

# EE-463 STATIC POWER CONVERSION-I

## 3-Phase Controlled Rectifiers

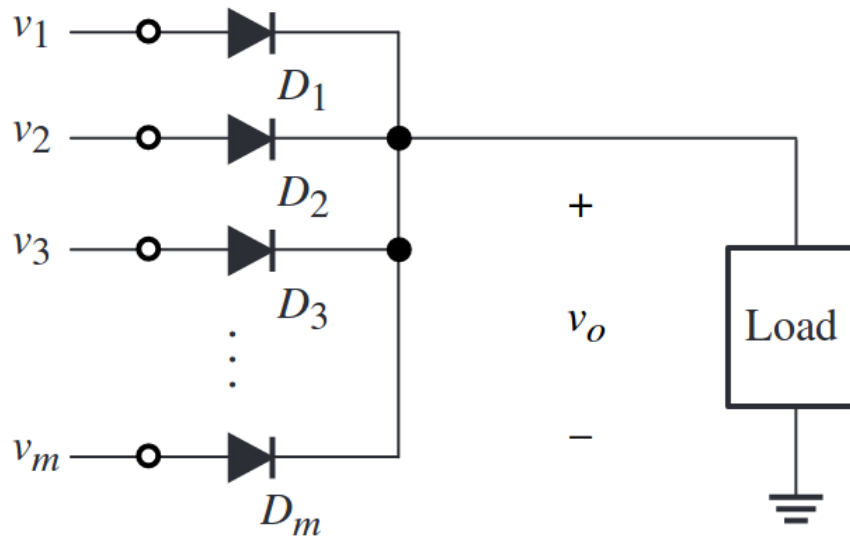
Ozan Keysan

[keysan.me](http://keysan.me)

Office: C-113 • Tel: 210 7586

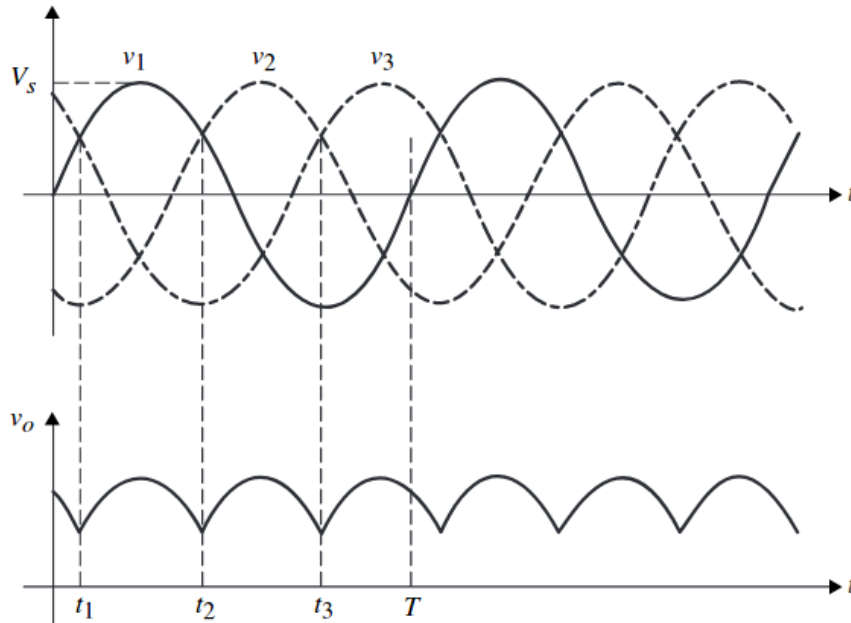
# Review

## N-Phase Half Wave Rectifier



# Review

## 3-Phase Half Wave Diode Rectifier



# Review

3-Phase Half Wave Diode Rectifier Average Voltage?

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3-Phase Half Wave Diode Rectifier Average Voltage?

$$V_{dc} = \frac{3\sqrt{6}}{2\pi} V_{ph,rms}$$

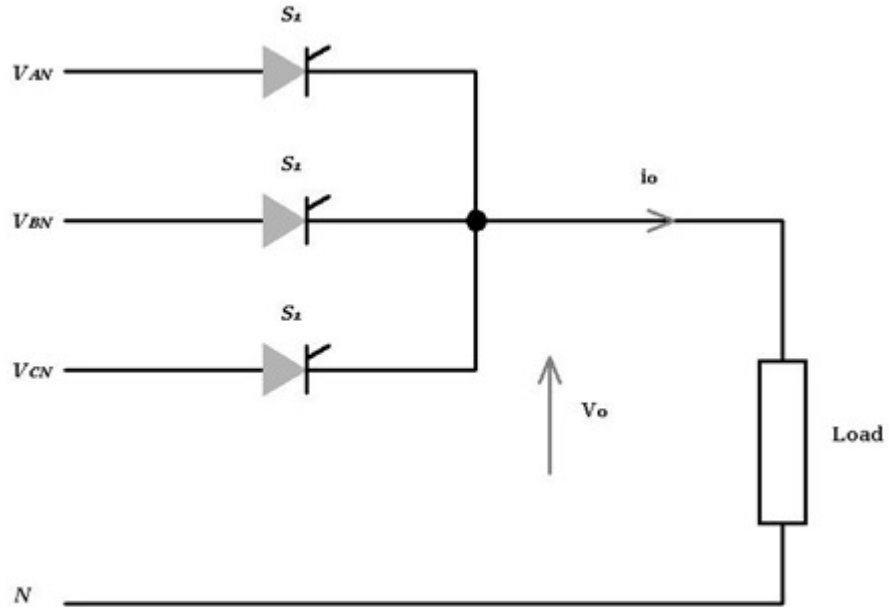
or

$$V_{dc} = \frac{3\sqrt{2}}{2\pi} V_{ll,rms}$$

# Half-bridge Thyristor Rectifier



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Average Voltage?



