

# EE-464 STATIC POWER CONVERSION-II

## Other PWM Techniques

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# Hysteresis (Bang-Bang) PWM

# Hysteresis (Bang-Bang) PWM

You already implemented in the first semester

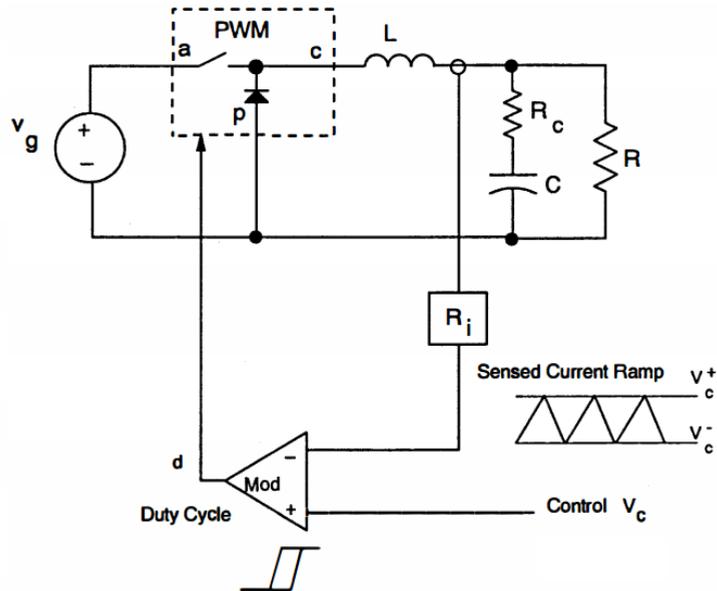
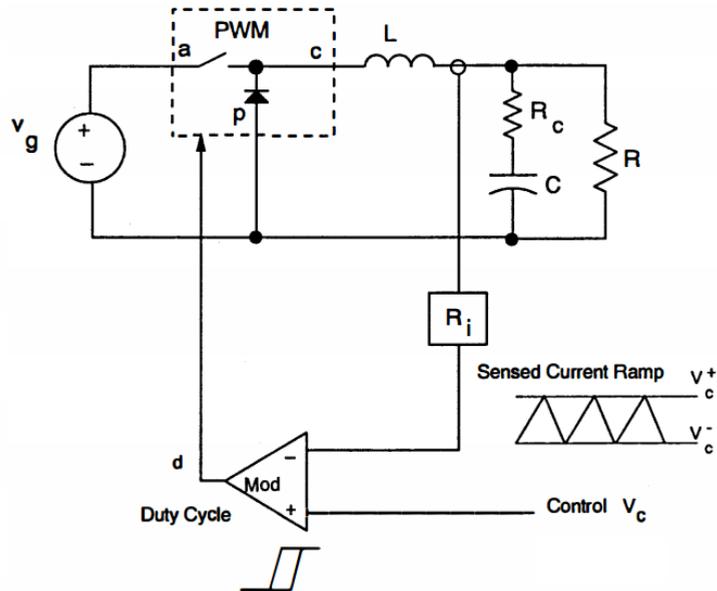


Figure 2.2. Buck Converter with Hysteretic Current-Mode Control: A control sig-

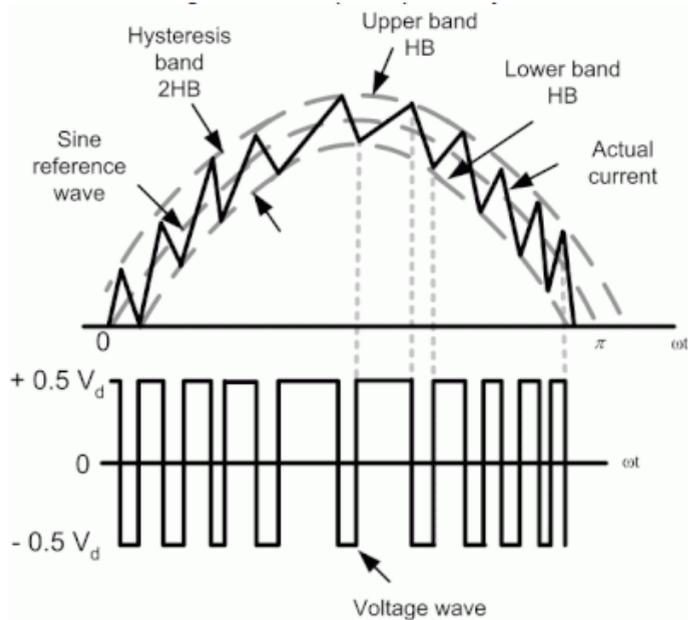
# Hysteresis (Bang-Bang) PWM

If your current is higher than your reference, reduce the current (switch off), if not increase the current (Switch ON)



# Hysteresis (Bang-Bang) PWM

For an inverter, just change your reference current to a sinusoidal waveform instead of a constant reference.



# Hysteresis (Bang-Bang) PWM

# Hysteresis (Bang-Bang) PWM

- . The switching frequency is varying

# Hysteresis (Bang-Bang) PWM

- The switching frequency is varying
- Difficult to design filter (because of varying  $f_s$ )

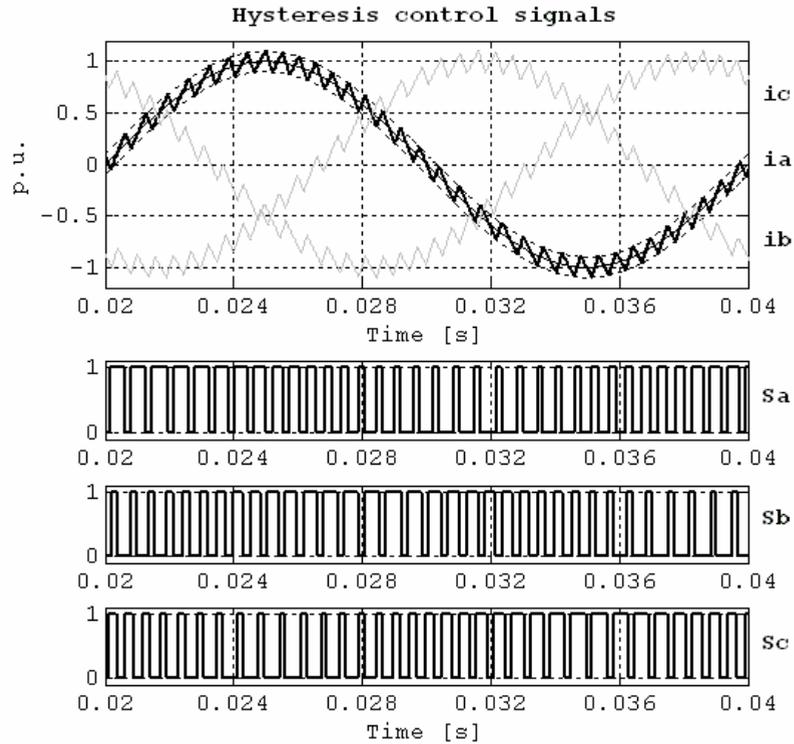
# Hysteresis (Bang-Bang) PWM

- The switching frequency is varying
- Difficult to design filter (because of varying  $f_s$ )
- Can induce side-band harmonics

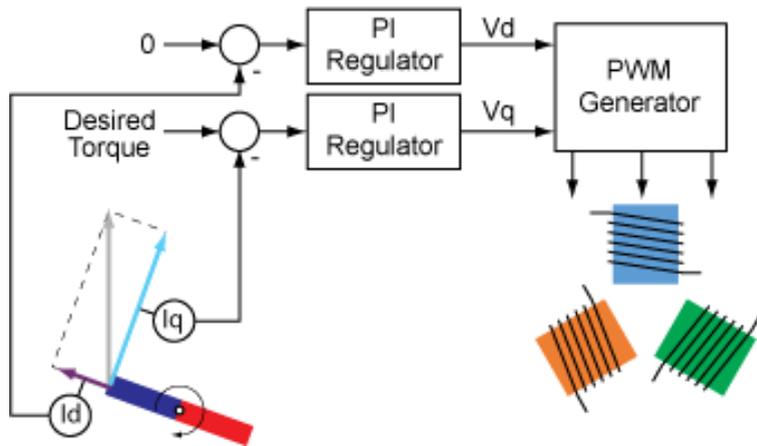
# Hysteresis (Bang-Bang) PWM

- The switching frequency is varying
- Difficult to design filter (because of varying  $f_s$ )
- Can induce side-band harmonics
- Simple control and implementation

# Hysteresis (Bang-Bang) PWM



# Field Oriented Control (FOC) in Electrical Machines



- [What is FOC?](#)
- [Field oriented Control of PM Motors](#)

# How to aim to a moving target?

# How to aim to a moving target?



# Some Useful Mathematical Tools

# Some Useful Mathematical Tools

- . Clarke Transformation
- . Park Transformation

# Clarke Transformation

(a-b-c) to  $\alpha\beta$  Transformation

From three-phase to two orthogonal phase transformation

# Clarke Transformation

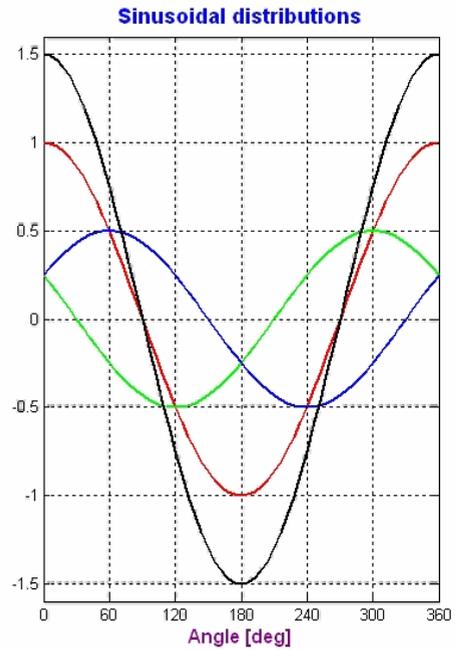
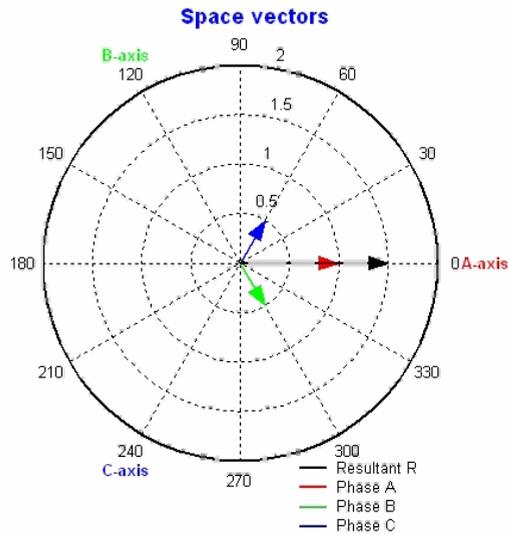
(a-b-c) to  $\alpha\beta$  Transformation

From three-phase to two orthogonal phase transformation

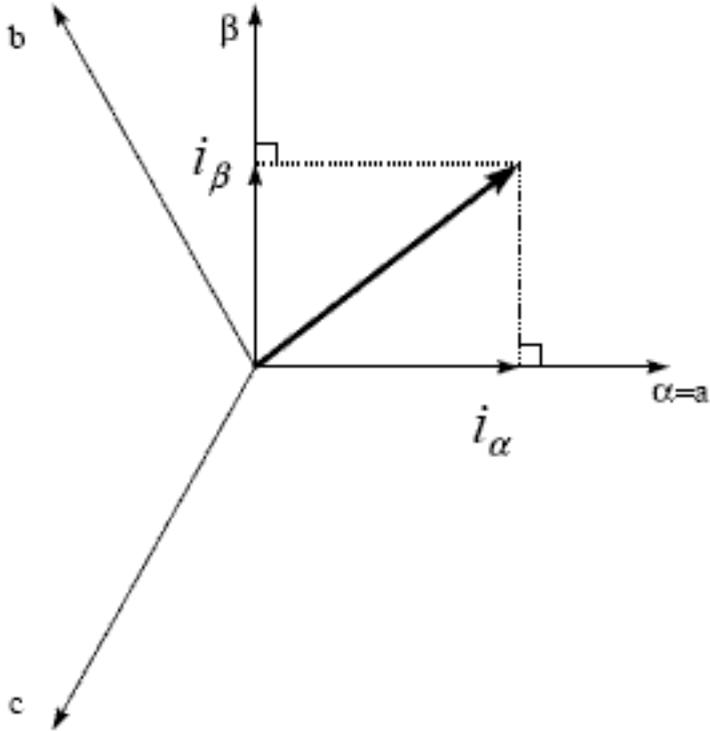
Main Idea: In a balanced three-phase system,

$I_a + I_b + I_c = 0$  so there is redundant information and system can be reduced to two variables.

