$

~~355 V~~
why pf?

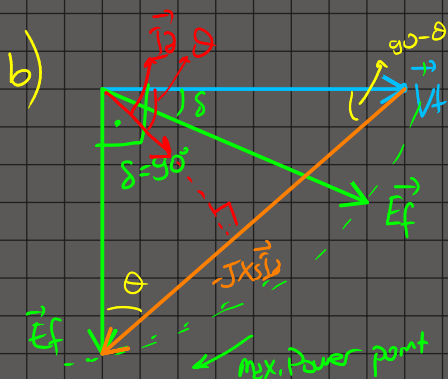
$$X_s \cdot I_a \cdot \sin(\theta) = 0 \Rightarrow \sin(\theta) = 0, \cos(\theta) = 1$$

$$I_a = \sqrt{(58.6 \cdot 95)^2 + 3993^2}$$

$$= 6845 \text{ V}$$

$$\sqrt{V_t^2 + X_s^2 I_a^2} = E_f$$

$$\sqrt{(3993)^2 + (58.6 \cdot 95)^2} = 6845 \text{ V}$$



$$|I_f| \text{ constant} \Rightarrow |E_f| \text{ constant} = 6845 \text{ V}$$

$$P_{max} \Rightarrow \delta = 90^\circ$$

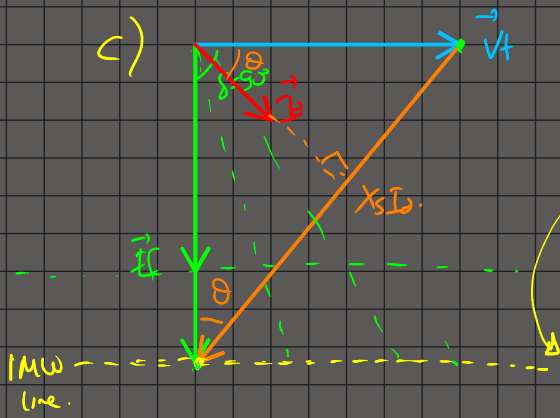
$$|X_s I_a| = \sqrt{V_t^2 + E_f^2} = \sqrt{3993^2 + 6845^2}$$

$$X_s I_a = 7920 \Rightarrow I_a = 83.36 \text{ A}$$

$$\cos(\theta) = \frac{|E_f|}{X_s I_a} \Rightarrow 0.864 \text{ (lagging)}$$

$$P = 3 V_{ph} \cdot I_{ph} \cdot \cos(\theta)$$

$$= 3 \cdot \frac{6.9 \text{ kV}}{\sqrt{3}} \cdot 83.36 \cdot \cos(\theta) = 860.7 \text{ kW}$$



$$P = \frac{3 \cdot V_t \cdot (E_f)}{X_s} \cdot \sin(\delta)$$

$|E_f|$ should be increased by increasing $|I_f|$

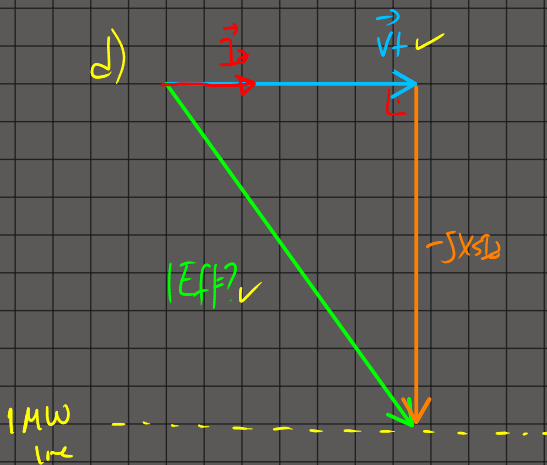
$$P = 3 V_t \cdot I_2 \cdot \cos(\theta) = \underline{1 \text{ MW}}$$

$$E_f \cdot \sin(\delta) = X_s \cdot I_2 \cdot \cos(\theta)$$

$$|E_f| = 7948 \text{ V}$$

$$\frac{7948}{6845} = 1.16 \Rightarrow I_f \text{ should be increased by } \underline{16\%}$$

↑
old value



$$3 V_t I_2 \overset{=1 \text{ in unity pf}}{\cos(\theta)} = 1 \text{ MW}$$

$$I_2 = \underline{83.68 \text{ A}}$$

$$E_f = \sqrt{V_t^2 + X_s I_2^2}$$

$$= \sqrt{3983^2 + (95 \cdot 83.68)^2}$$

$$\boxed{|E_f| = \underline{8892 \text{ V}}}$$

field loss < armature loss

→ $I_2^2 \cdot R_a$ loss decreased compared to part (c)

$I_f^2 \cdot R_f$ loss increased " " " "