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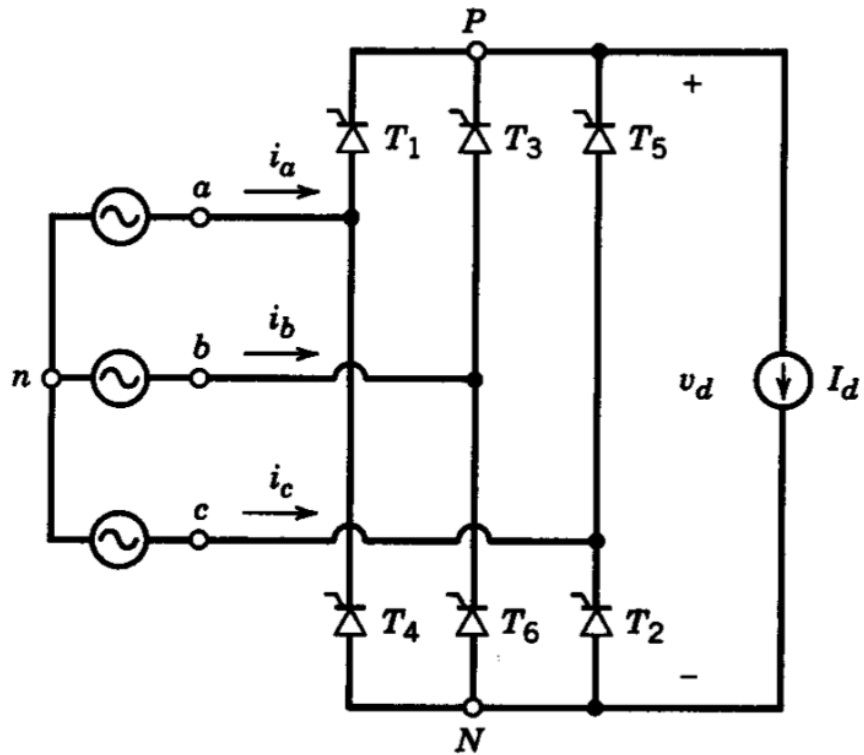
Average Voltage?

$$V_{dc(\alpha)} = \frac{3\sqrt{6}}{2\pi} V_{ph,rms} \cos(\alpha)$$

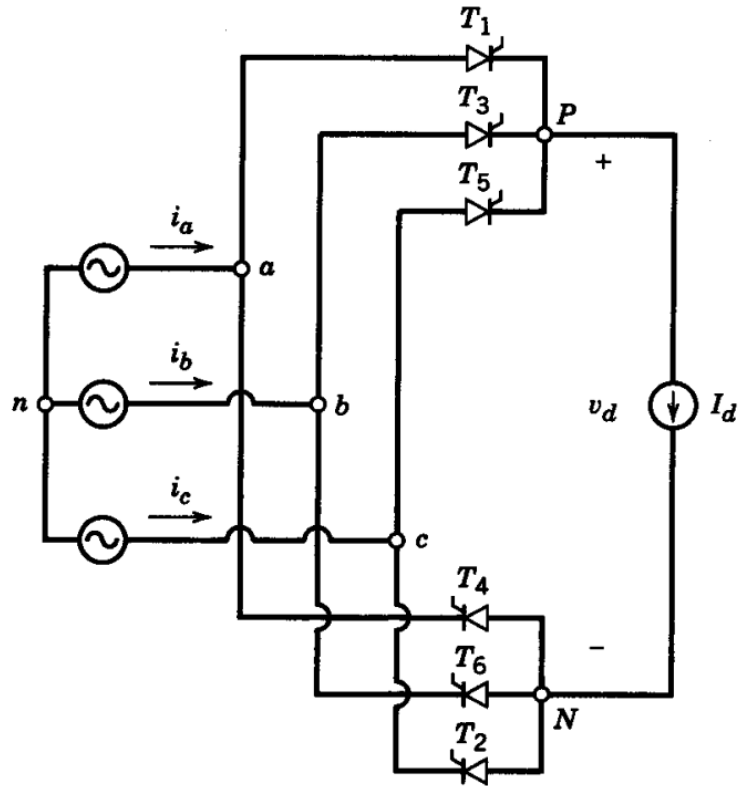
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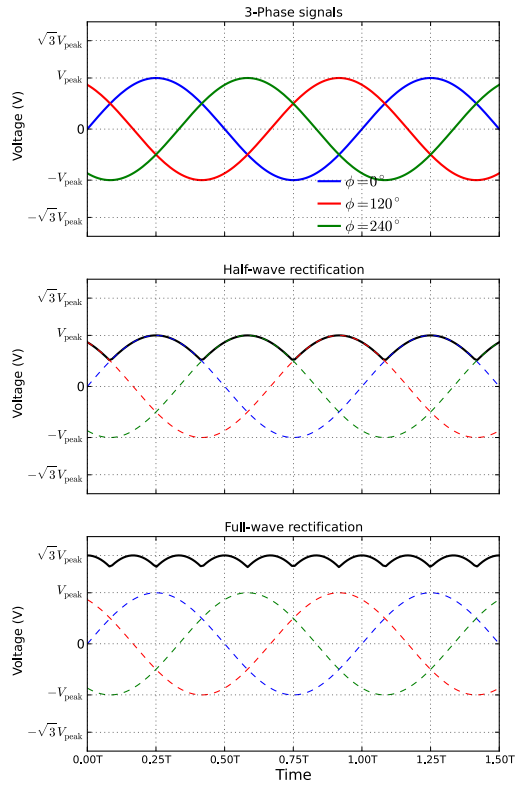
# Full-bridge Thyristor Rectifier



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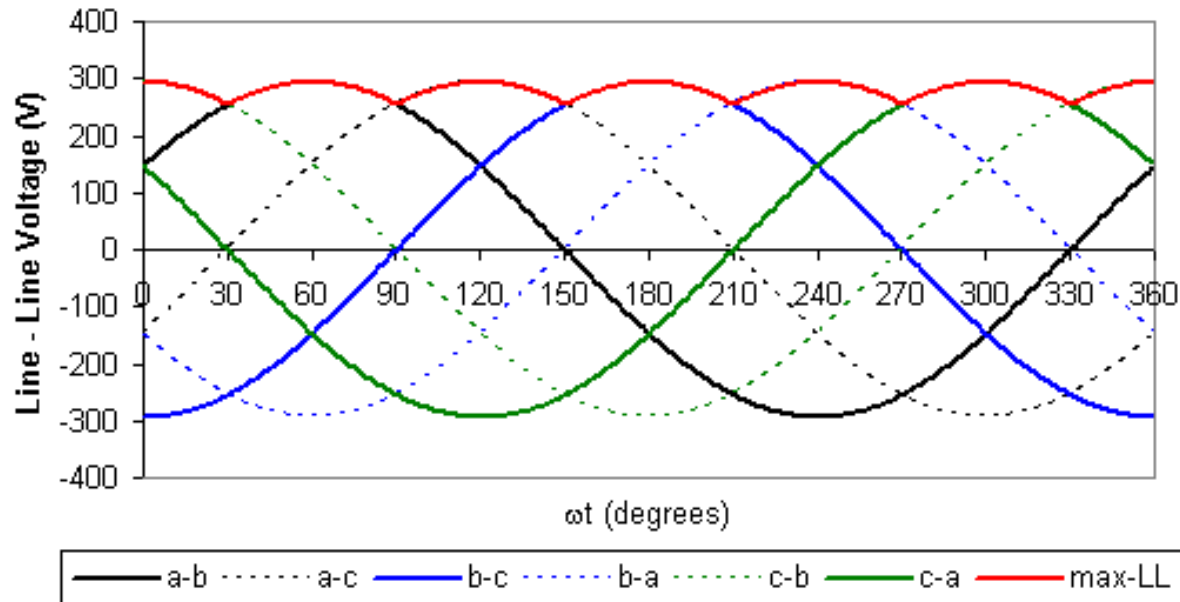


