

EE-464 STATIC POWER CONVERSION-II

Resonant Converters

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Advantages of High Switching Frequency?

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Disadvantages of High Switching Frequency?

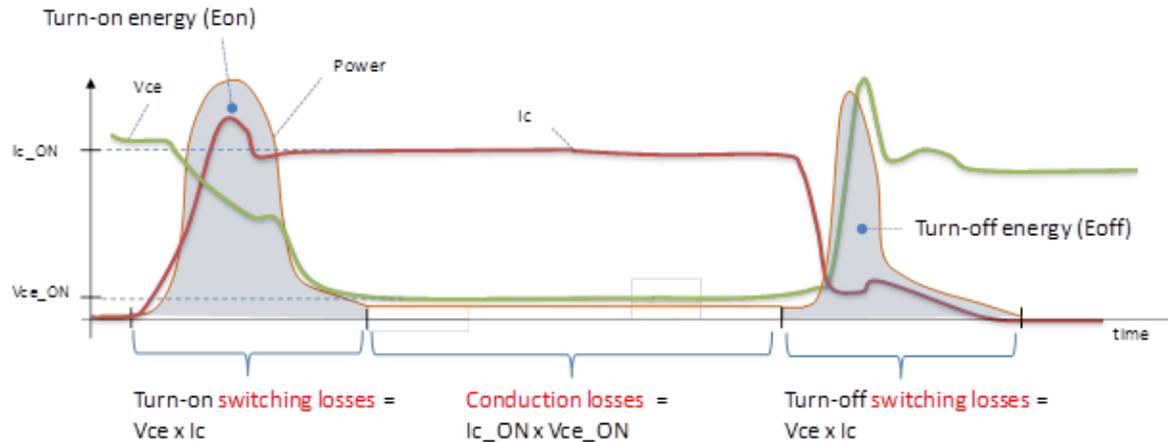
Advantages of High Switching Frequency?

- Reduces filter element sizes
- Reduces transformer size
- Reduced ripple

Disadvantages of High Switching Frequency?

- Increased switching losses

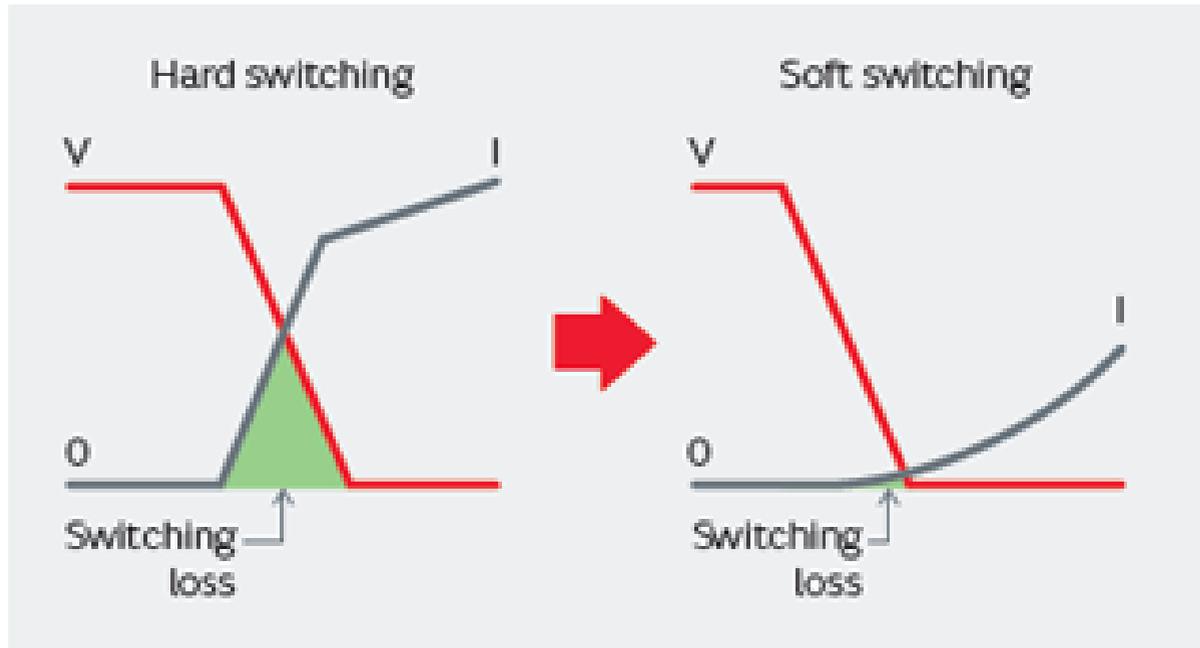
Switching Loss



You have more turn-on, turn-off energy dissipation as the frequency increases

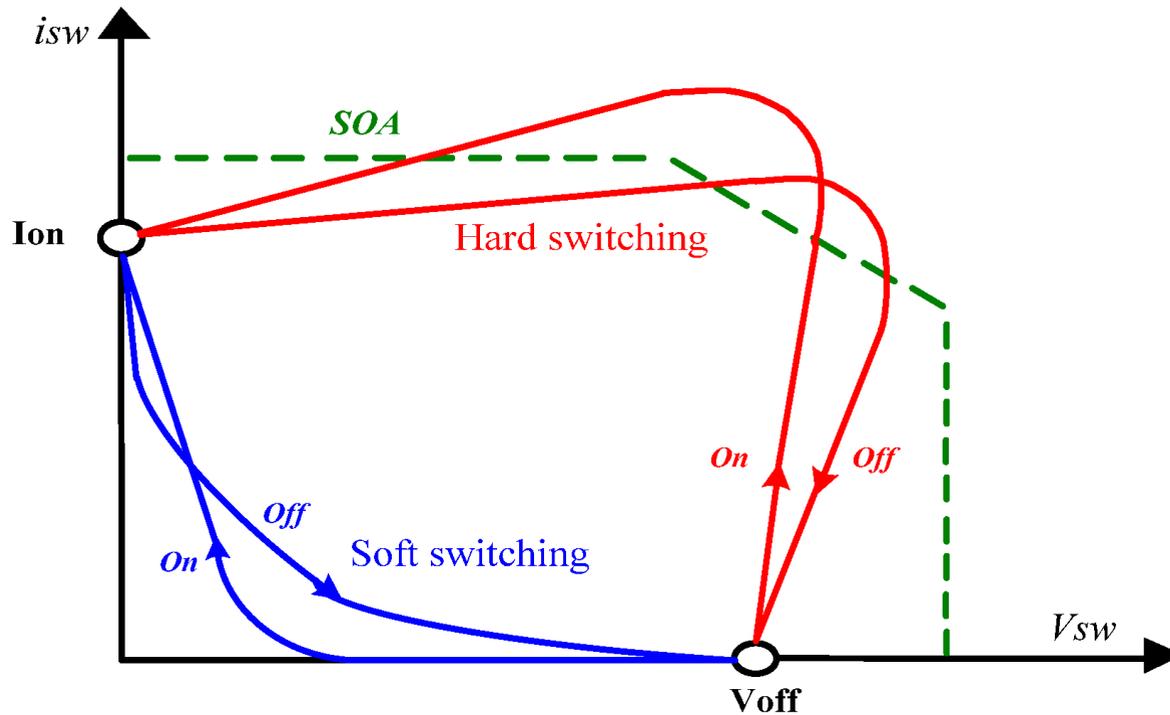
Hard Switching vs. Soft Switching

Hard Switching vs. Soft Switching



Hard Switching vs. Soft Switching

Hard Switching vs. Soft Switching



Resonant Converters

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Two main types of switching:

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Two main types of switching:

- when voltage is zero (ZVS)

Resonant Converters

Two main types of switching:

- when voltage is zero (ZVS)
- when current is zero (ZCS)

Resonant Converters

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There are many resonant converter topologies.