# How do you define the resultant (black) phasor?



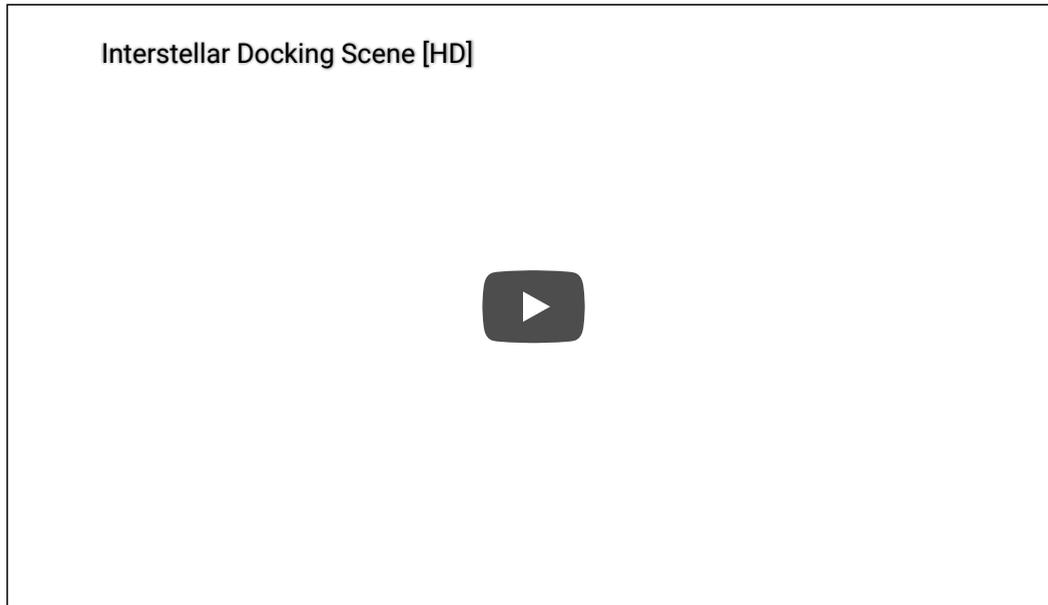
# Clarke Transformation



# Clarke Transformation

$$i_{\alpha\beta}(t) = \frac{2}{3} \begin{bmatrix} 1 & -\frac{1}{2} & -\frac{1}{2} \\ 0 & \frac{\sqrt{3}}{2} & -\frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} i_a(t) \\ i_b(t) \\ i_c(t) \end{bmatrix}$$

# Park Transformation in Space



i.e. [Interstellar - Docking Scene](#)

# Park Transformation

# Park Transformation

From stationary frame to rotary frame

# Park Transformation

From stationary frame to rotary frame

Instead of dealing with sinusoidal signals, just use the magnitudes.

# Park Transformation

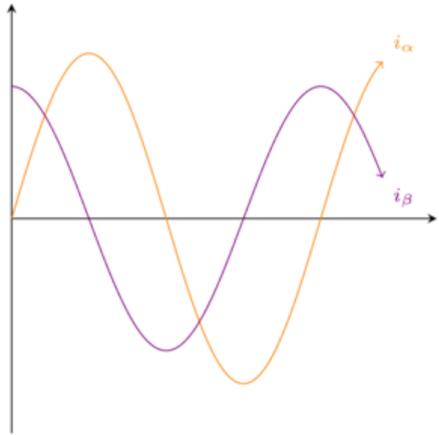
From stationary frame to rotary frame

Instead of dealing with sinusoidal signals, just use the magnitudes.

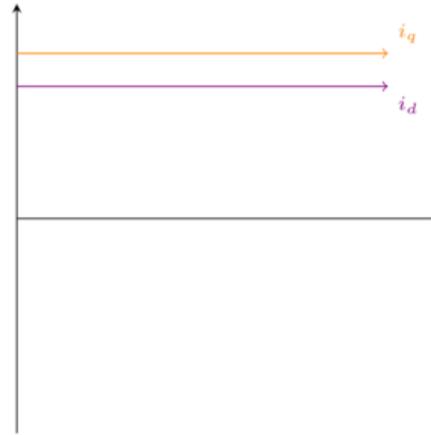
When reconstructing signals use the rotor position information

# Park Transformation

Torque- and flux producing currents  
(from a stationary reference frame)



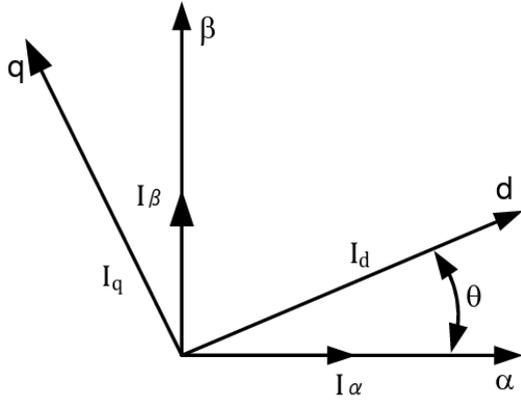
Torque- and flux producing currents  
(from a rotating reference frame)



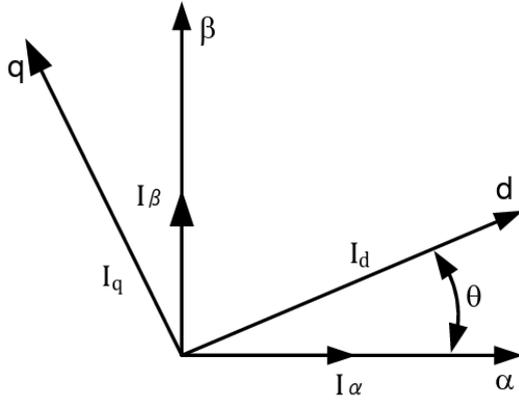
Park  
Transformation

# Park Transformation

# Park Transformation

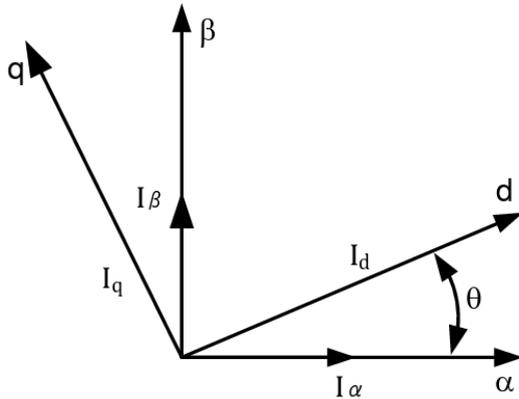


# Park Transformation



$$I_d = I_\alpha \cos(\theta) + I_\beta \sin(\theta)$$

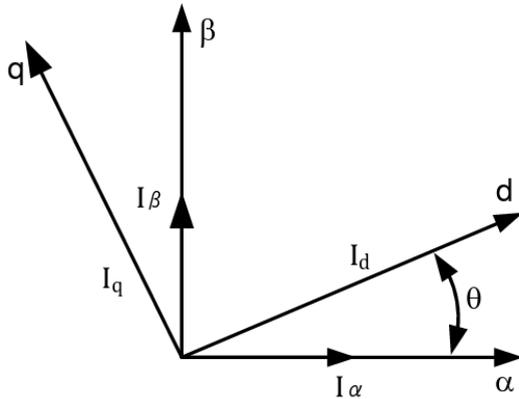
# Park Transformation



$$I_d = I_\alpha \cos(\theta) + I_\beta \sin(\theta)$$

$$I_q = I_\beta \cos(\theta) - I_\alpha \sin(\theta)$$

# Park Transformation

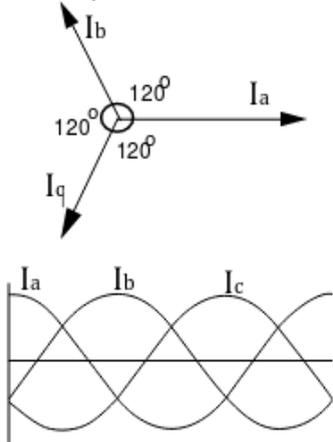


$$I_d = I_\alpha \cos(\theta) + I_\beta \sin(\theta)$$

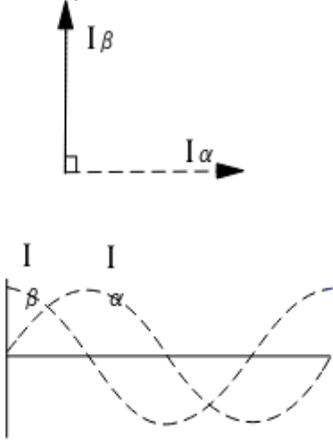
$$I_q = I_\beta \cos(\theta) - I_\alpha \sin(\theta)$$

# Reference Frames

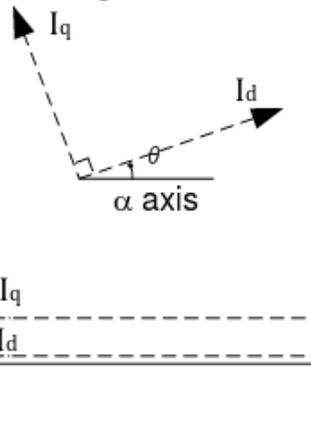
Three-phase reference frame



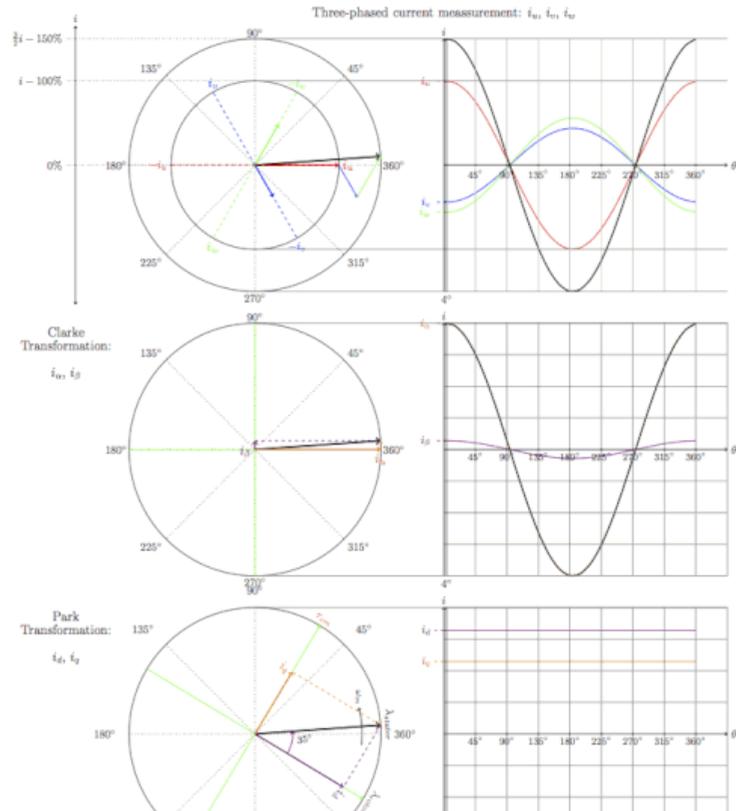
Two-phase reference frame



Rotating reference frame



# Clarke and Park Transformations



# Torque and Flux Control

$I_d$ : Proportional to flux in the air-gap

$I_q$ : Proportional to torque generated

# Inverse Transforms

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Required to apply reference voltage and current waveforms (sinusoidals)

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- Inverse Park Transform
- Inverse Clarke Transform

# Inverse Park Transform

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From rotation frame to stationary frame

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From rotation frame to stationary frame

$$I_{\alpha} = I_d \cos(\theta) - I_q \sin(\theta)$$

# Inverse Park Transform

From rotation frame to stationary frame

$$I_{\alpha} = I_d \cos(\theta) - I_q \sin(\theta)$$

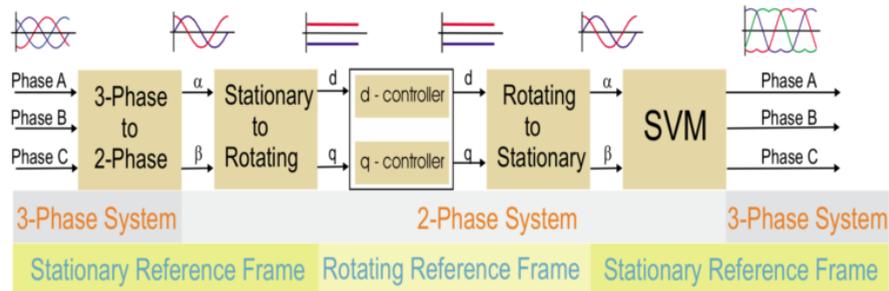
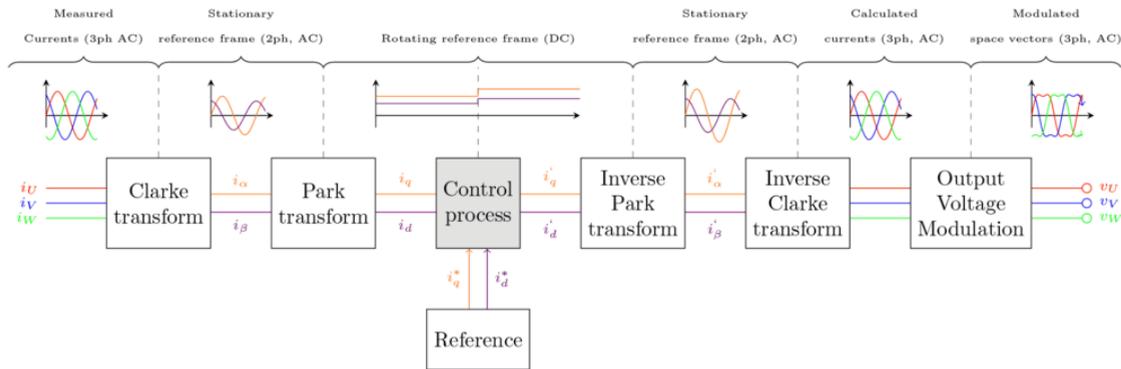
$$I_{\beta} = I_q \cos(\theta) + I_d \sin(\theta)$$

# Inverse Clarke Transform

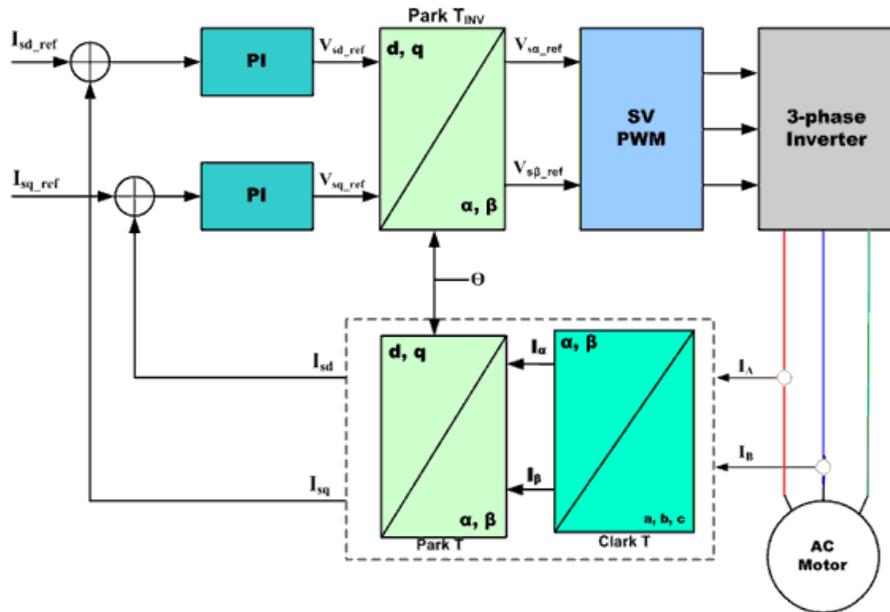
From two-axis orthogonal plane to 3-phase stationary frame.