# Diode Rectifier (or $\alpha = 0$ )



# Full-bridge Thyristor Rectifier

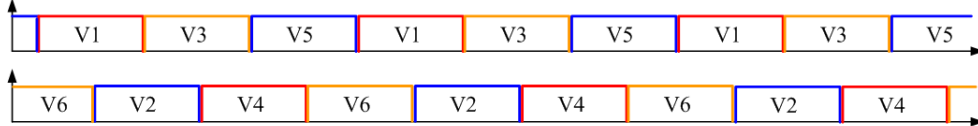
Remember output voltage follows line to line voltages!



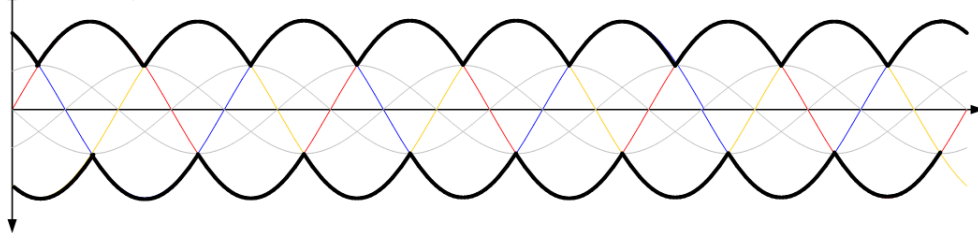
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Remember output voltage follows line to line voltages!