Most common types:

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- Resonant Switch Converters
- Load Resonant Converter

Resonant Converters

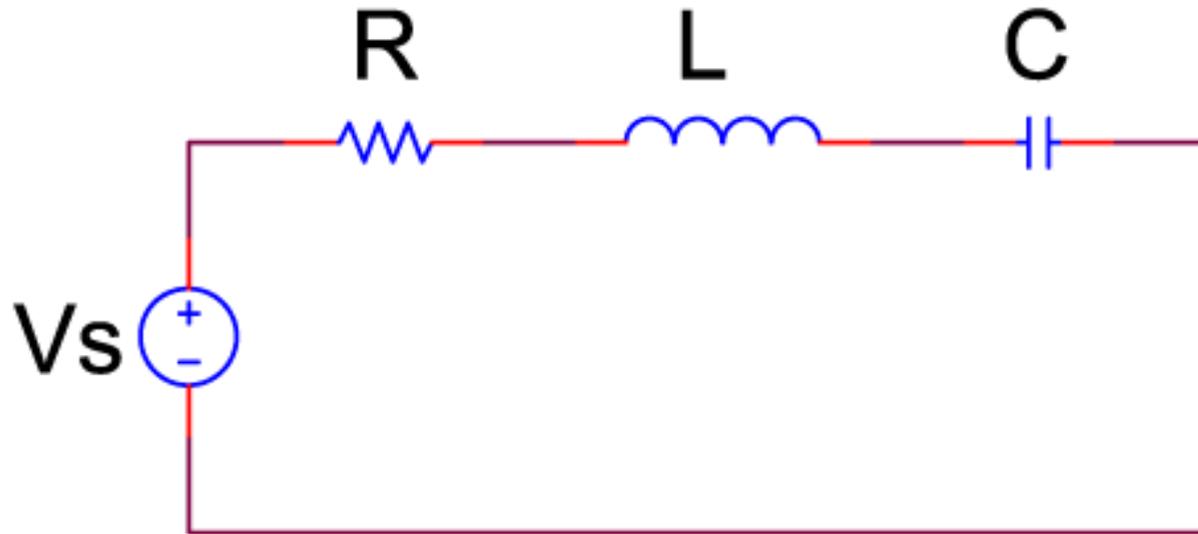
There are many resonant converter topologies.

Most common types:

- Resonant Switch Converters
- Load Resonant Converter
- Resonant DC-link Converter

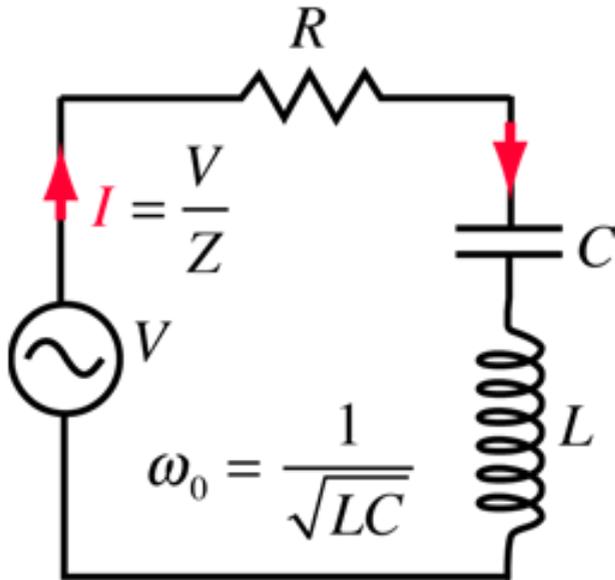
Review: RLC Resonant Circuits

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Review: RLC Resonant Circuits

Minimum impedance
at resonant frequency



Review: RLC Resonant Circuits

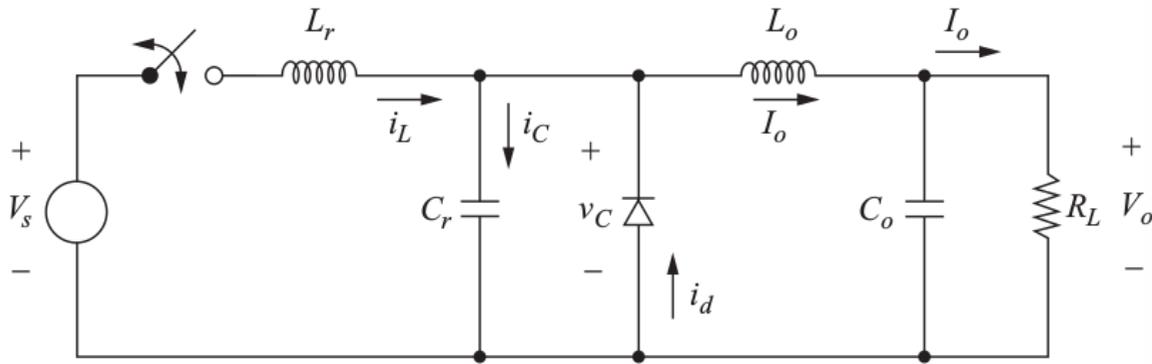
- [Series RLC Circuit Animation](#)
- [Series RLC Circuit Animation](#)
- [Signal Transmission and Reflection](#)