$\alpha, \beta$	$\rightarrow$	<b>a, b, c</b>
$i_a = i_\alpha$		
$i_b = -\frac{1}{2} \cdot i_\alpha + \frac{\sqrt{3}}{2} \cdot i_\beta$		
$i_c = -\frac{1}{2} \cdot i_\alpha - \frac{\sqrt{3}}{2} \cdot i_\beta$		

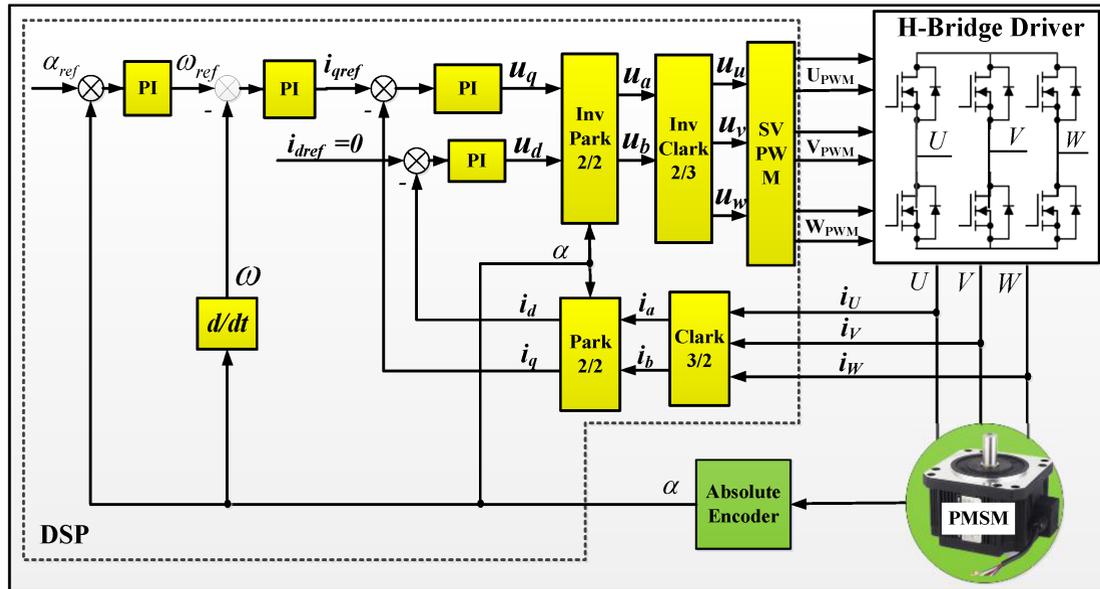
# Whole Workflow



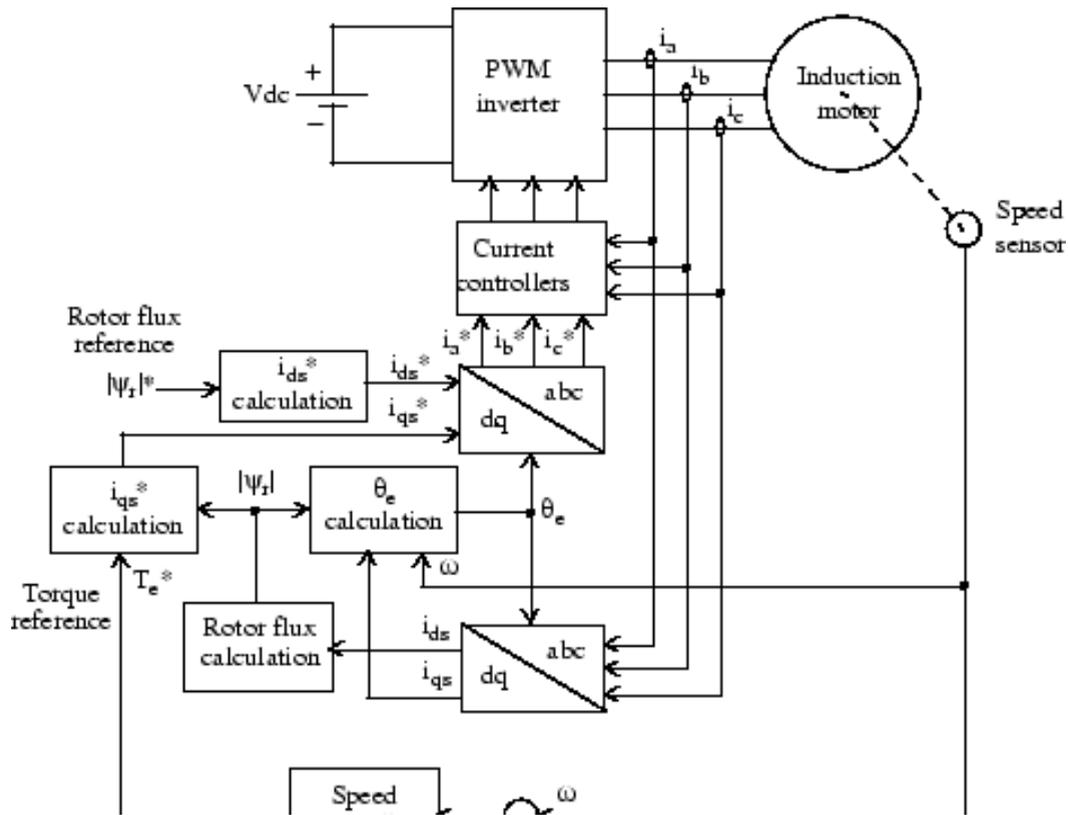
# Classical Vector Control Diagram



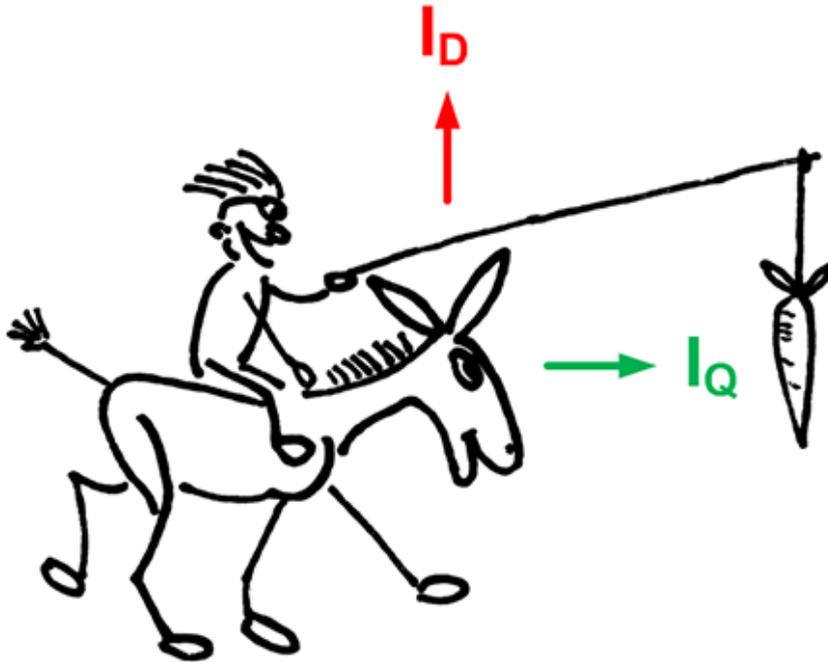
# Vector Control in PMSM



# Vector Control in Induction Motors



# Summary



# Further Reading

[Vector Control for Dummies](#)

[What is Field Oriented Control?](#)

[Field Oriented Control](#)

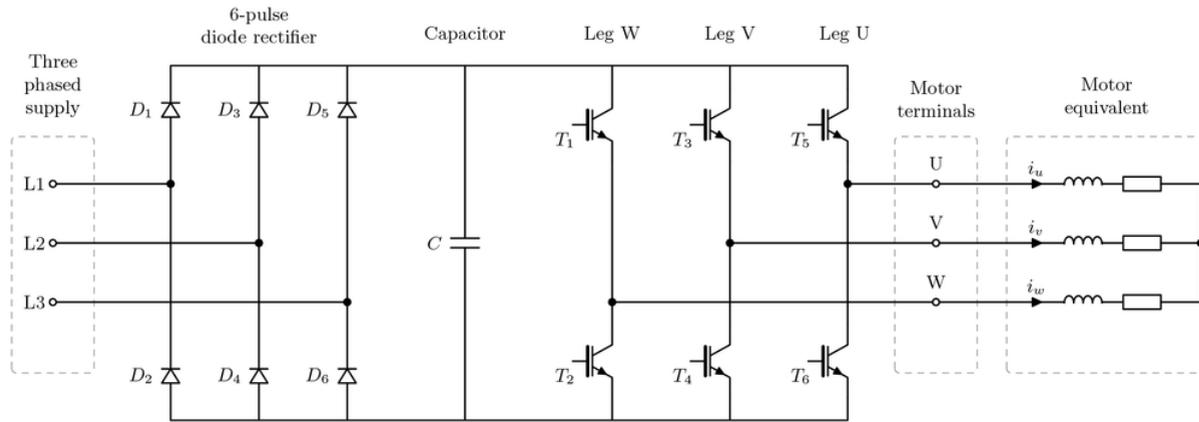
[Field Oriented Control of AC Motors](#)

[Sensorless PMSM Field Oriented Control](#)

[Space Vector PWM](#)

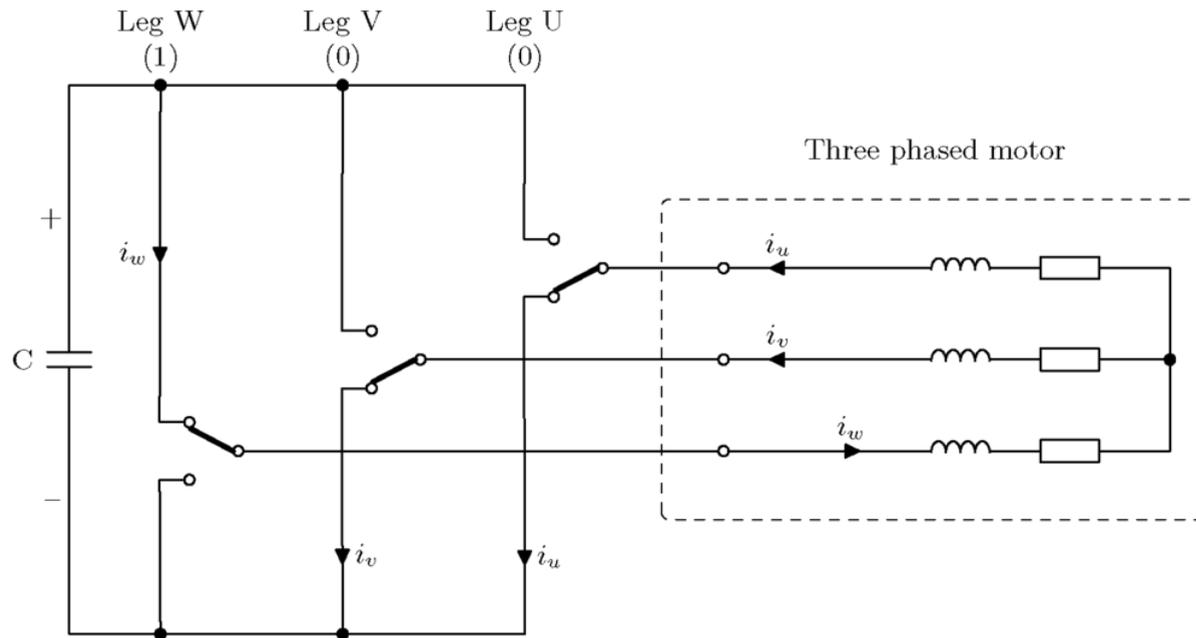
# 3-Phase Two-Level Inverter

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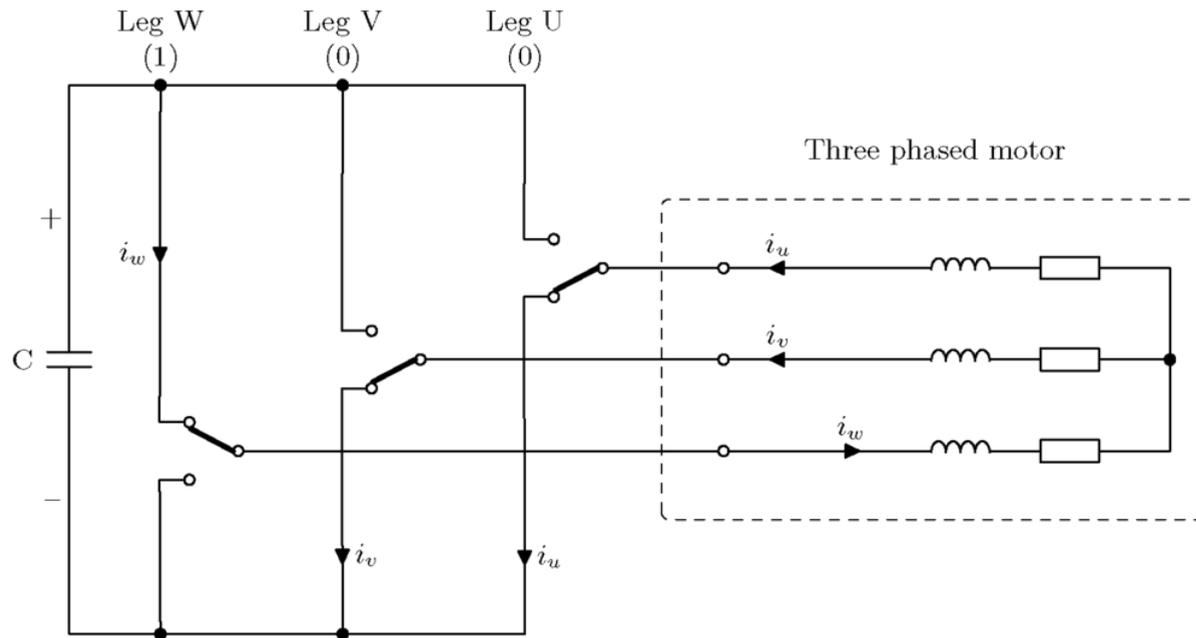
Anti-parallel diodes are not shown.