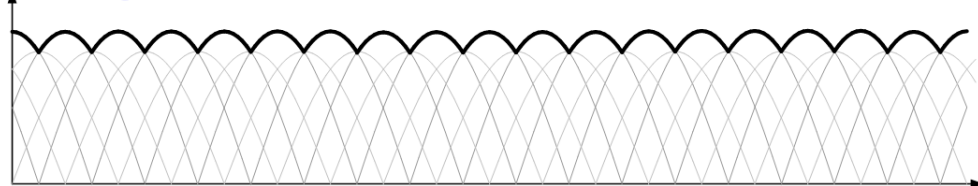
Currents in each valve



DC voltage, line to neutral



DC voltage, line to line

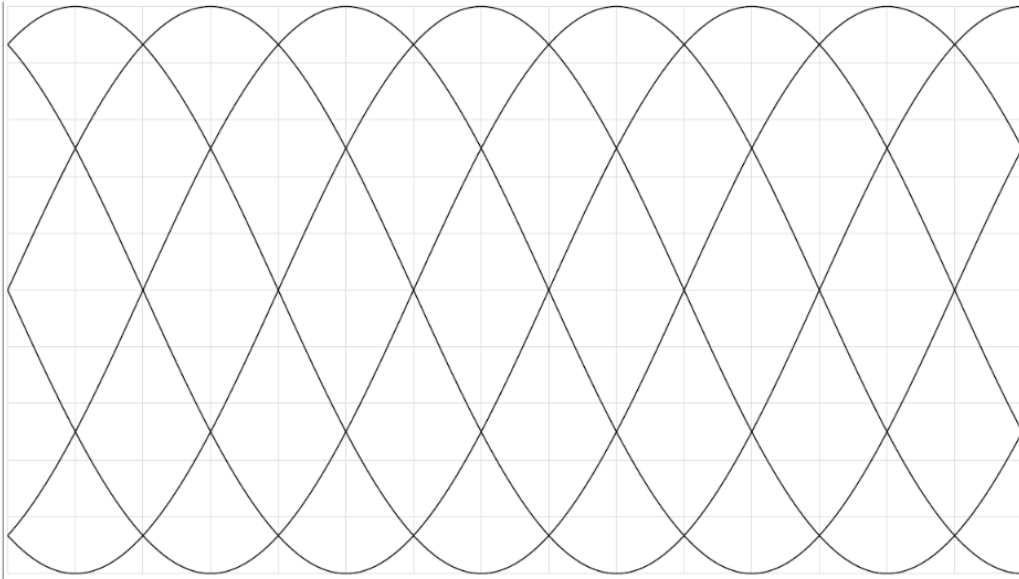


# Full-bridge Thyristor Rectifier

Non-zero firing angle

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Non-zero firing angle



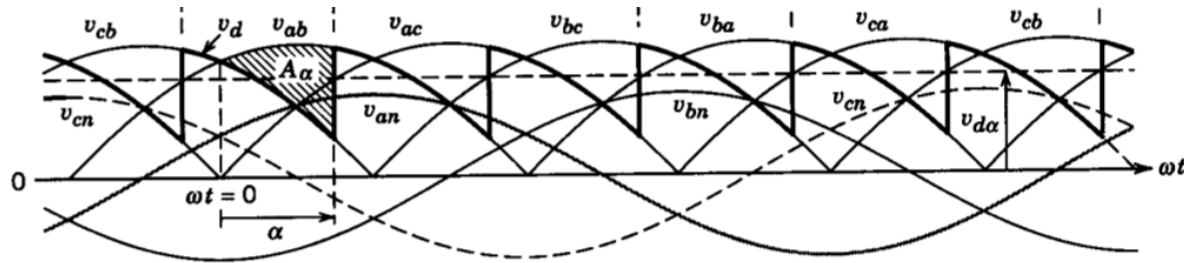


# Full-bridge Thyristor Rectifier

Non-zero firing angle

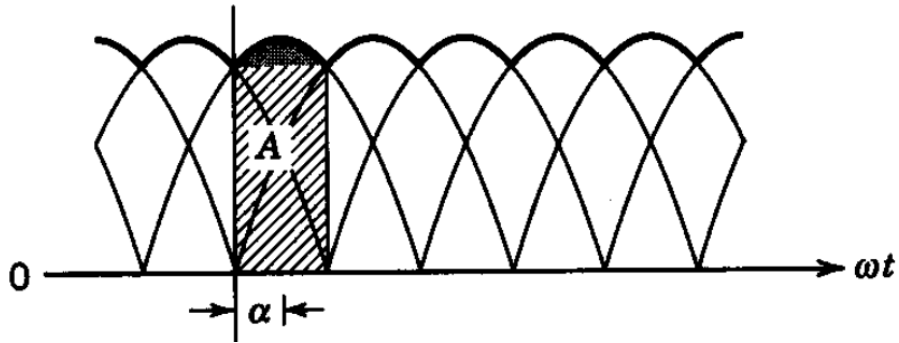
# Full-bridge Thyristor Rectifier

## Non-zero firing angle



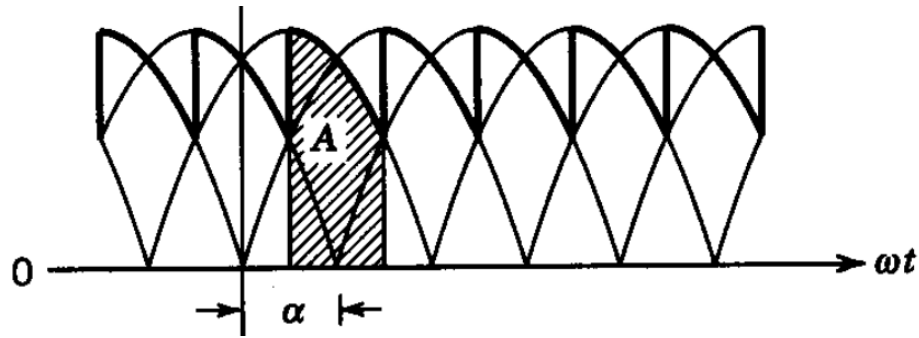
# Output Voltage vs. Firing Angle

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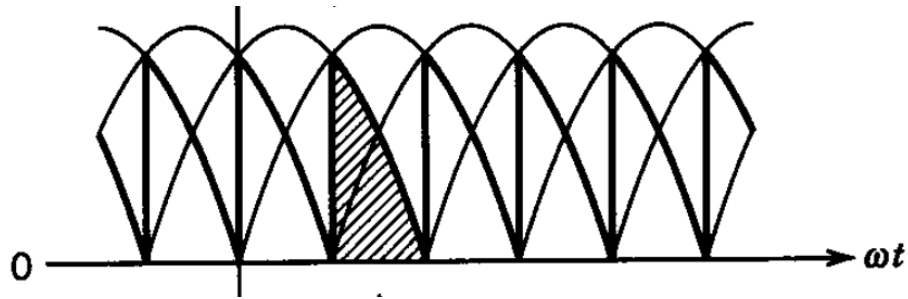
(a)  $\alpha = 0$