Resonant Switch Converter: Zero Current Switching

W. Hart., Power Electronics, Ch.9

Resonant Switch Converter: Zero Current Switching

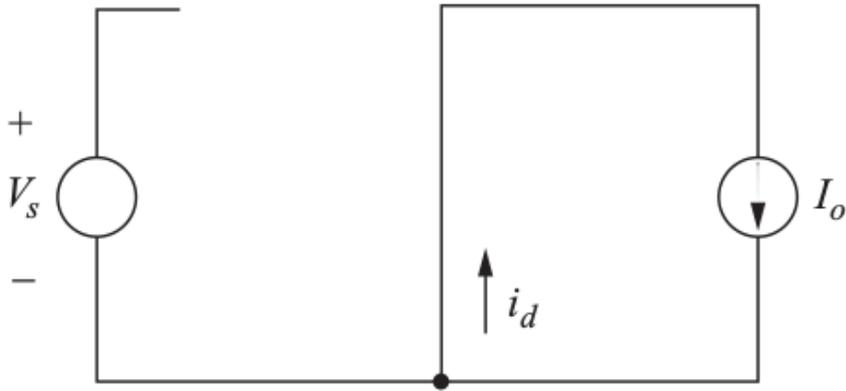
W. Hart., Power Electronics, Ch.9



Assumption: L_o is large enough, I_o is constant

Operating Mode: $t < 0$

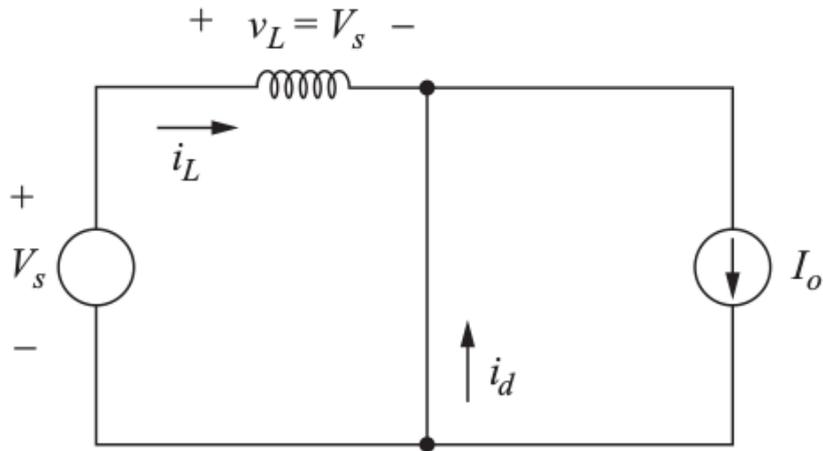
Operating Mode: $t < 0$



Switch open, Diode ON (freewheeling), $v_C = 0$

Operating Mode: $0 < t < t_1$

Operating Mode: $0 < t < t_1$

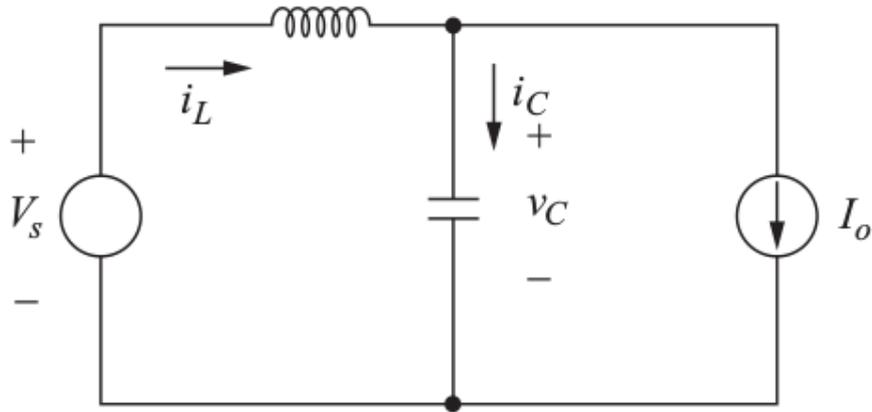


Switch closed, L_r start charging

$i_L < I_o$ so the diode is still ON

Operating Mode: $t_1 < t < t_2$

Operating Mode: $t_1 < t < t_2$

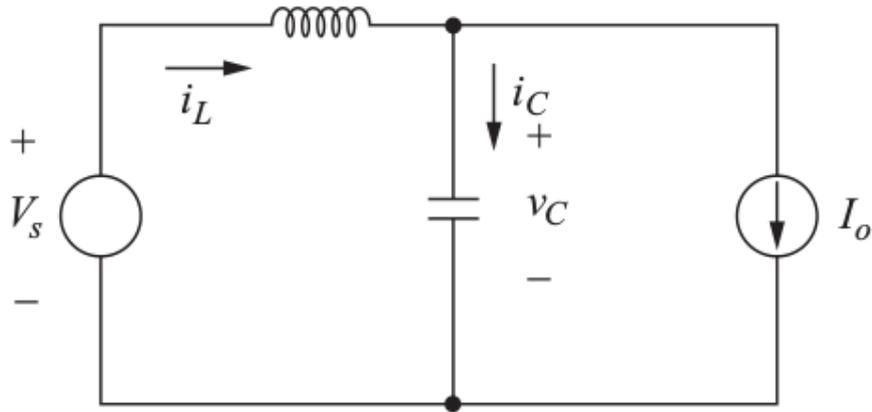


When $i_L = I_o$, the diode turns OFF

Excess inductor current charges the capacitor $v_C > 0$

Operating Mode: $t_1 < t < t_2$

Operating Mode: $t_1 < t < t_2$



If no action is taken, oscillation starts in the LC circuit!

Operating Mode: $t_2 < t < t_3$

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Turn the switch off, when $i_L = 0$

Operating Mode: $t_2 < t < t_3$

Turn the switch off, when $i_L = 0$

=Zero current switching!

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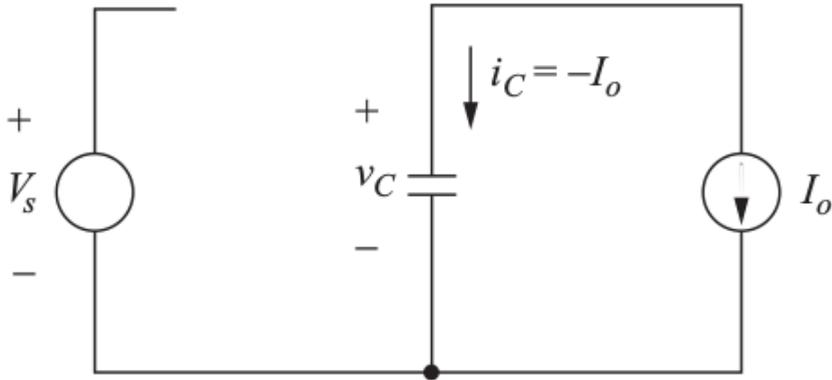
Turn the switch off, when $i_L = 0$

=Zero current switching!

Alternatively a unidirectional switch (SCR) can be used.

Operating Mode: $t_2 < t < t_3$

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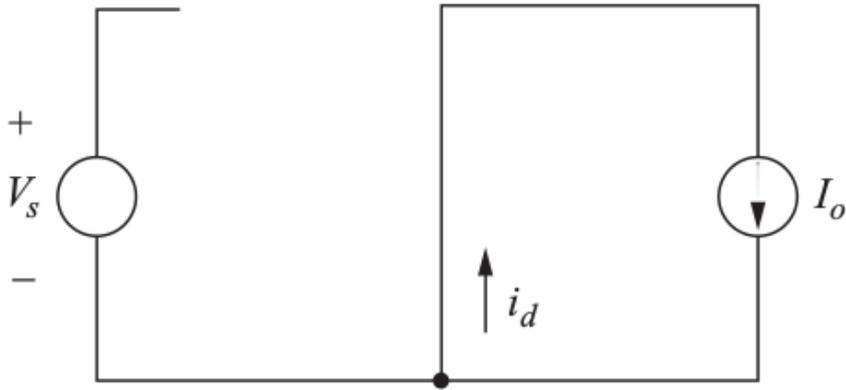


Very small switching loss (due to capacitances in the switch)

Output current is supplied by C (discharges linearly)