# 3-Phase Two-Level Inverter



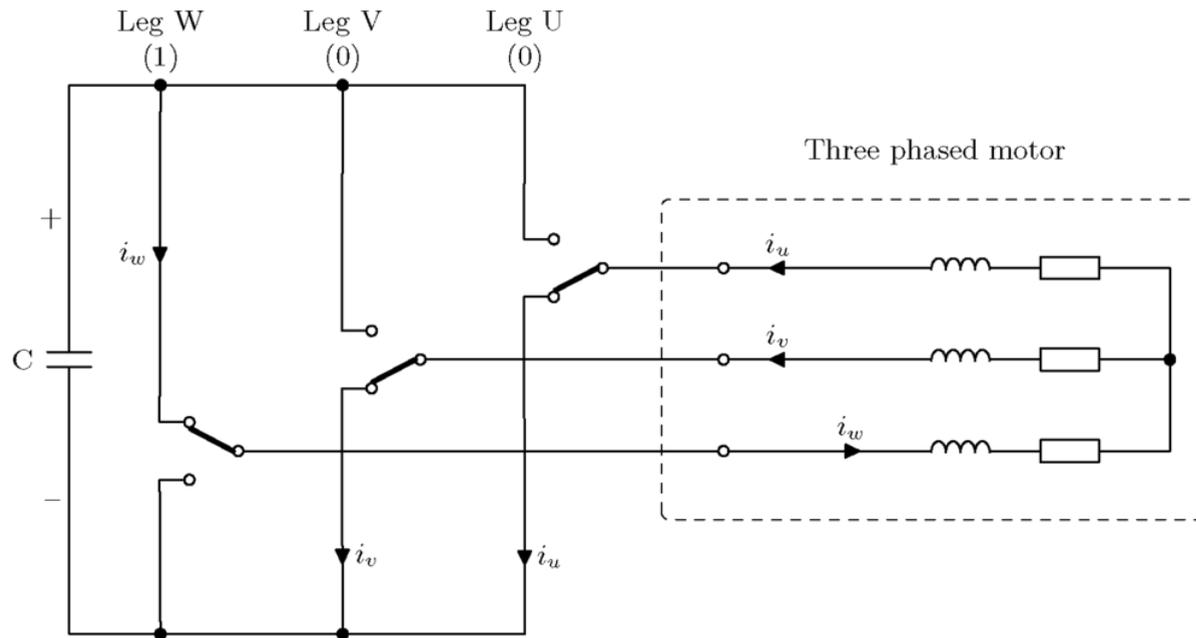
Each leg has two positions:

# 3-Phase Two-Level Inverter



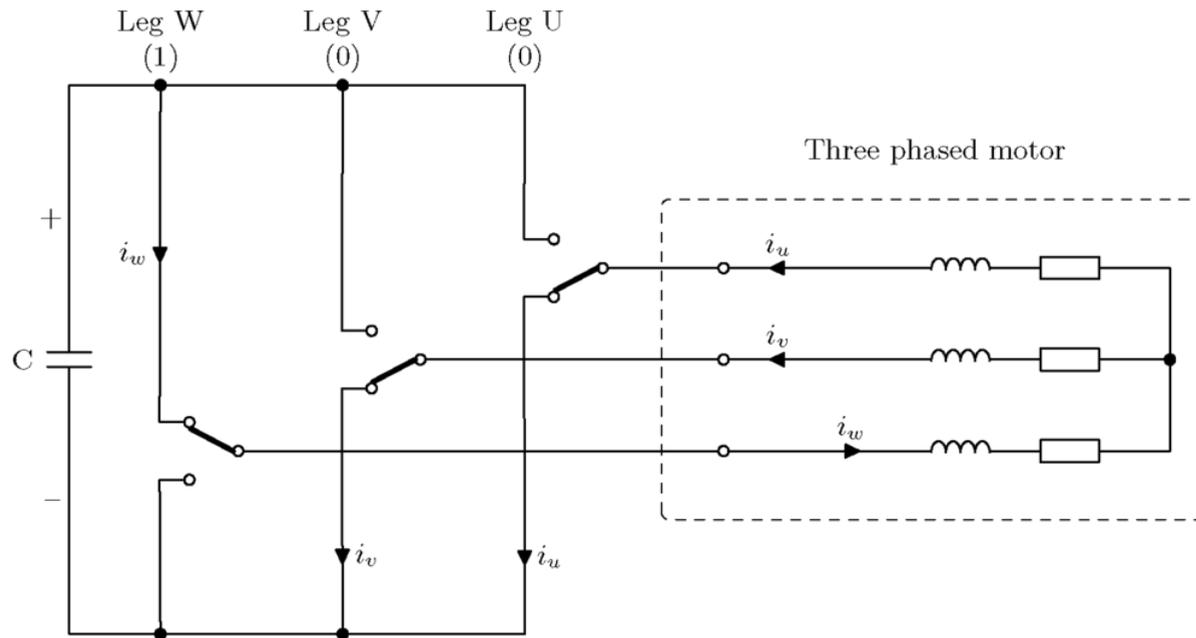
Each leg has two positions: top switch closed (1)

# 3-Phase Two-Level Inverter



Each leg has two positions:

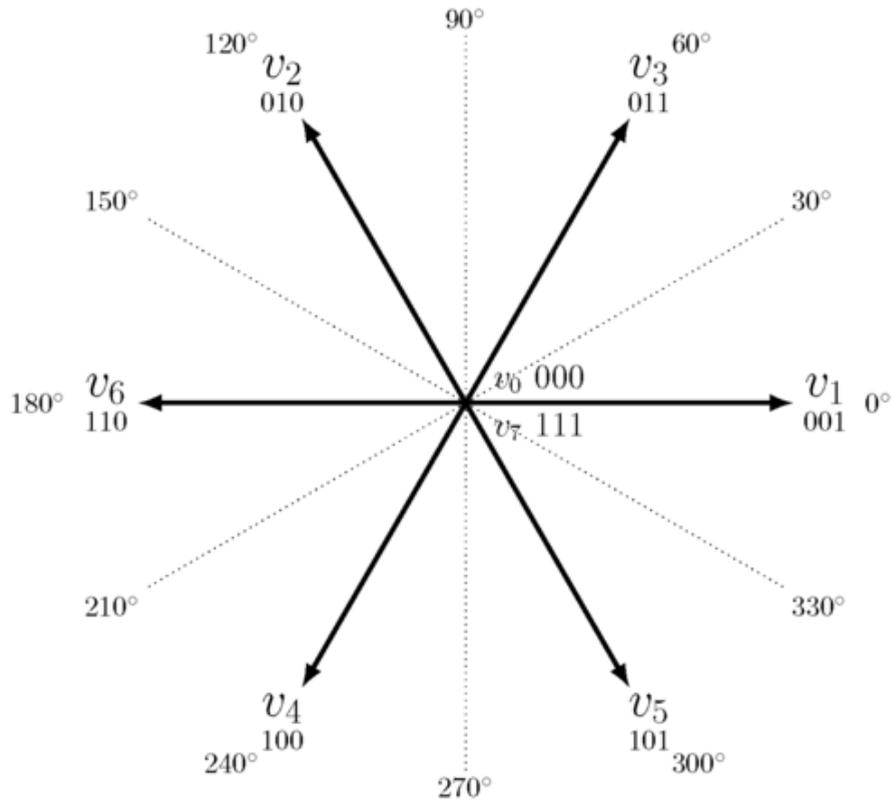
# 3-Phase Two-Level Inverter



Each leg has two positions: bottom switch closed (0)

# Voltage Vectors

# Voltage Vectors



000 -  $v_0$  (zero vector)

001 -  $v_1$  (Phase +U)

010 -  $v_2$  (Phase +V)

011 -  $v_3$  (Phase -W)

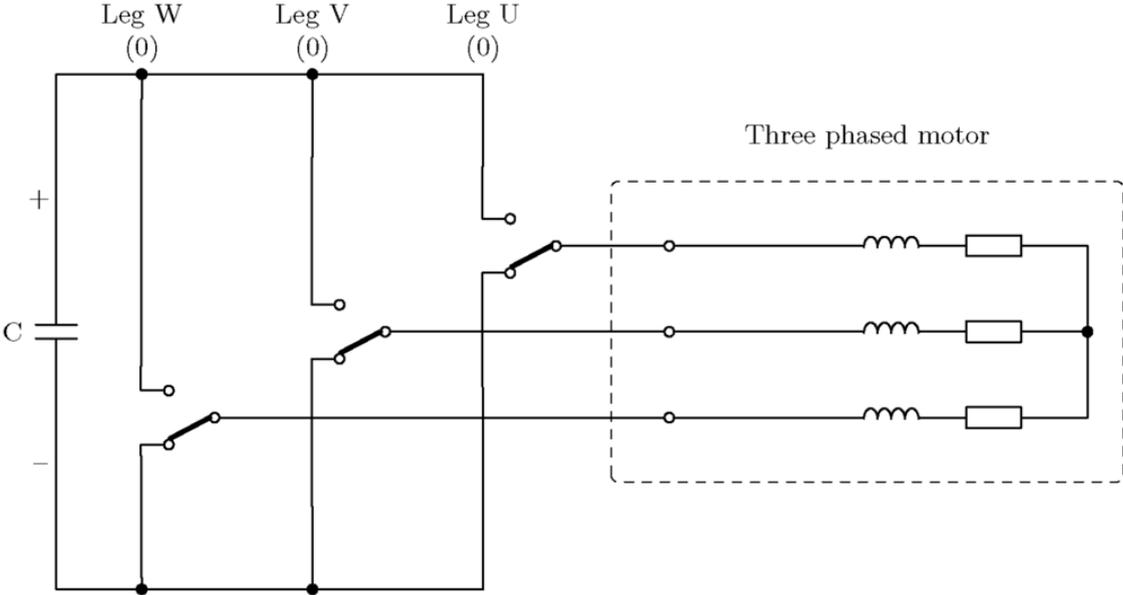
100 -  $v_4$  (Phase +W)

101 -  $v_5$  (Phase -V)

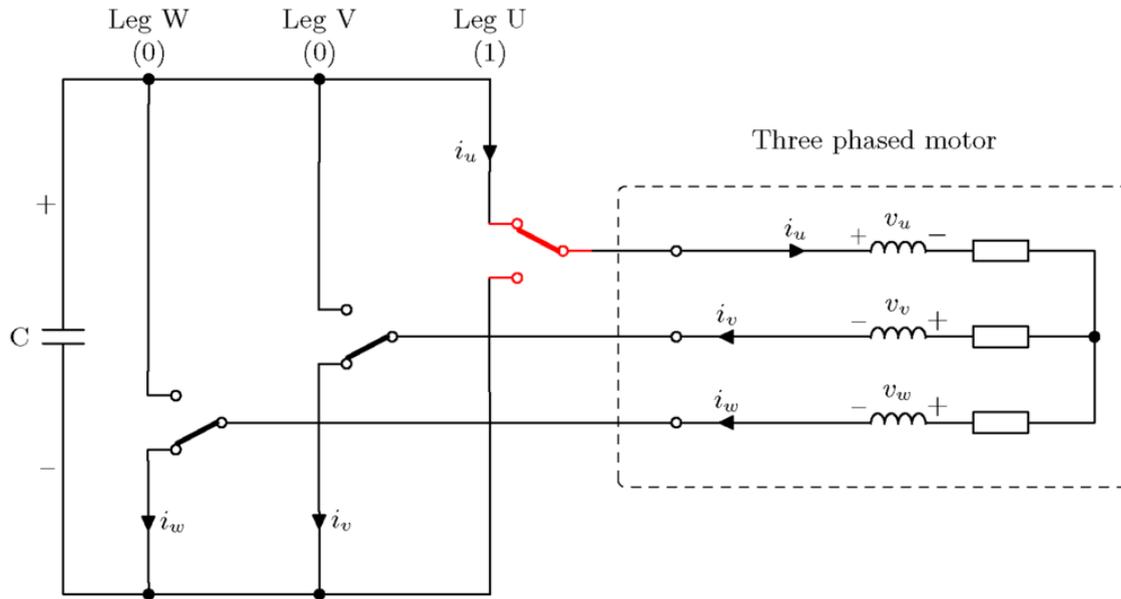
110 -  $v_6$  (Phase -U)

111 -  $v_7$  (zero vector)