# Output Voltage vs. Firing Angle



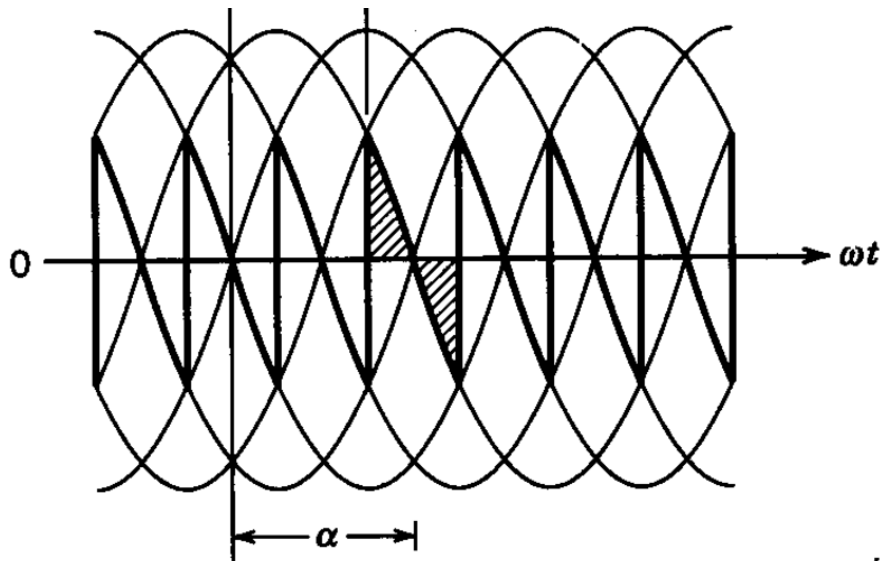
(b)  $\alpha = 30^\circ$

# Output Voltage vs. Firing Angle



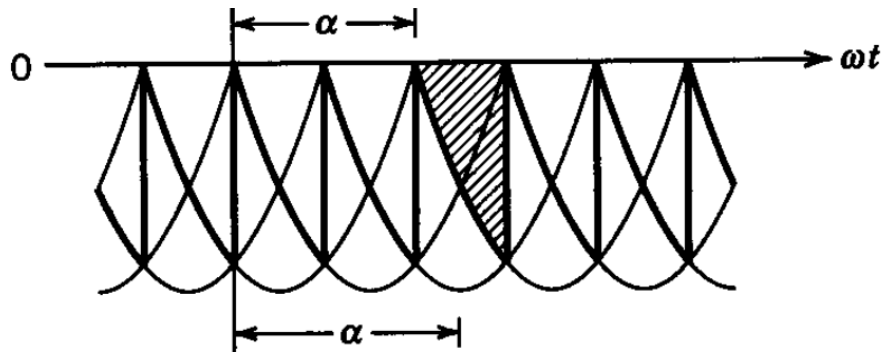
(c)  $\alpha = 60^\circ$

# Output Voltage vs. Firing Angle



(d)  $\alpha = 90^\circ$

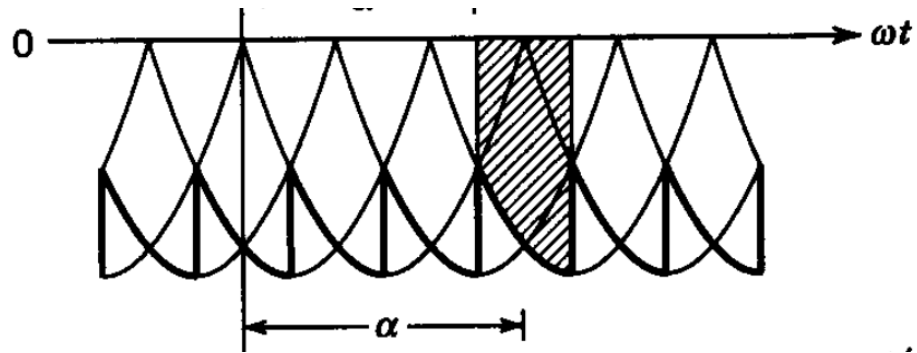
# Output Voltage vs. Firing Angle



(e)  $\alpha = 120^\circ$

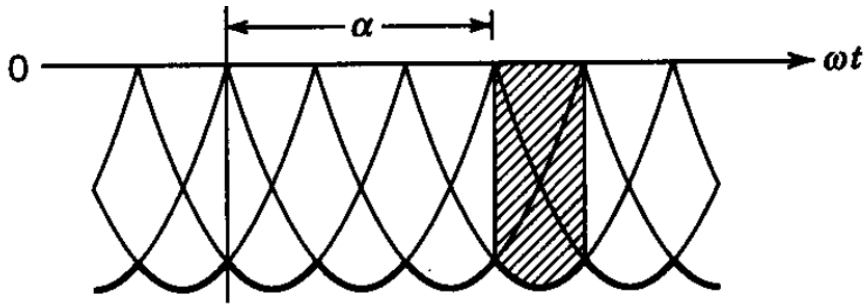


# Output Voltage vs. Firing Angle



(f)  $\alpha = 150^\circ$

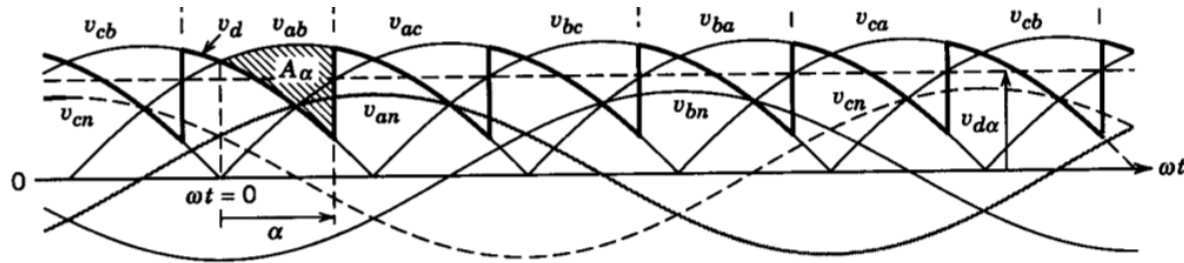
# Output Voltage vs. Firing Angle



(g)  $\alpha = 180^\circ$

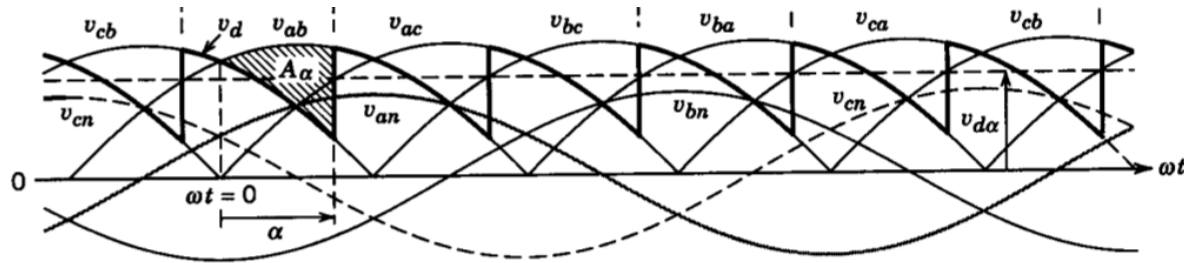
# Full-bridge Thyristor Rectifier

Average output voltage?



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Average output voltage?



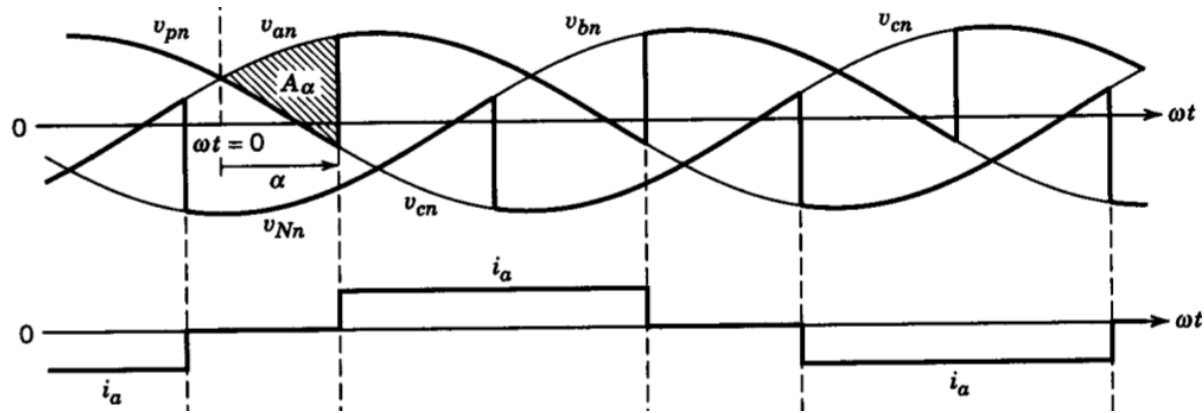
$$V_{d(\alpha)} = \frac{3\sqrt{2}}{\pi} V_{ll,rms} \cos(\alpha)$$

# Full-bridge Thyristor Rectifier

What about the current?