Initial Mode: $t_3 < t < T$

Initial Mode: $t_3 < t < T$

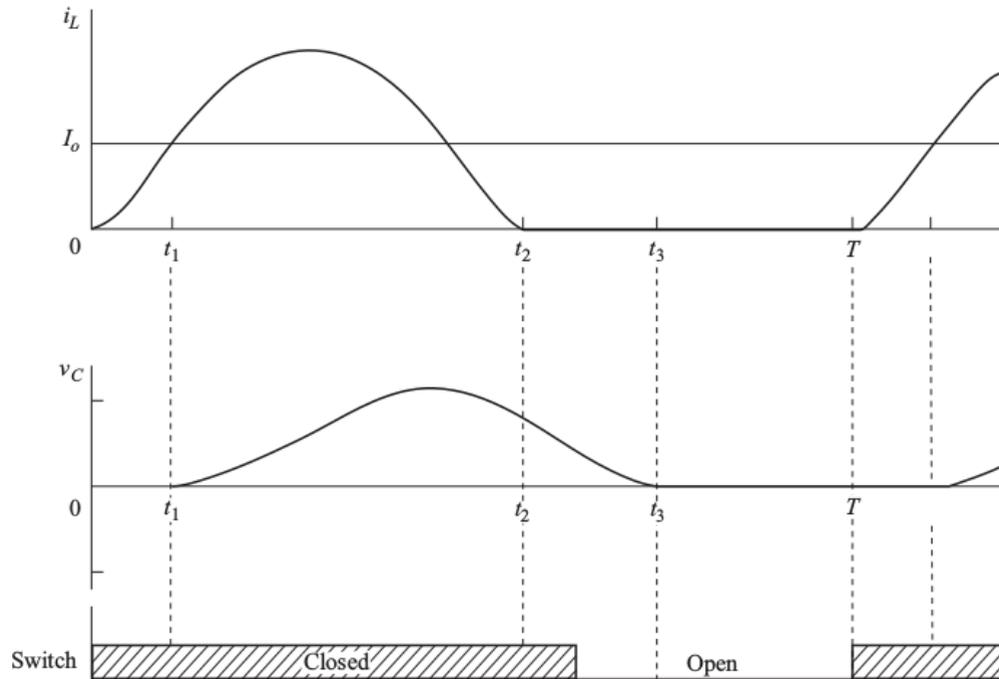


$v_C = 0$, diode starts freewheeling,

Switch ready to turn ON (zero current)

Analysis of the Operating Modes

W. Hart., Power Electronics, Ch.9-2



Operating Mode: $0 < t < t_1$

Inductor L_r sees constant V_s voltage and the current increases linearly

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$$i_L(t) = \frac{V_s}{L_r} t$$

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The moment that the current reaches to I_o is:

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$$i_L(t) = \frac{V_s}{L_r} t$$

The moment that the current reaches to I_o is:

$$t_1 = \frac{I_o L_r}{V_s}$$

Operating Mode: $t_1 < t < t_2$

Diode is off, capacitor voltage starts building up:

Operating Mode: $t_1 < t < t_2$

Diode is off, capacitor voltage starts building up:

$$v_c(t) = V_s - L_r \frac{di_L(t)}{dt}$$

Operating Mode: $t_1 < t < t_2$

Differentiating and solving second order LC circuit (as in Ch9.2)

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Differentiating and solving second order LC circuit (as in Ch9.2)

$$i_L(t) = I_o + \frac{V_s}{Z_o} \sin \omega_0 (t - t_1)$$

$$Z_o = \sqrt{\frac{L_r}{C_r}}$$

$$\omega_0 = \frac{1}{\sqrt{L_r C_r}}$$

Operating Mode: $t_1 < t < t_2$

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$$\omega_0 = \frac{1}{\sqrt{L_r C_r}}$$

$$t_2 - t_1 = \frac{1}{\omega_0} \left[\sin^{-1} \left(\frac{-I_o Z_o}{V_s} \right) \right]$$

Operating Mode: $t_1 < t < t_2$

Capacitor voltage can be expressed as:

$$V_c(t) = V_s [1 - \cos(\omega_0(t - t_1))]$$

which implies capacitor voltage can reach up to $2V_s$ (a disadvantage of resonant converters)

Operating Mode: $t_2 < t < t_3$

As the inductor current reaches to zero at t_2 , the switch can be opened with no current (ZCS)

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Capacitor discharges with constant load current.

$$V_c(t) = \frac{I_0}{C_r} (t_2 - t) + V_c(t_2)$$

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Capacitor discharges with constant load current.

$$V_c(t) = \frac{I_0}{C_r} (t_2 - t) + V_c(t_2)$$

If $V_c=0$ at t_3 :

$$t_3 - t_2 = \frac{C_r v_c(t_2)}{I_0} = \frac{C_r V_s [1 - \cos(\omega_o(t_2 - t_1))]}{I_0}$$

Operating Mode: $t_3 < t < T$

In this interval switch is off (diode freewheeling)

The length of this interval directly controls the output voltage.

The switching frequency should be adjusted so that t_3 is less than period (T).

Derivation of the Output Voltage

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Use energy balance (L-C are lossless)

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$$V_o = V_s f_s \left[\frac{t_1}{2} + (t_2 - t_1) + (t_3 - t_2) \right]$$

Derivation of the Output Voltage

Use energy balance (L-C are lossless)

$$V_o = V_s f_s \left[\frac{t_1}{2} + (t_2 - t_1) + (t_3 - t_2) \right]$$

$V_o < V_s$ operates as a buck converter

Output voltage is controlled by the switching frequency!

Analysis of the Operating Modes

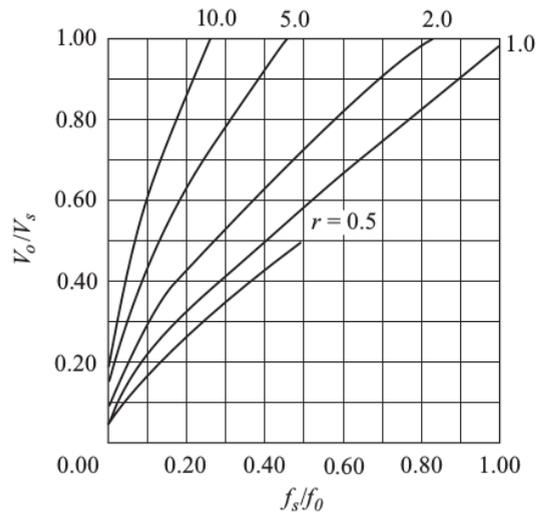
Analysis of the Operating Modes

Time internals are a function of output current

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Time internals are a function of output current

Load changes switching frequency must be changed



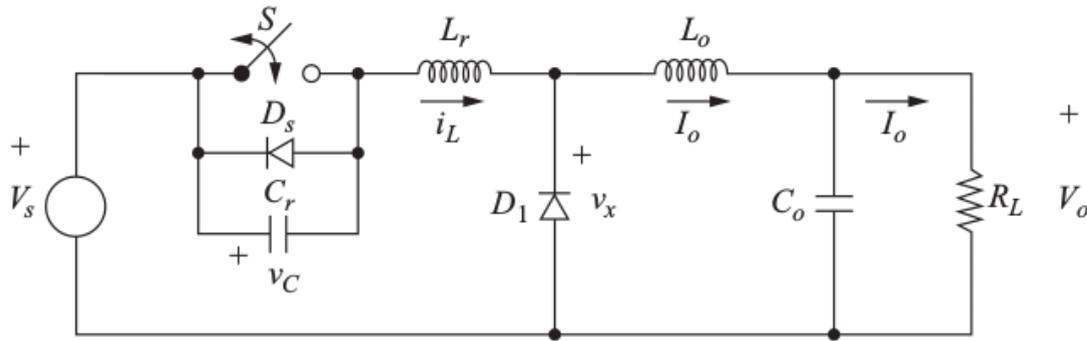
Example (Hart 9-1)

Resonant Switch Converter: Zero Voltage Switching

W. Hart., Power Electronics, Ch.9

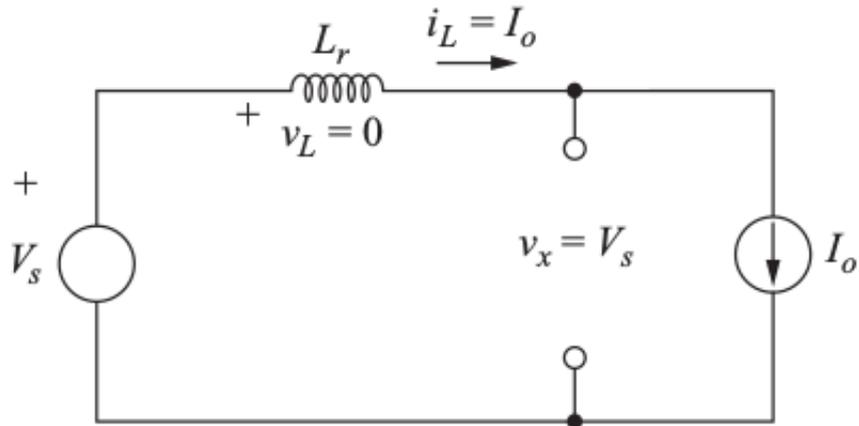
Resonant Switch Converter: Zero Voltage Switching