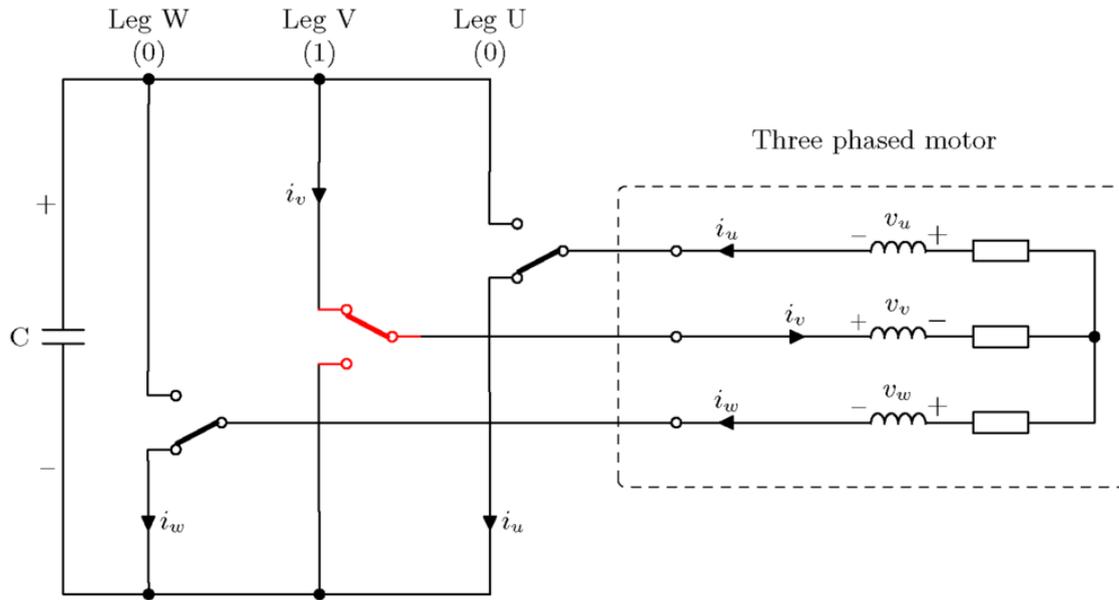
# Voltage Vectors: $V_0$



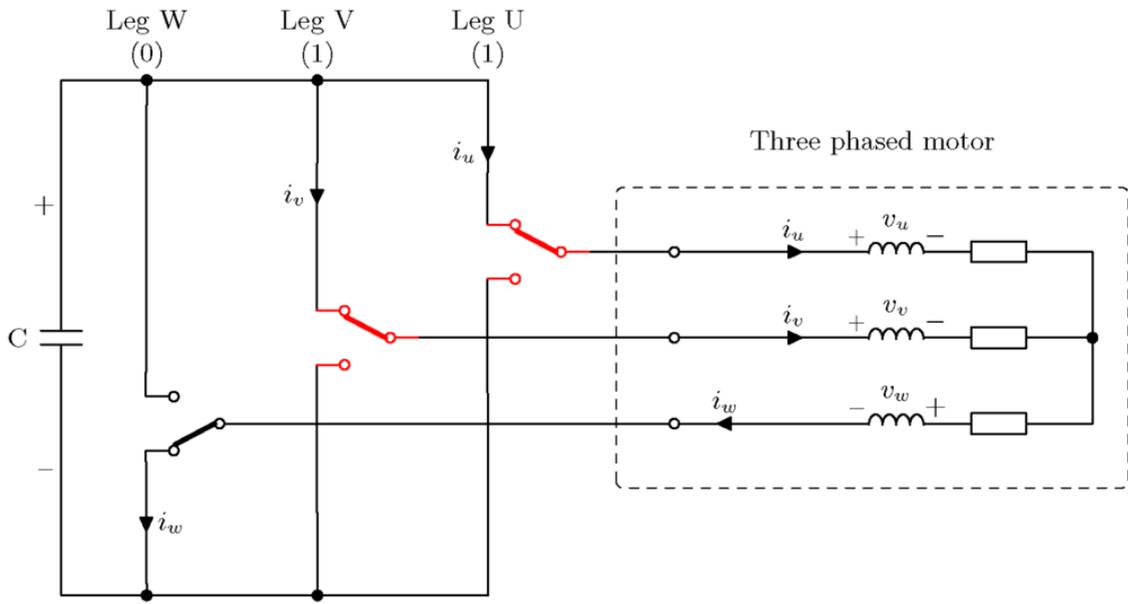
# Voltage Vectors: V1



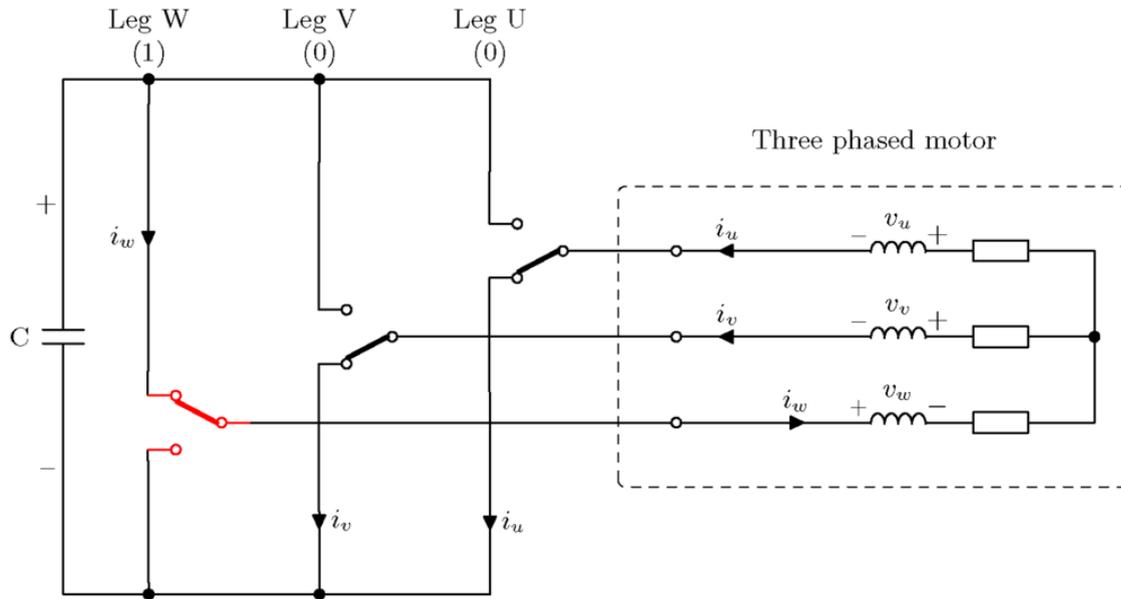
# Voltage Vectors: V2



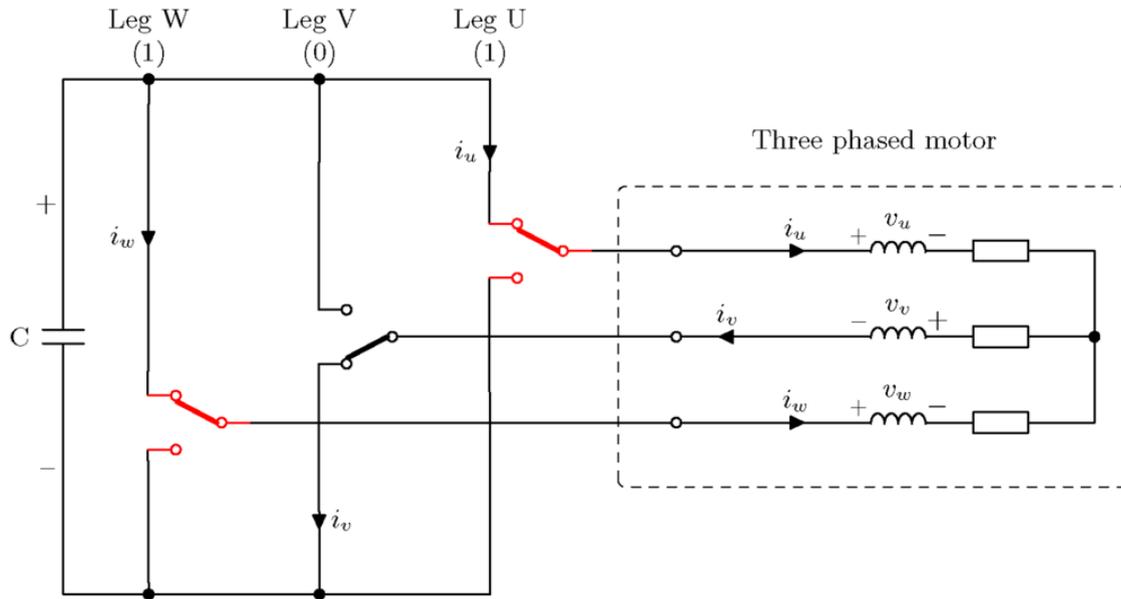
# Voltage Vectors: V3



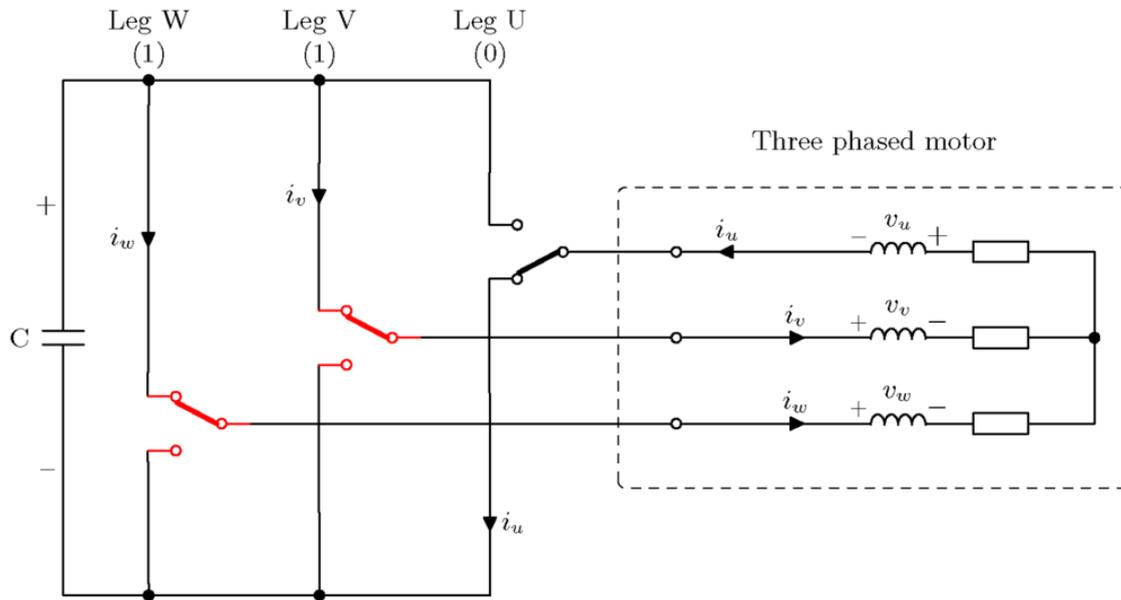
# Voltage Vectors: V4



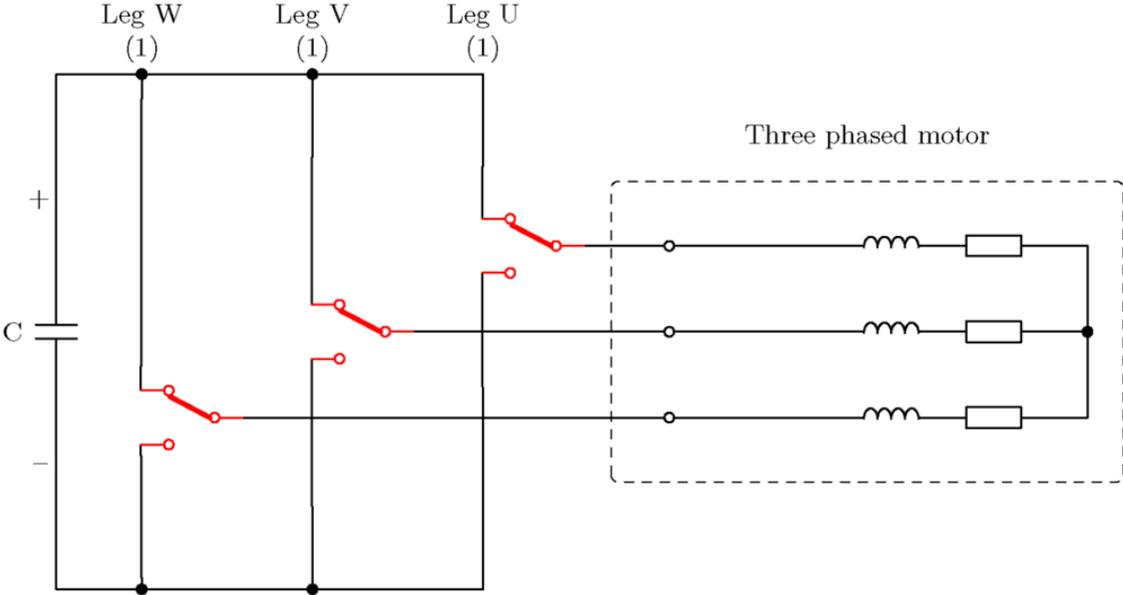
# Voltage Vectors: V5



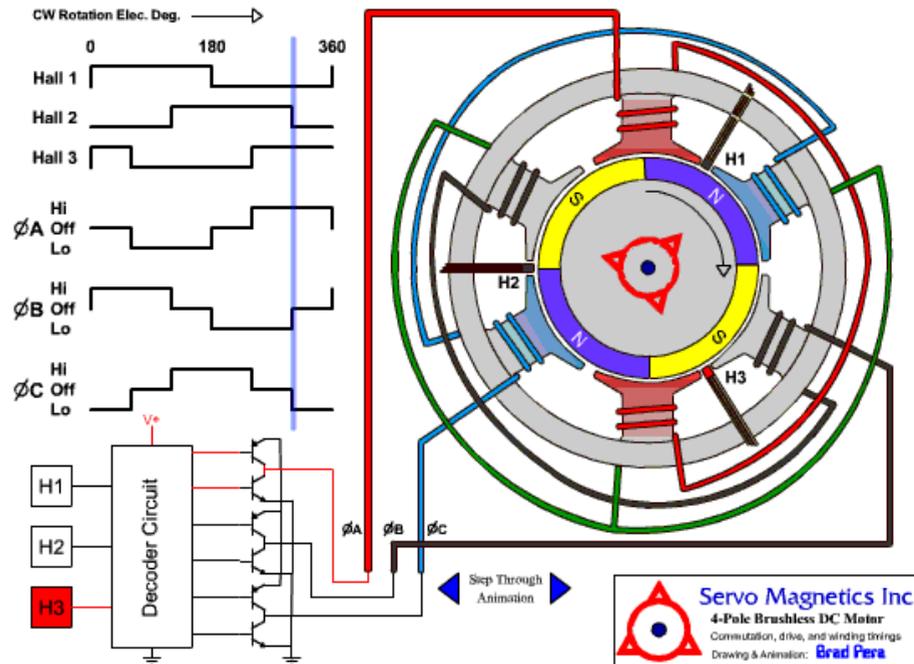
# Voltage Vectors: V6



# Voltage Vectors: V7



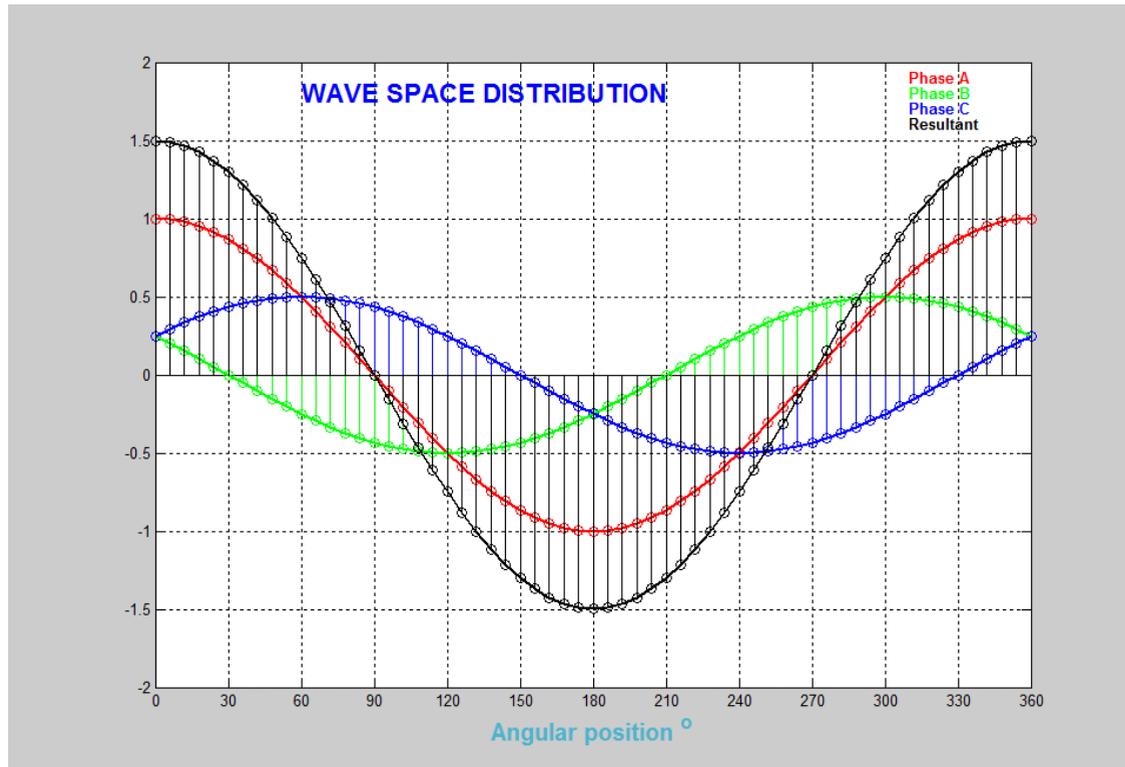
# Square Wave Operation



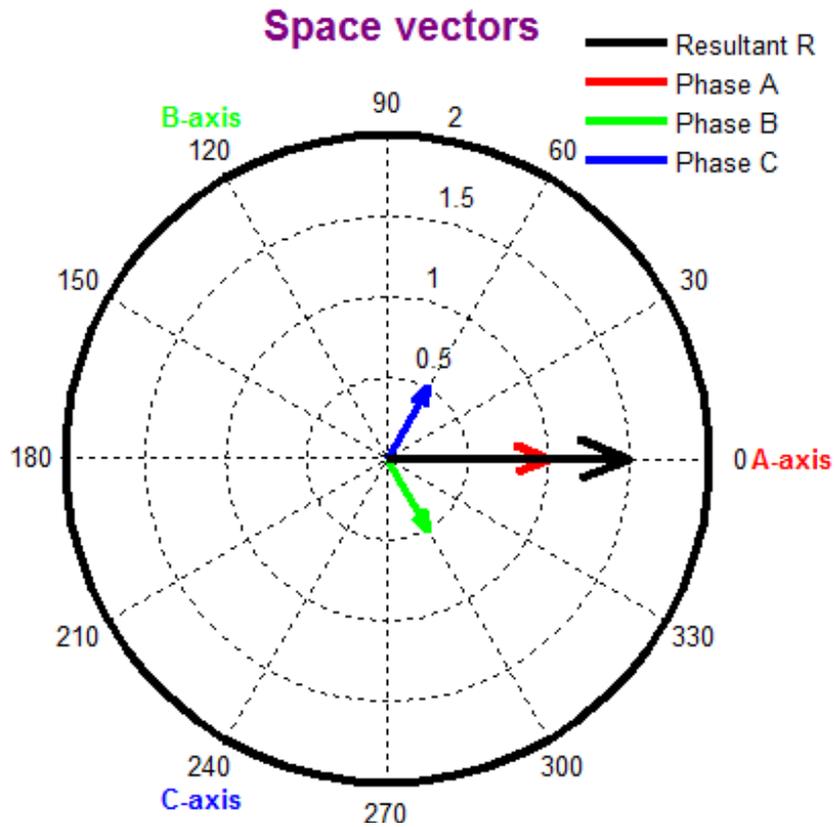
[BLDC Drive with square wave](#)