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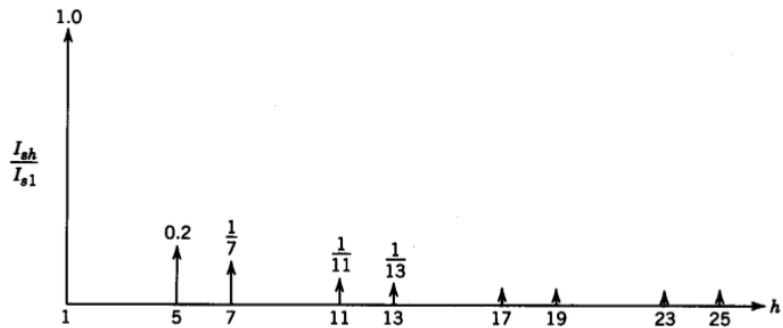
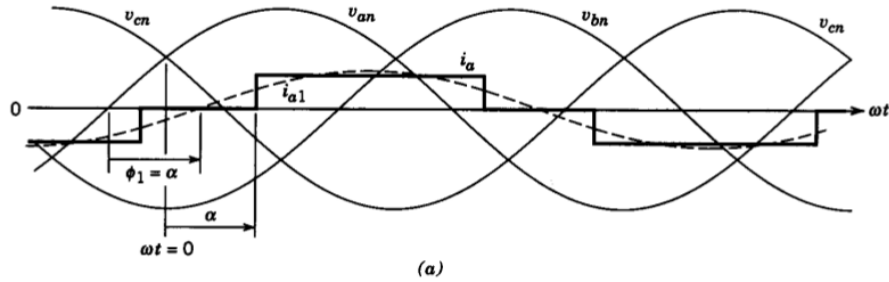


# Current Waveform: No triple harmonics

Comparison: [Single Phase](#), [Three Phase](#)

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# Full-bridge Thyristor Rectifier

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$$\text{Fundamental RMS: } I_{s1} = \frac{\sqrt{6}}{\pi} = 0.78I_d$$

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# Full-bridge Thyristor Rectifier

Current Waveform:

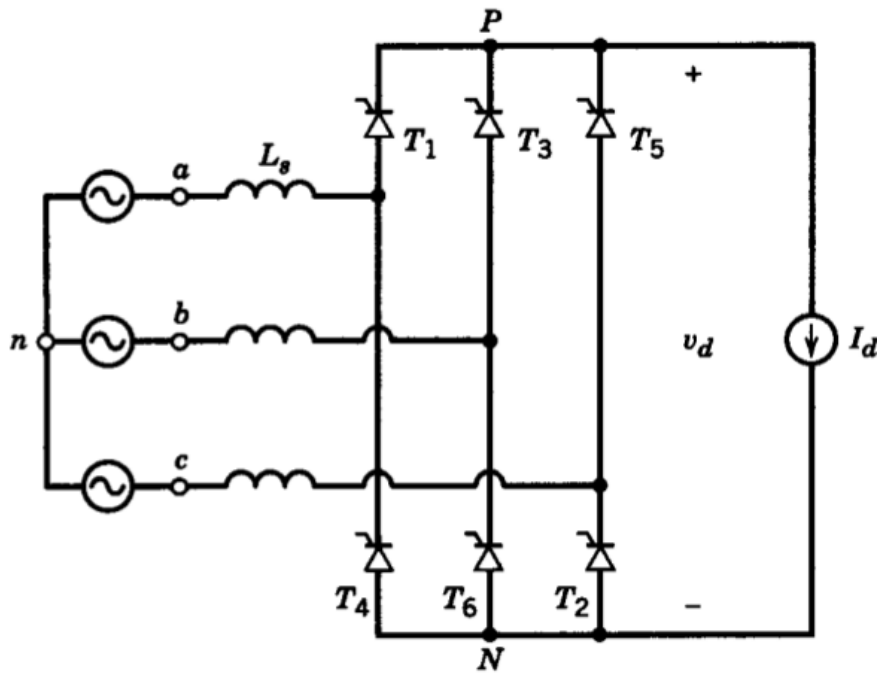
$$\text{Fundamental RMS: } I_{s1} = \frac{\sqrt{6}}{\pi} I_d = 0.78 I_d$$

$$\text{Total RMS: } I_s = \sqrt{\frac{2}{3}} I_d = 0.816 I_d$$

THD= 31.08 %

# Effect of $L_s$ (Commutation)

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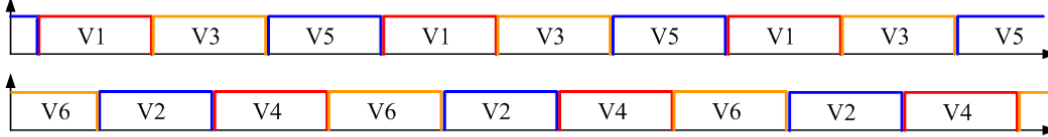