W. Hart., Power Electronics, Ch.9



Operating Mode: $t < 0$

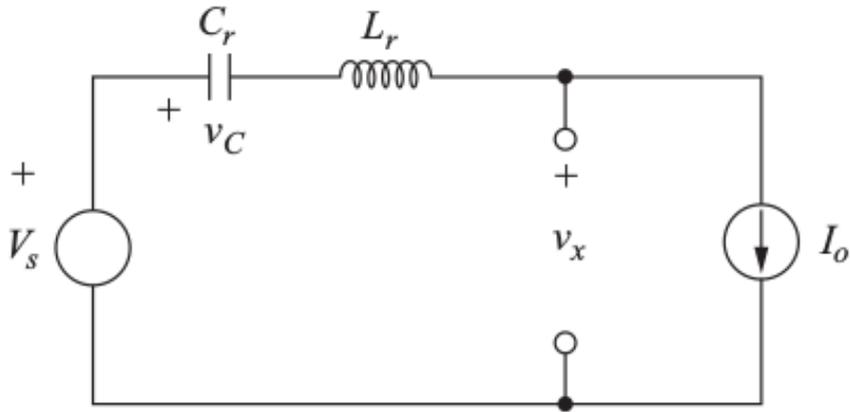
Operating Mode: $t < 0$



D1 off, switch ON, $i_L = I_o$

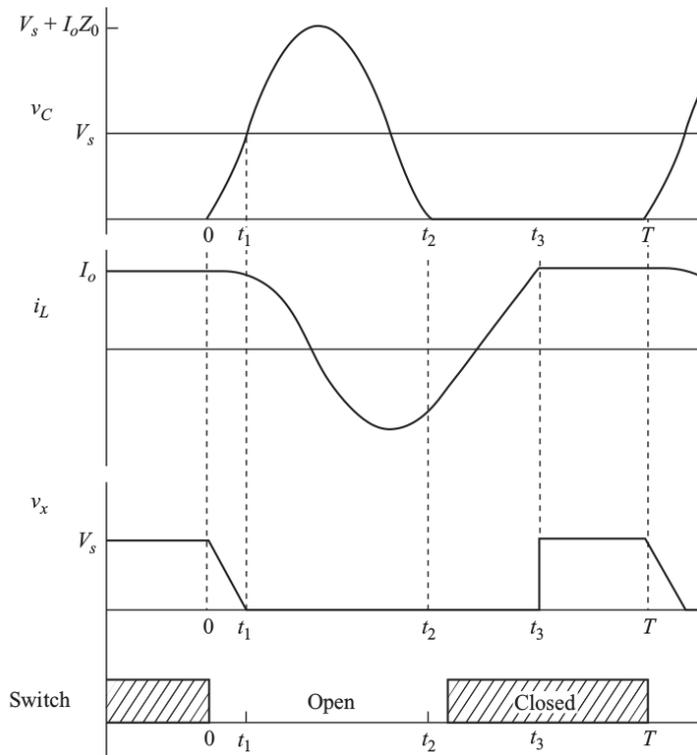
Operating Mode: $0 < t < t_1$

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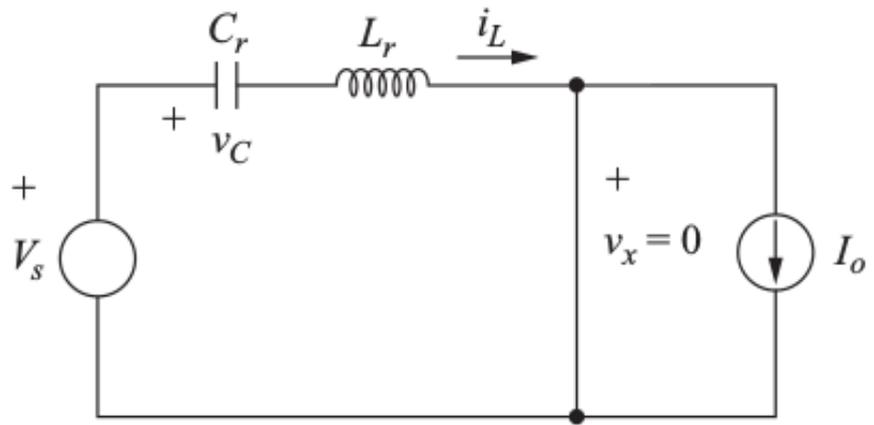
Switch opened, v_C start charging linearly

Resonant Switch Converter: Zero Voltage Switching



Operating Mode: $t_1 < t < t_2$

Operating Mode: $t_1 < t < t_2$

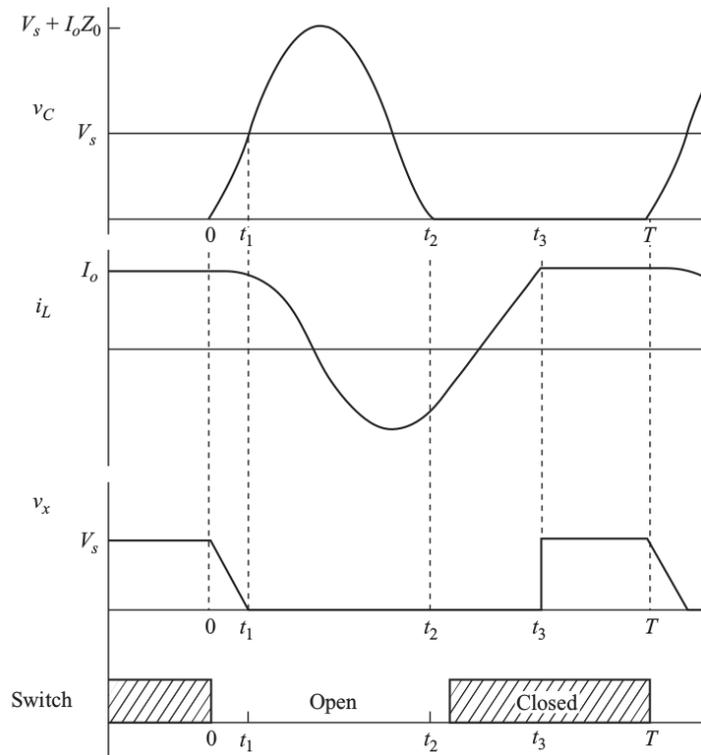


When $v_C = V_s$, the diode (D1) is forward biased

LC resonant circuit start oscillating,

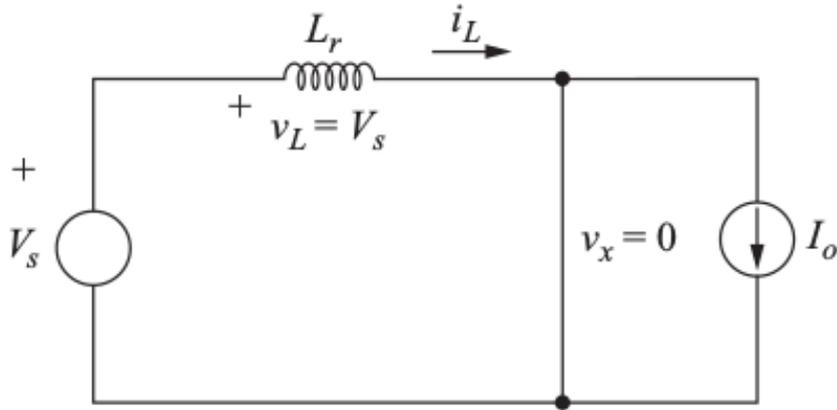
When $v_C = 0$, the diode (Ds) turns on to carry i_L . (which is negative)