What about the vectors in between?

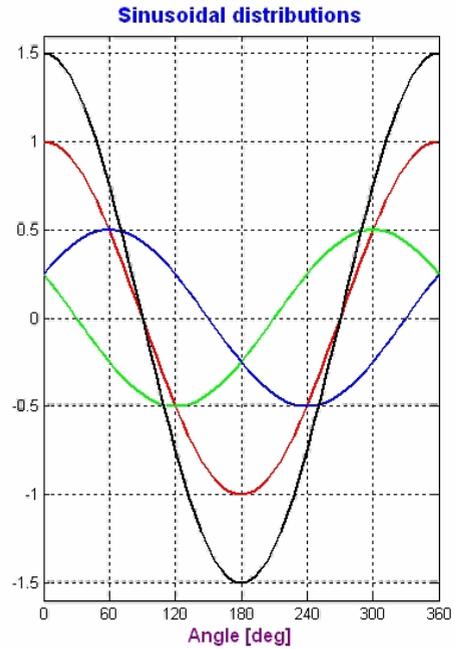
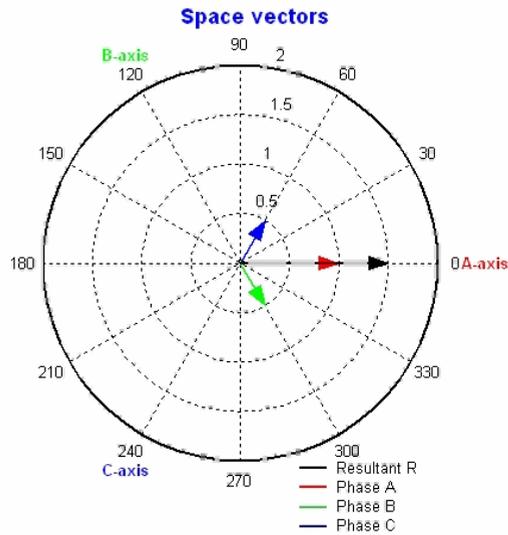
# What about the vectors in between?



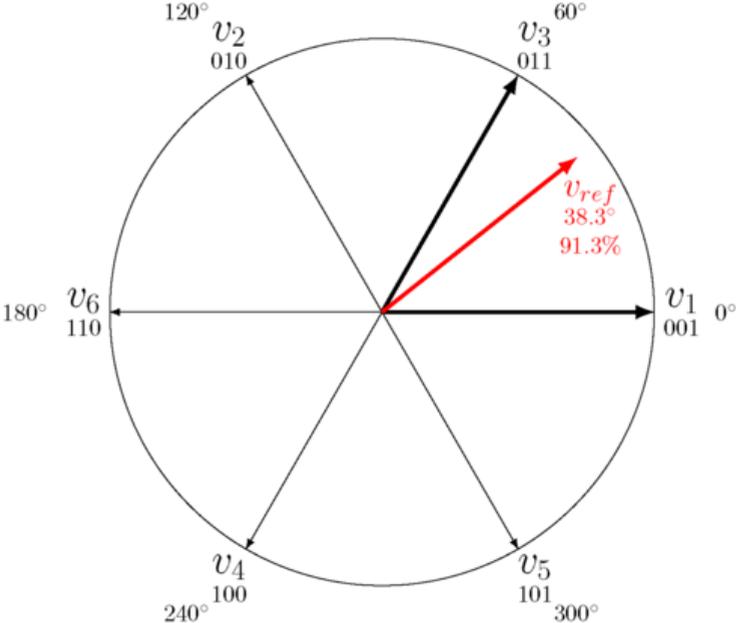
# What about the vectors in between?



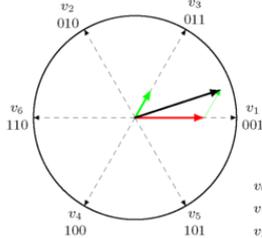
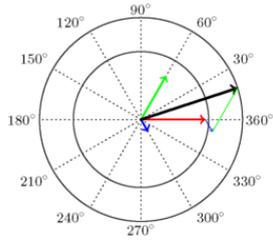
# What about the vectors in between?



# Voltage Synthesizing

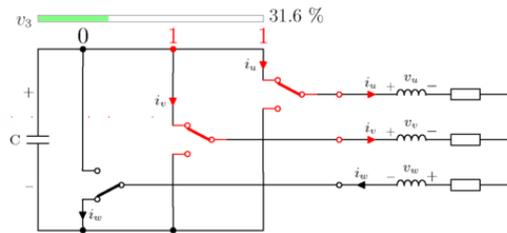
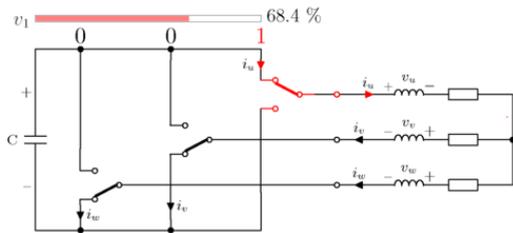
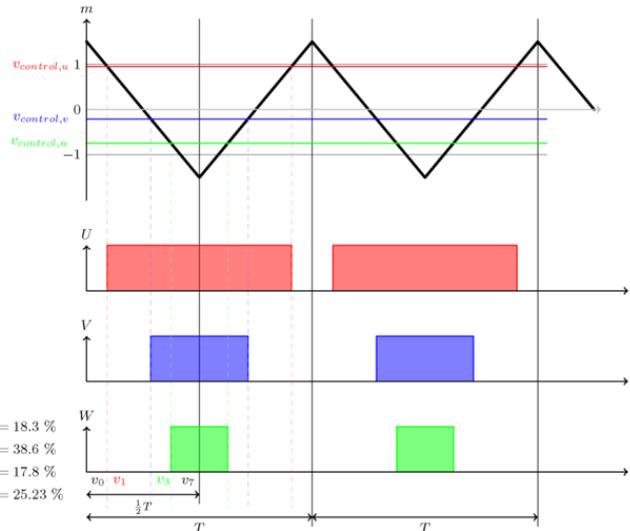


# Voltage Synthesizing

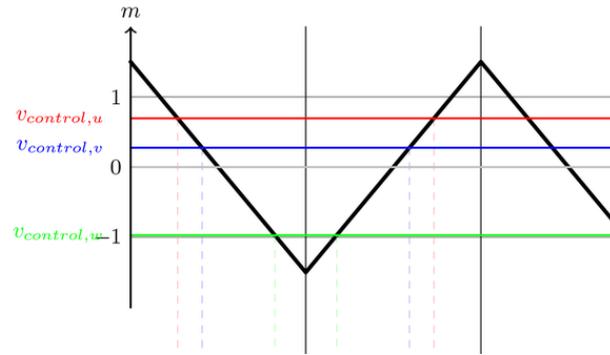
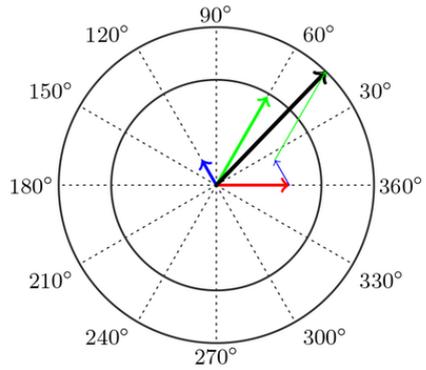