# Effect of $L_s$ (Commutation)

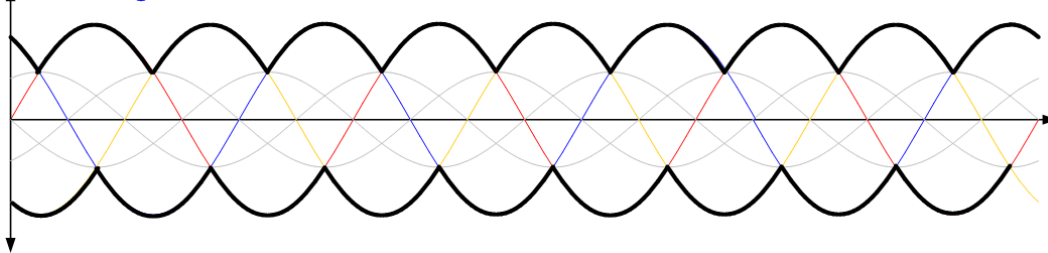


# Commutation: $\alpha = 0, L_s = 0$

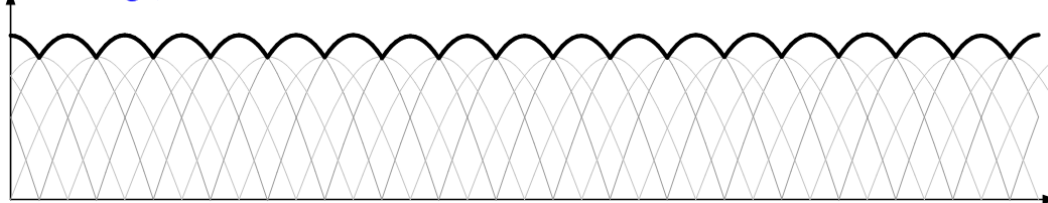
Currents in each valve



DC voltage, line to neutral

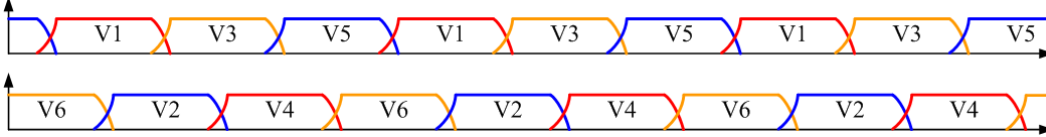


DC voltage, line to line

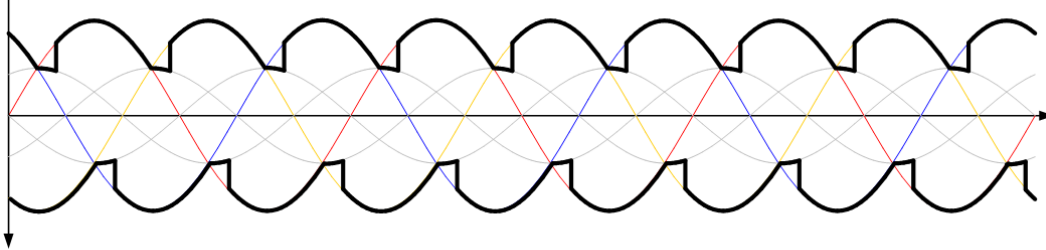


# Commutation: $\alpha = 0, L_s > 0$

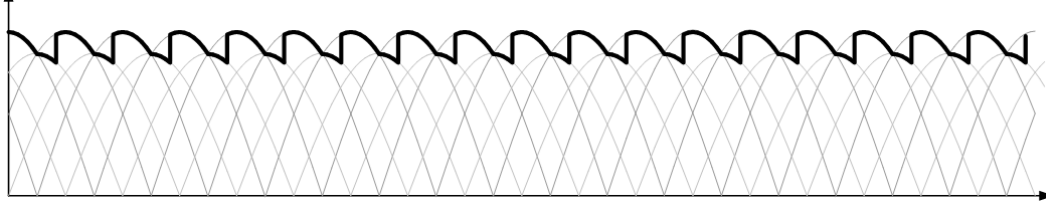
Currents in each valve



DC voltage, line to neutral

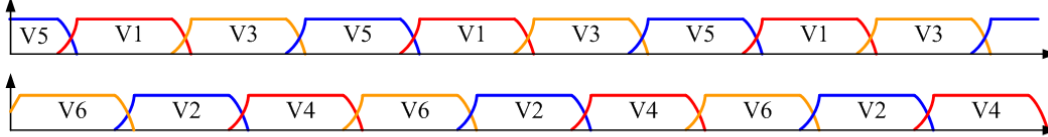


DC voltage, line to line

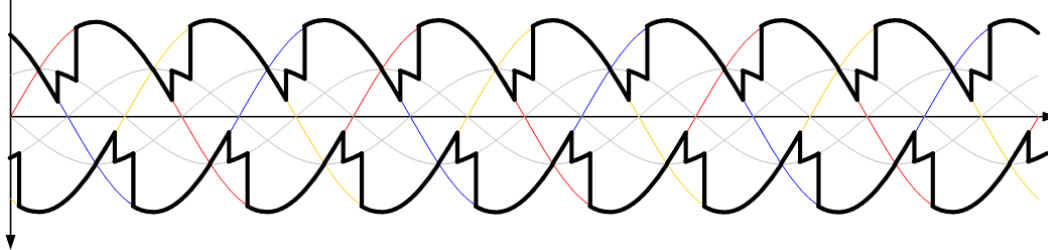


# Commutation: $\alpha = 20, L_s > 0$

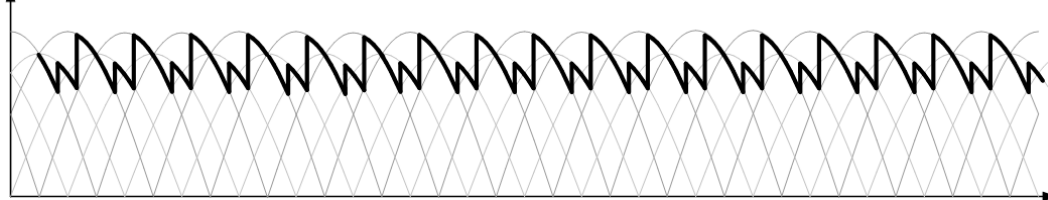
Currents in each valve



DC voltage, line to neutral

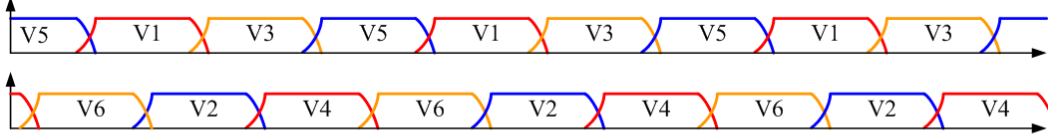


DC voltage, line to line

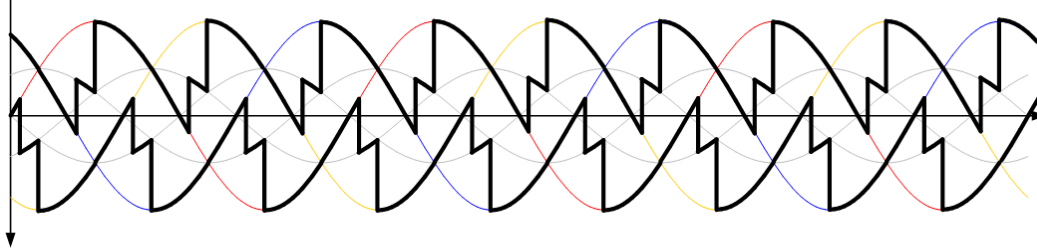


# Commutation: $\alpha = 40, L_s > 0$

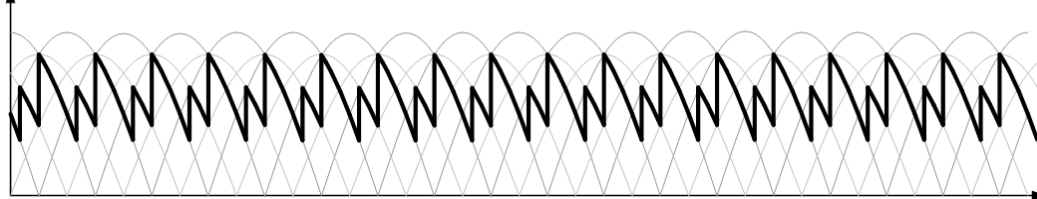
Currents in each valve



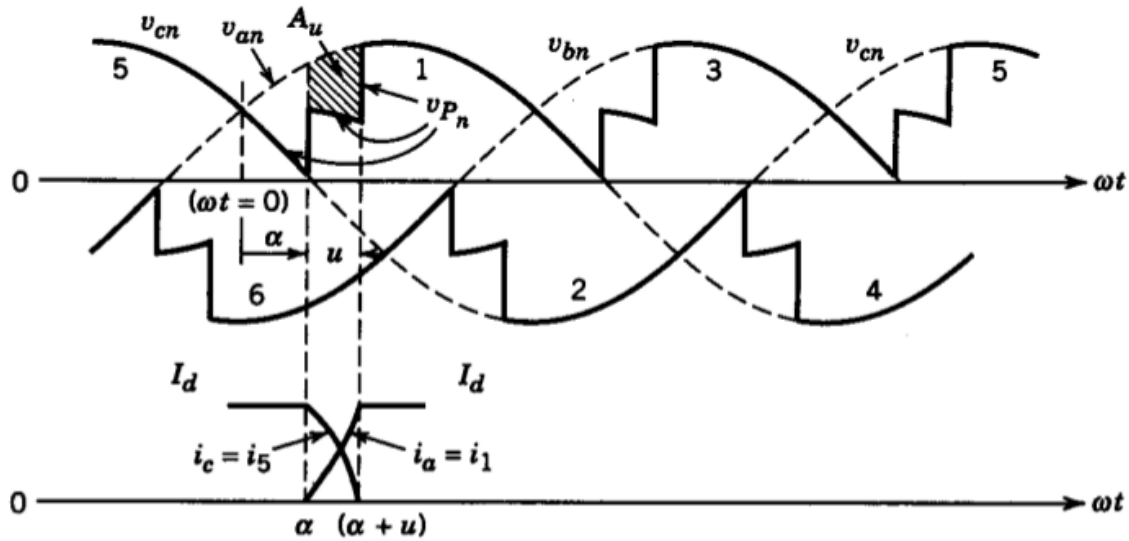
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DC voltage, line to line



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$$A_u = \omega L_s I_d \text{ (repeats itself every } \pi/3 \text{)}$$

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$$V_{d(\alpha)} = \frac{3\sqrt{2}}{\pi} V_{ll,rms} \cos(\alpha) - \frac{3\omega L_s I_d}{\pi}$$