Resonant Switch Converter: Zero Voltage Switching



Operating Mode: $t_2 < t < t_3$

Operating Mode: $t_2 < t < t_3$



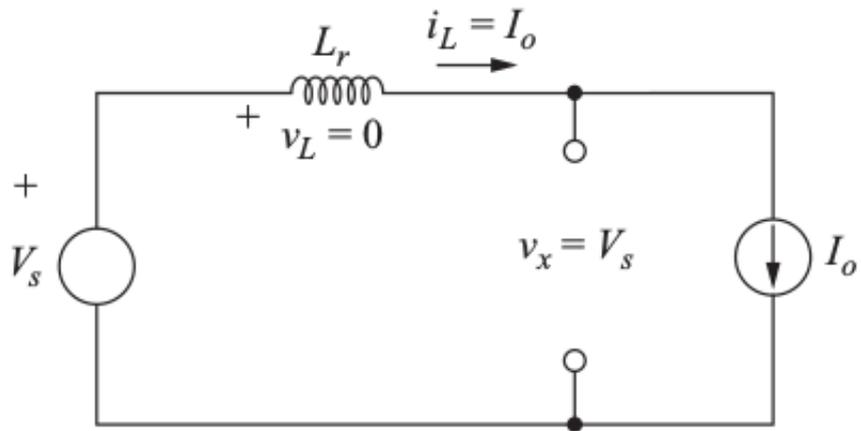
Ds is ON, $V_L = V_s$, inductor current increases linearly

Switch should be closed just after Ds turns on (zero voltage switching)

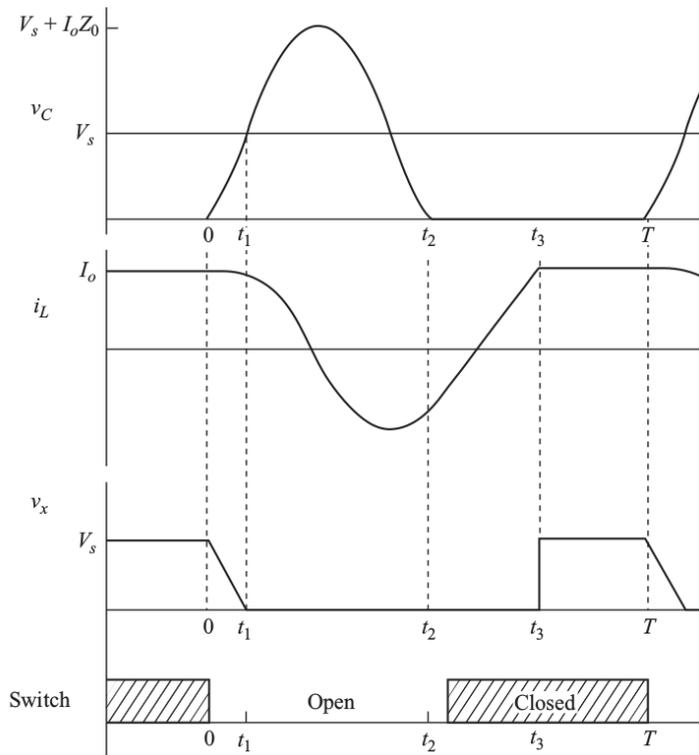
When $i_L = I_o$, D1 is off and back to the initial position

Initial Mode: $t_3 < t < T$

Initial Mode: $t_3 < t < T$



Resonant Switch Converter: Zero Voltage Switching



Resonant Switch Converter: Zero Voltage Switching

Output voltage=?

Resonant Switch Converter: Zero Voltage Switching

Output voltage = Average of $v_x(t)$

Resonant Switch Converter: Zero Voltage Switching

Output voltage = Average of $v_x(t)$

$$v_x(t) = V_s(1 - t/t_1) \quad \text{for } 0 < t < t_1$$

Resonant Switch Converter: Zero Voltage Switching

Output voltage = Average of $v_x(t)$

$$v_x(t) = V_s(1 - t/t_1) \quad \text{for } 0 < t < t_1$$

$$v_x(t) = 0 \quad \text{for } t_1 < t < t_3$$

Resonant Switch Converter: Zero Voltage Switching

Output voltage = Average of $v_x(t)$

$$v_x(t) = V_s(1 - t/t_1) \quad \text{for } 0 < t < t_1$$

$$v_x(t) = 0 \quad \text{for } t_1 < t < t_3$$

$$v_x(t) = V_s \quad \text{for } t_3 < t < T$$

Resonant Switch Converter: Zero Voltage Switching

Output voltage = Average of $v_x(t)$

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Calculate the average voltage