$s = 1$   
 $\phi = 18^\circ$   
 $x = 0.68419$   
 $y = 0.31581$

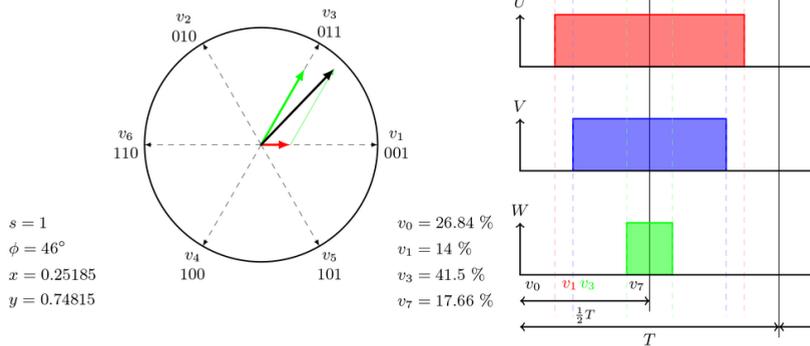
$v_0 = 18.3\%$   
 $v_1 = 38.6\%$   
 $v_3 = 17.8\%$   
 $v_7 = 25.23\%$



# PWM Generation



# PWM Generation



Switching Sequence: 000-001-011-111

# PWM Generation

Switching Sequence:

- Zero Vector (000)

# PWM Generation

Switching Sequence:

- . Zero Vector (000)
- . Basic Vector (i.e. 001)

# PWM Generation

## Switching Sequence:

- . Zero Vector (000)
- . Basic Vector (i.e. 001)
- . Basic Vector (i.e. 011)

# PWM Generation

Switching Sequence:

- . Zero Vector (000)
- . Basic Vector (i.e. 001)
- . Basic Vector (i.e. 011)
- . Zero Vector (i.e. 111)

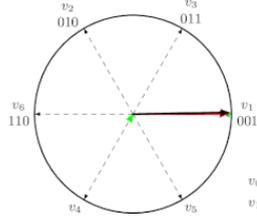
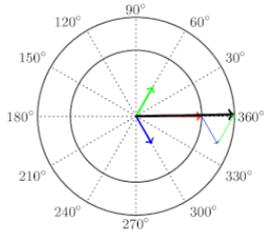
# PWM Generation

## Switching Sequence:

- . Zero Vector (000)
- . Basic Vector (i.e. 001)
- . Basic Vector (i.e. 011)
- . Zero Vector (i.e. 111)

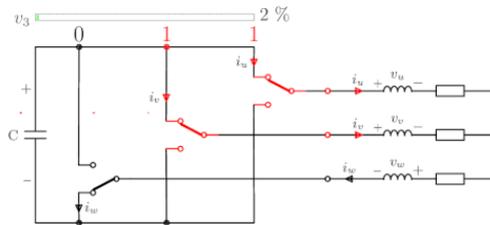
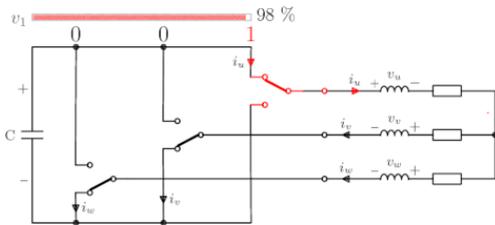
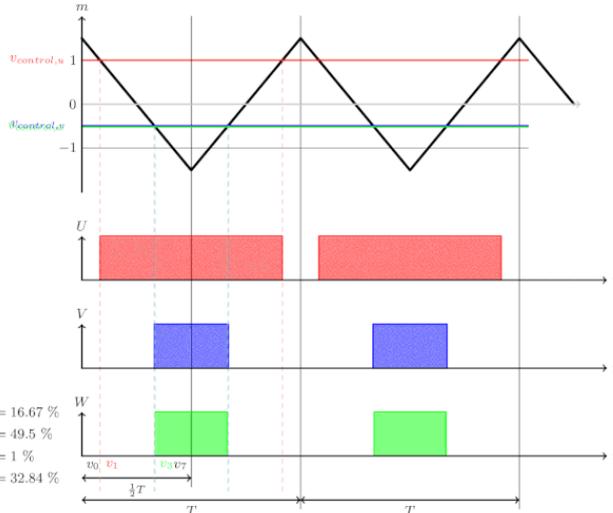
Only one switch position is changed at each step!

# PWM Generation



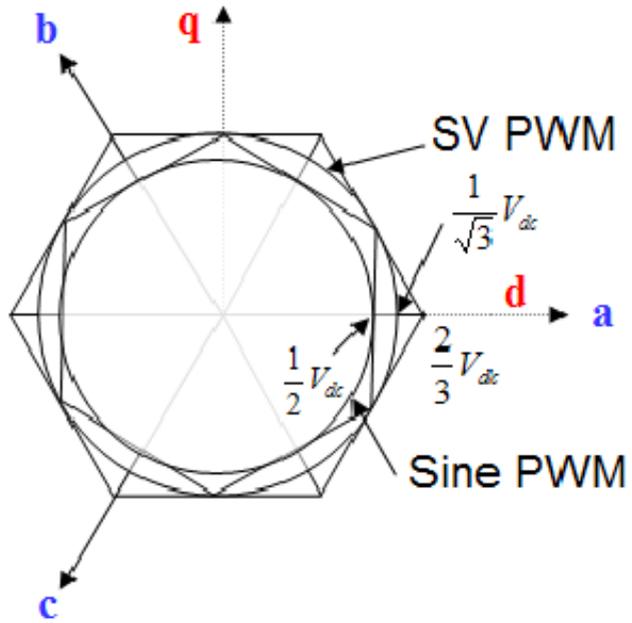
$s = 1$   
 $\phi = 1^\circ$   
 $x = 0.98007$   
 $y = 0.01993$

$v_0 = 16.67\%$   
 $v_1 = 49.5\%$   
 $v_3 = 1\%$   
 $v_7 = 32.84\%$



# SPWM vs SVPWM

# SPWM vs SVPWM



Phase Voltages

# SPWM vs SVPWM

## SPWM vs SVPWM

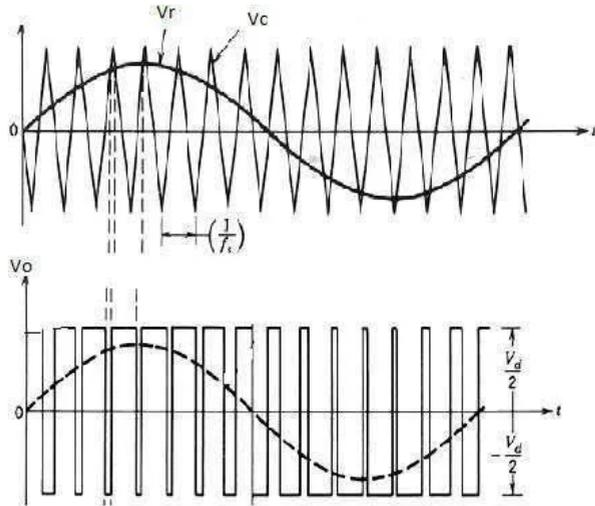
- Space Vector PWM generates less harmonic distortion

## SPWM vs SVPWM

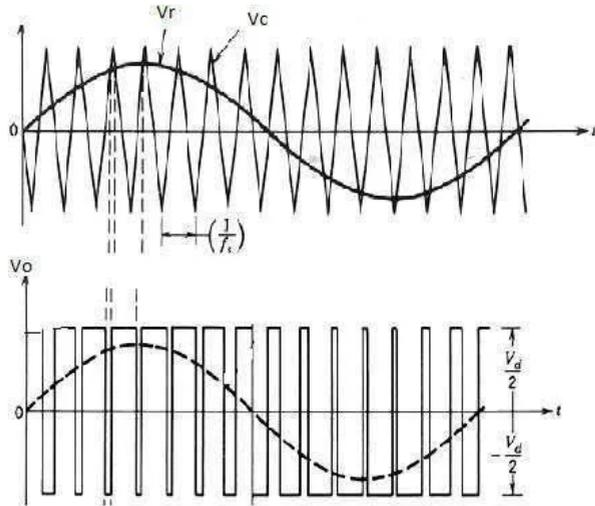
- Space Vector PWM generates less harmonic distortion
- Space Vector PWM utilizes input voltage more  $1/2$  vs  $1/\sqrt{3}$  (15% more)

What is the max. possible phase voltage with SPWM (Sinusoidal PWM)?

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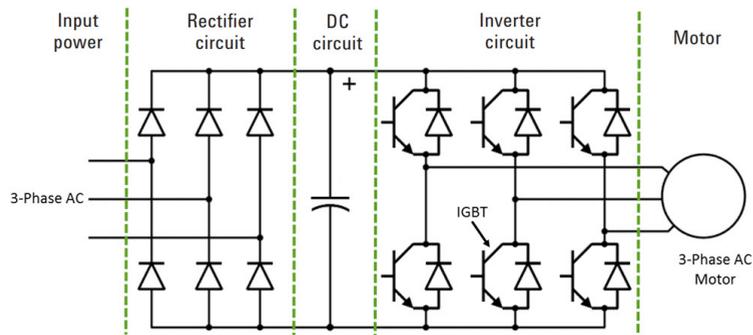


$$\hat{V}_{p-n} = \frac{V_{DC}}{2}$$

What is the max. possible phase voltage with SPWM (Sinusoidal PWM)?

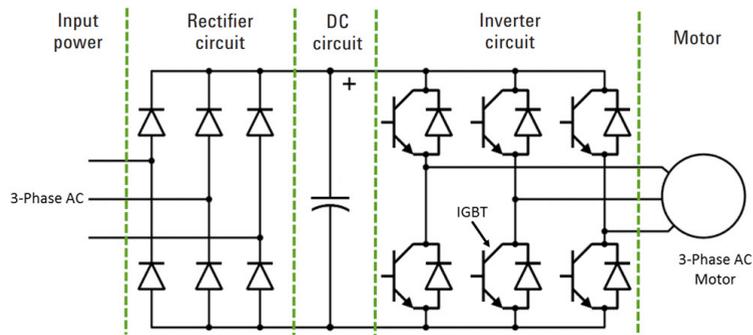
What is the max. possible phase voltage with SPWM (Sinusoidal PWM)?

The inverter is connected to 400 V<sub>l-l</sub> grid with a 3-ph diode rectifier:



What is the max. possible phase voltage with SPWM (Sinusoidal PWM)?

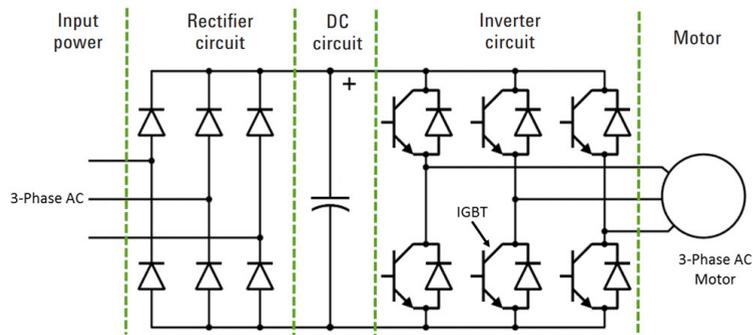
The inverter is connected to 400 V<sub>l-l</sub> grid with a 3-ph diode rectifier:



$$V_{DC} =$$

What is the max. possible phase voltage with SPWM (Sinusoidal PWM)?

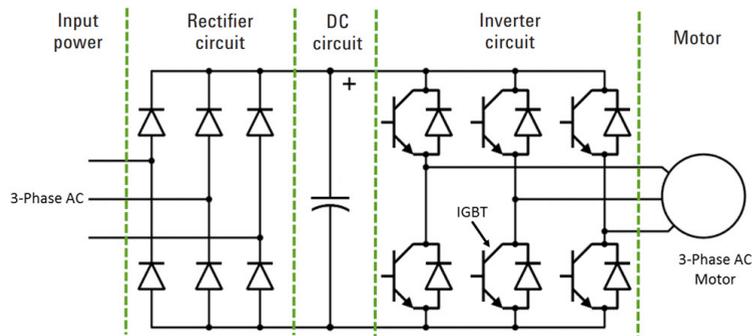
The inverter is connected to 400 V<sub>l-l</sub> grid with a 3-ph diode rectifier:



$$V_{DC} = \frac{3\sqrt{2}}{\pi} V_{l-l}$$

What is the max. possible phase voltage with SPWM (Sinusoidal PWM)?

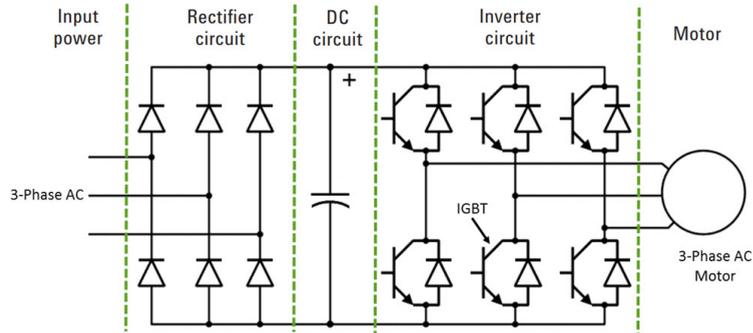
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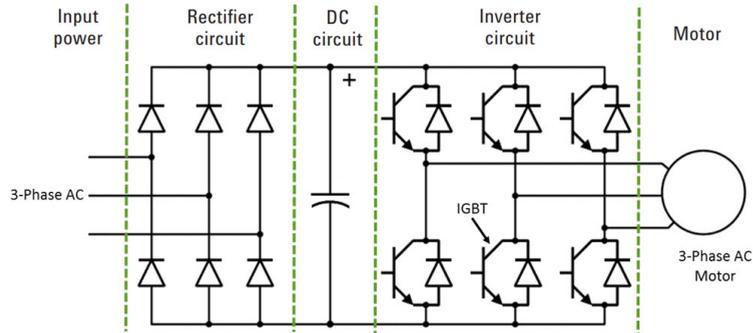
$$V_{DC} = \frac{3\sqrt{2}}{\pi} V_{l-l} = 1.35 V_{l-l} = 540V$$

What is the max. possible phase voltage with SPWM (Sinusoidal PWM)?