# Effect of $L_s$ (Commutation)

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Introduces a voltage drop on the rectified side

- Single Phase:  $\frac{2\omega L_s}{\pi} I_a$

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# Effect of $L_s$ (Commutation)

Introduces a voltage drop on the rectified side

- Single Phase:  $\frac{2\omega L_s}{\pi} I_a$

- Three Phase:  $\frac{3\omega L_s}{\pi} I_a$

- Resultant voltage in a 3-ph rectifier:

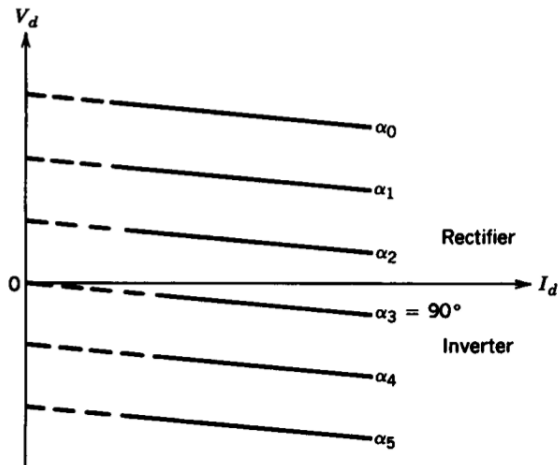
$$V_{d\alpha} = \frac{3\sqrt{2}}{\pi} V_{l-l} \cos(\alpha) - \frac{3\omega L_s}{\pi} I_a$$

# Inverter Mode of Operation

## Two Quadrant Operation

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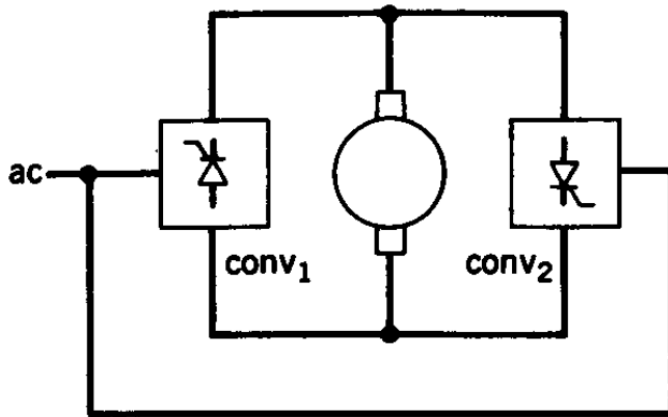


Two quadrant operation with source side voltage (i.e. DC motor)

How can you obtain four-quadrant operation?

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Use two separate converters

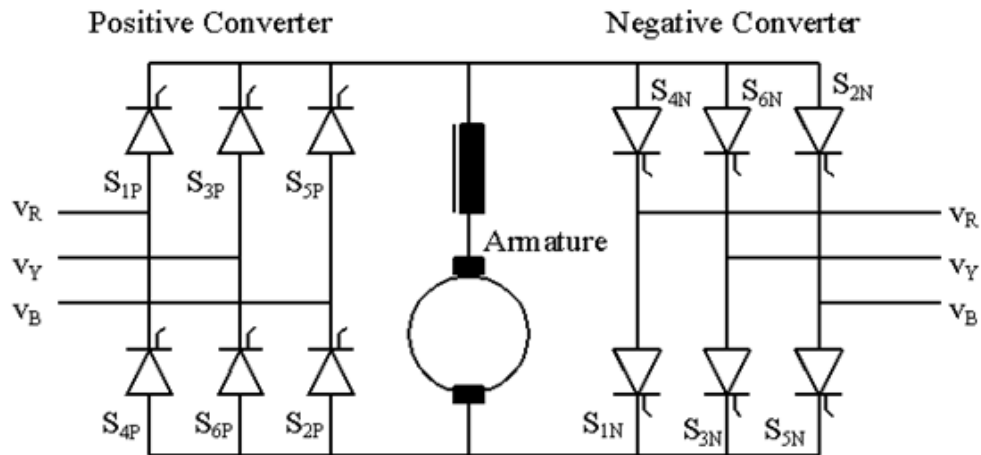


Ref: Mohan Chapter 13 DC Motor Drives



# How can you obtain four-quadrant operation?

## Use two separate converters



Ref: Mohan Chapter 13 DC Motor Drives

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