Resonant Switch Converter: Zero Voltage Switching

Output voltage

Resonant Switch Converter: Zero Voltage Switching

Output voltage

$$V_o = \frac{V_s}{T} \left[\frac{t_1}{2} + (T - t_3) \right]$$

Resonant Switch Converter: Zero Voltage Switching

Output voltage

$$V_o = \frac{V_s}{T} \left[\frac{t_1}{2} + (T - t_3) \right]$$

or

$$V_o = V_s \left[1 - f_s \left(t_3 - \frac{t_1}{2} \right) \right]$$

Resonant Switch Converter: Zero Voltage Switching

Output voltage

$$V_o = \frac{V_s}{T} \left[\frac{t_1}{2} + (T - t_3) \right]$$

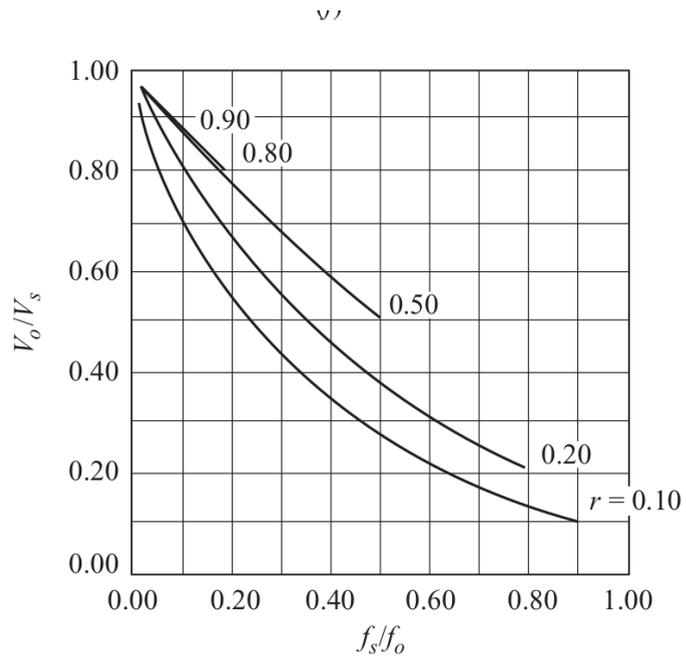
or

$$V_o = V_s \left[1 - f_s \left(t_3 - \frac{t_1}{2} \right) \right]$$

Output voltage is controlled by varying f_s

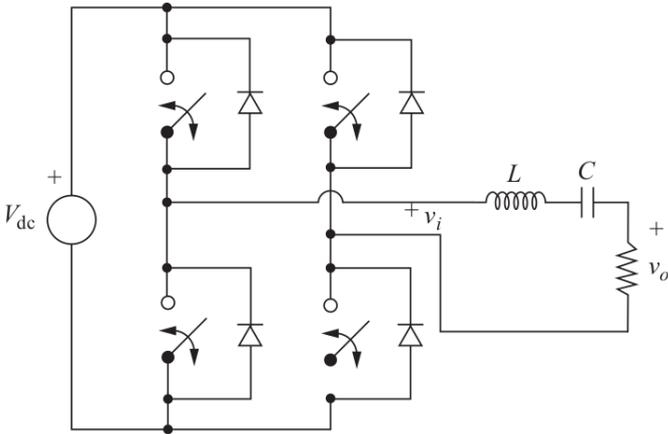
$V_o < V_s$, buck converter

Resonant Switch Converter: Zero Voltage Switching

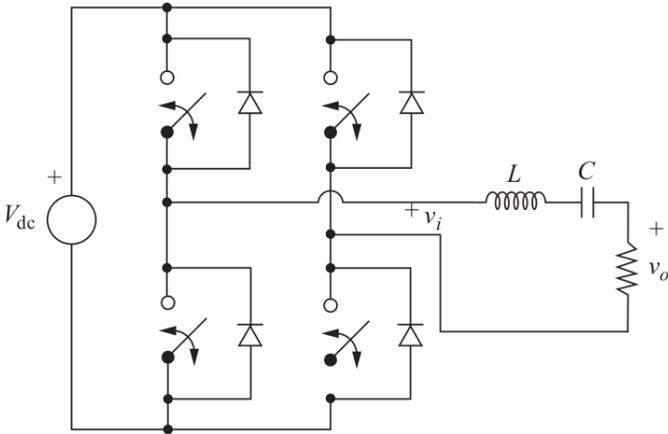


Output voltage is controlled by varying f_s

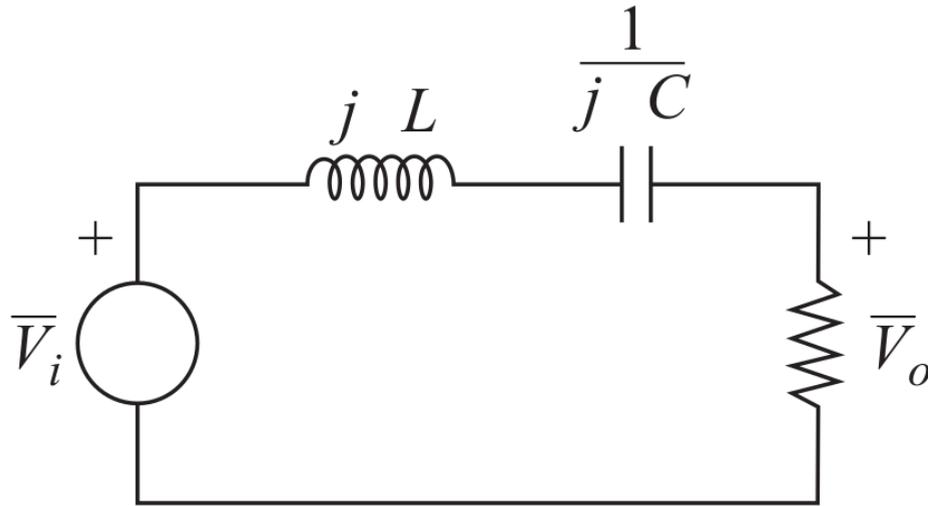
Series Resonant Inverter



Series Resonant Inverter

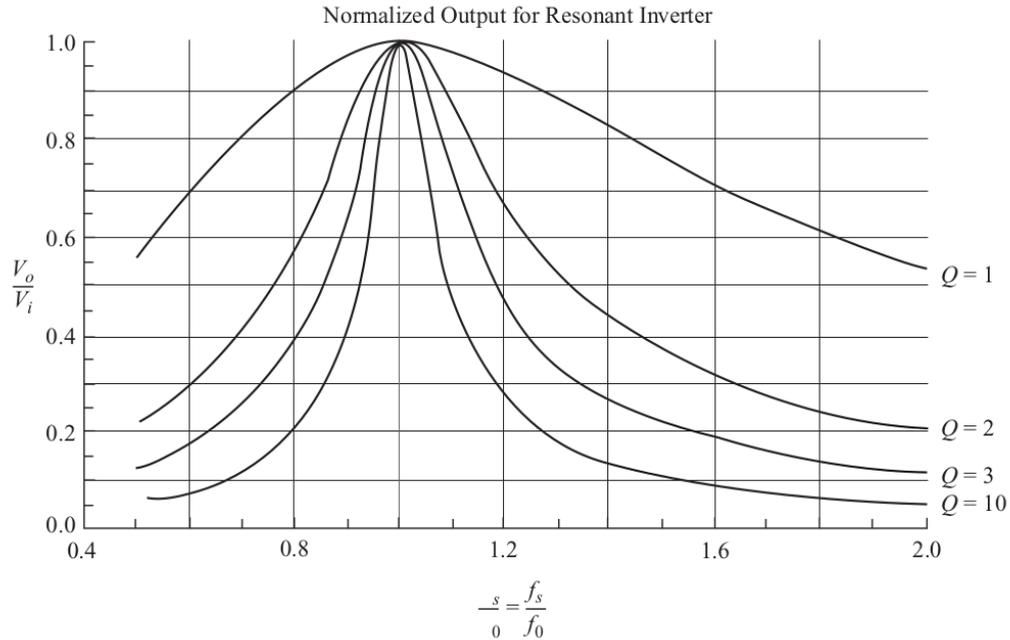


Series Resonant Inverter



Phasor equivalent circuit

Series Resonant Inverter



Frequency Response

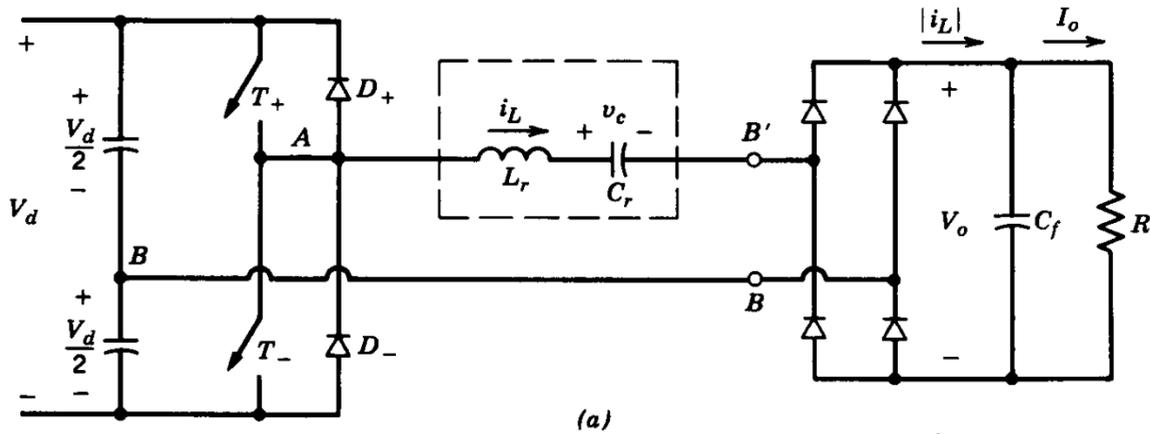
Series Resonant Converter

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Add a diode rectifier to the output of the series resonant inverter