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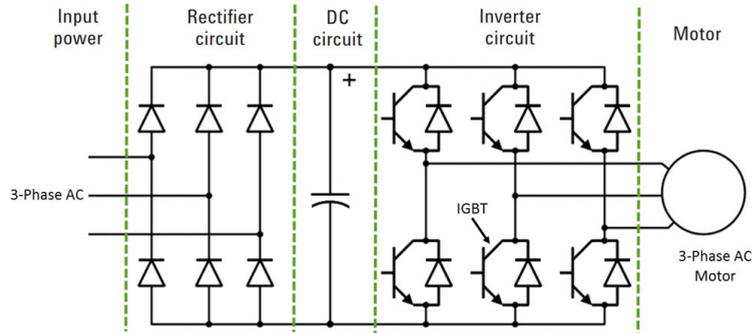


What is the max. possible phase voltage with SPWM (Sinusoidal PWM)?



Maximum motor phase voltage:

What is the max. possible phase voltage with SPWM (Sinusoidal PWM)?



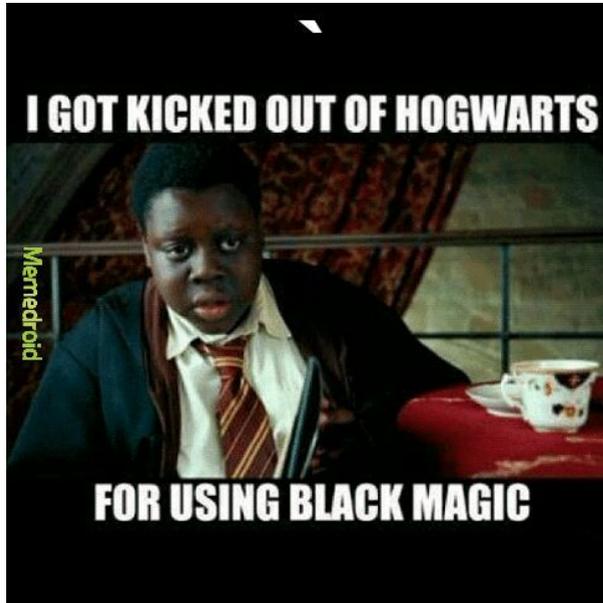
Maximum motor phase voltage:

$$V_{phase-rms} = \frac{V_{DC}}{2\sqrt{2}} = 190V$$

which is quite low for standard motors!

How can you increase the output voltage beyond the DC-link voltage limit?

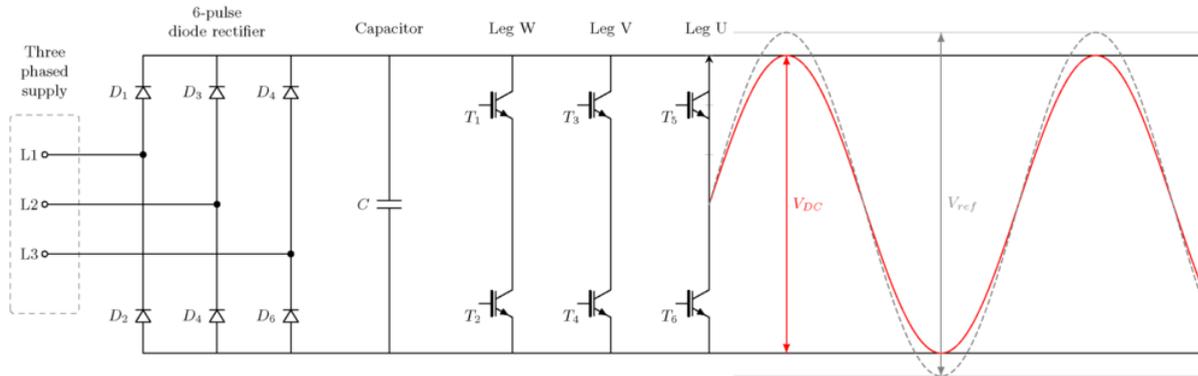
How can you increase the output voltage beyond the DC-link voltage limit?



# Third Harmonic Injection (THIPWM)

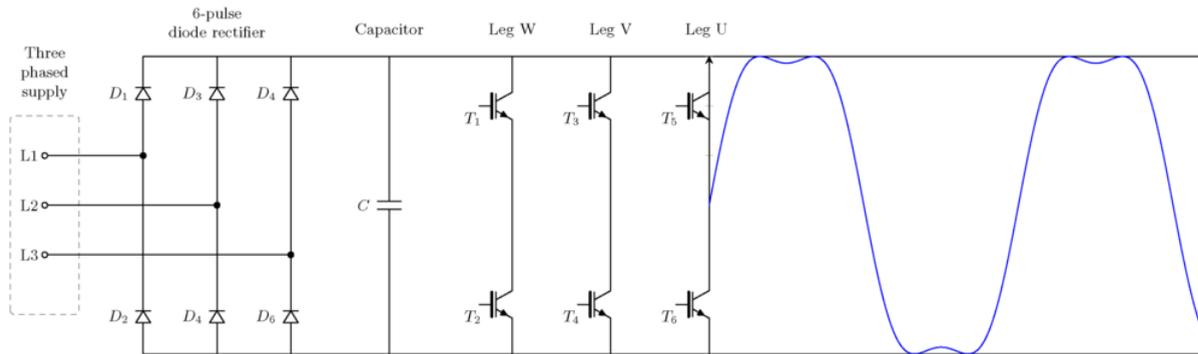
# Third Harmonic Injection (THIPWM)

A sinusoidal reference voltage output:



# Third Harmonic Injection (THIPWM)

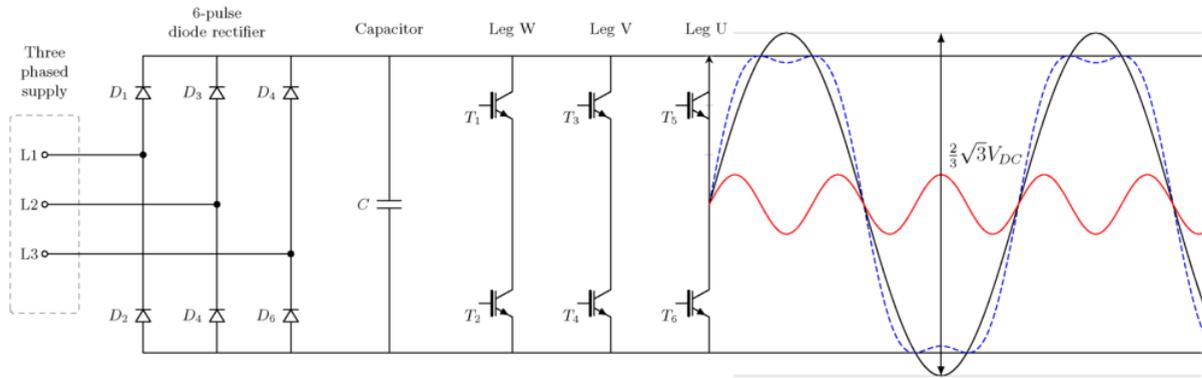
Assume you apply a waveform like that:



which composes of the fundamental and a third-harmonic component

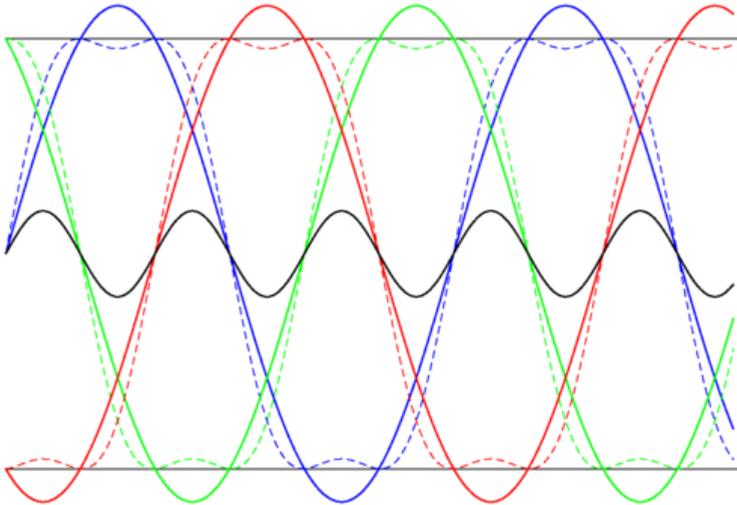
# Third Harmonic Injection (THIPWM)

Such that  $V = \frac{V_{DC}}{2}$  at  $\pi/3$



# Third Harmonic Injection (THIPWM)

What is the phase voltage?



**Third harmonic cancels itself (common-mode voltage), the potential of the neutral voltage is oscillating, but the winding doesn't see this change and observe a pure sinusoidal.**

# Third Harmonic Injection (THIPWM)

What is the phase voltage?

$$\text{THIPWM: } V_{\text{phase-rms}} = \frac{V_{DC}}{\sqrt{6}} = 220V$$

# Third Harmonic Injection (THIPWM)

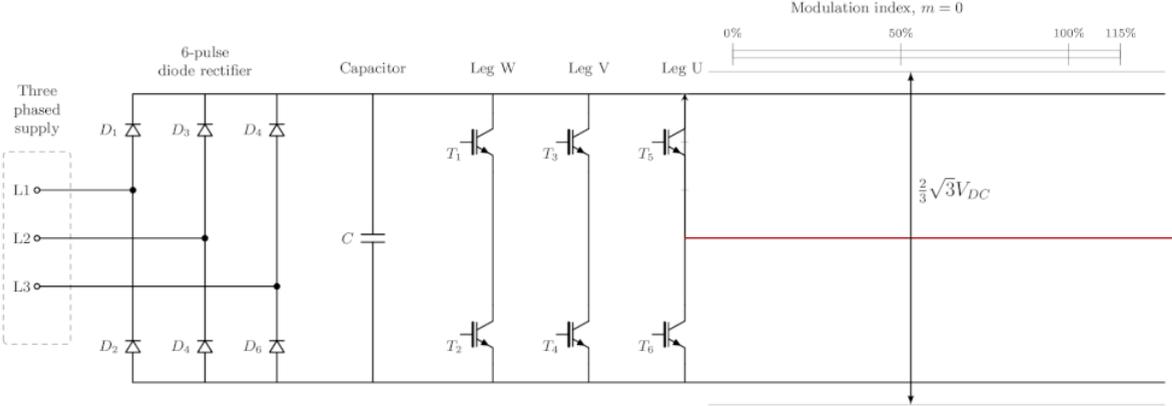
What is the phase voltage?

$$\text{THIPWM: } V_{\text{phase-rms}} = \frac{V_{DC}}{\sqrt{6}} = 220V$$

%15 higher than SPWM

$$(V_{\text{phase-rms}} = \frac{V_{DC}}{2\sqrt{2}} = 190V)$$

# Third Harmonic Injection (THIPWM)



How about SVPWM?

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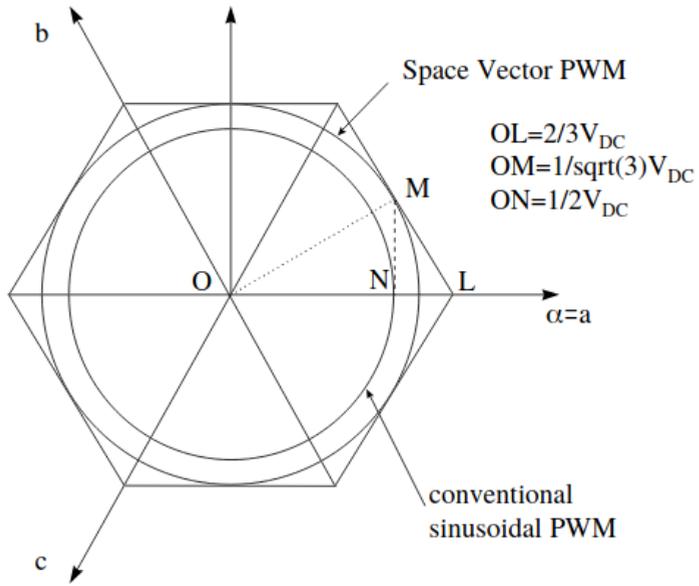
What if two adjacent vectors are applied for %50, %50?

$$= \frac{2}{3} V_{DC} \frac{\sqrt{3}}{2} = \frac{1}{\sqrt{3}} V_{DC}$$

$$\text{Same with THIPWM: } V_{ph,rms} = \frac{1}{\sqrt{6}} V_{DC} = 220V$$

# How about SVPWM?

## Magnitude comparison of SPWM and SVPWM



## Magnitude comparison of SPWM and SVPWM

### Space Vector (SVPWM)

$$\text{Max. } V_{l-l,rms} = \sqrt{3} \frac{\frac{V_{dc}}{\sqrt{3}}}{\sqrt{2}}$$

## Magnitude comparison of SPWM and SVPWM

### Space Vector (SVPWM)

$$\text{Max. } V_{l-l,rms} = \sqrt{3} \frac{\frac{V_{dc}}{\sqrt{3}}}{\sqrt{2}} = \frac{V_{dc}}{\sqrt{2}} = 0.707V_{dc}$$

## Magnitude comparison of SPWM and SVPWM

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### Sinusoidal (SPWM)

## Magnitude comparison of SPWM and SVPWM

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### Sinusoidal (SPWM)

$$\text{Max. } V_{l-l,rms} = \sqrt{3} \frac{\frac{V_{dc}}{2}}{\sqrt{2}}$$

## Magnitude comparison of SPWM and SVPWM

### Space Vector (SVPWM)

$$\text{Max. } V_{l-l,rms} = \sqrt{3} \frac{\frac{V_{dc}}{\sqrt{3}}}{\sqrt{2}} = \frac{V_{dc}}{\sqrt{2}} = 0.707V_{dc}$$

### Sinusoidal (SPWM)

Max.

$$V_{l-l,rms} = \sqrt{3} \frac{\frac{V_{dc}}{2}}{\sqrt{2}} = \frac{\sqrt{3}V_{dc}}{2\sqrt{2}} = 0.612V_{dc}$$

SVPWM is %15 higher than SPWM

You can download this presentation from:  
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