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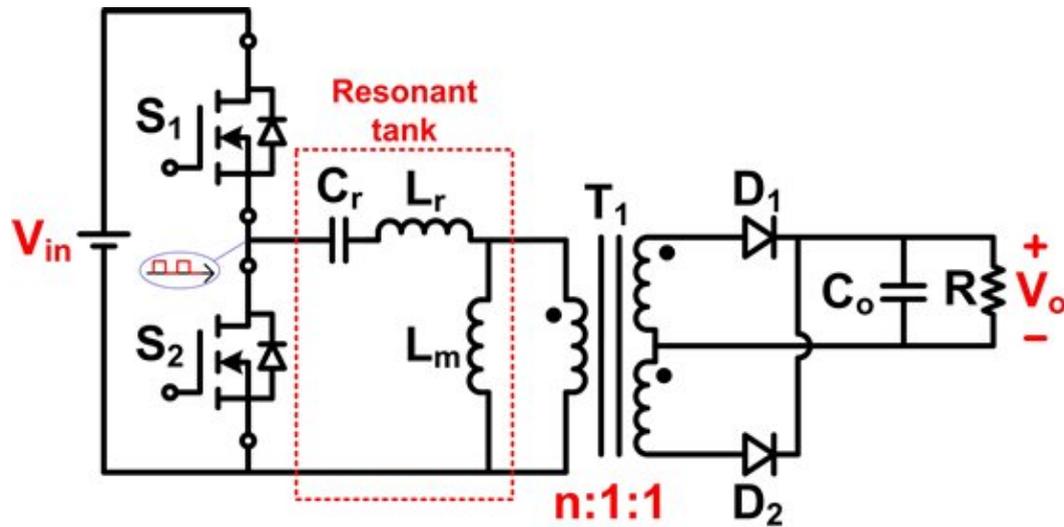
Variations of the Resonant Converters

Variations of the Resonant Converters

LLC Resonant Converter

Variations of the Resonant Converters

LLC Resonant Converter



Resonant Converter (Wireless Power Transfer)



[Qi Wireless Charging](#)

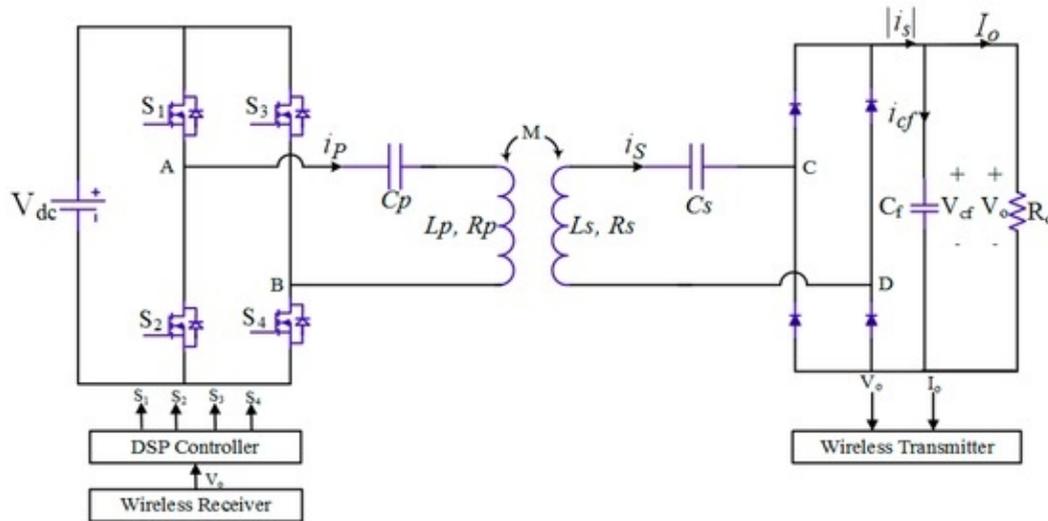
[Multi-Coil Wireless Charger](#)

Resonant Converter (Wireless Power Transfer)



[BMW Electric Car Charger](#)

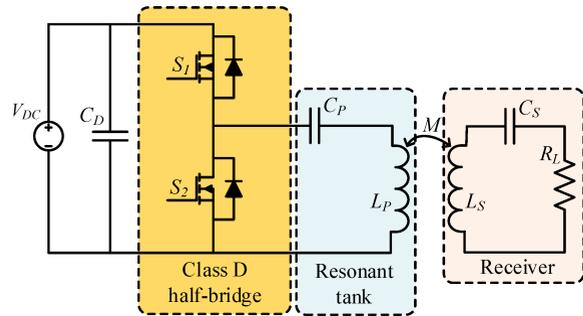
Resonant Converter (Wireless Power Transfer)



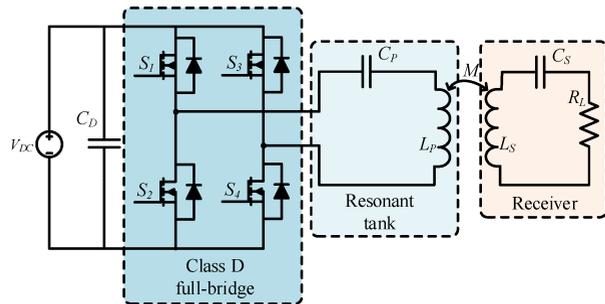
Linearization and Control of Series-Series WPT

Various Configurations

For curious students: Overview of resonant circuits



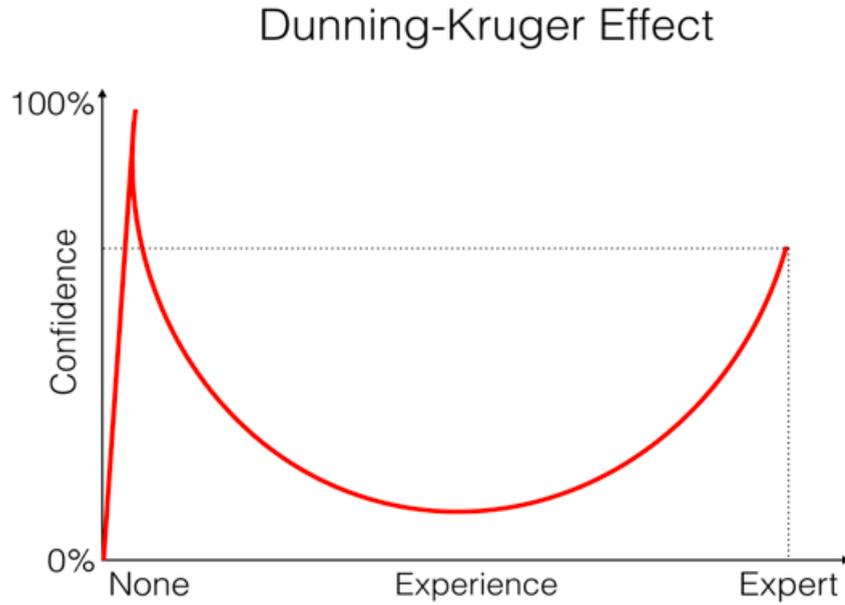
(a)



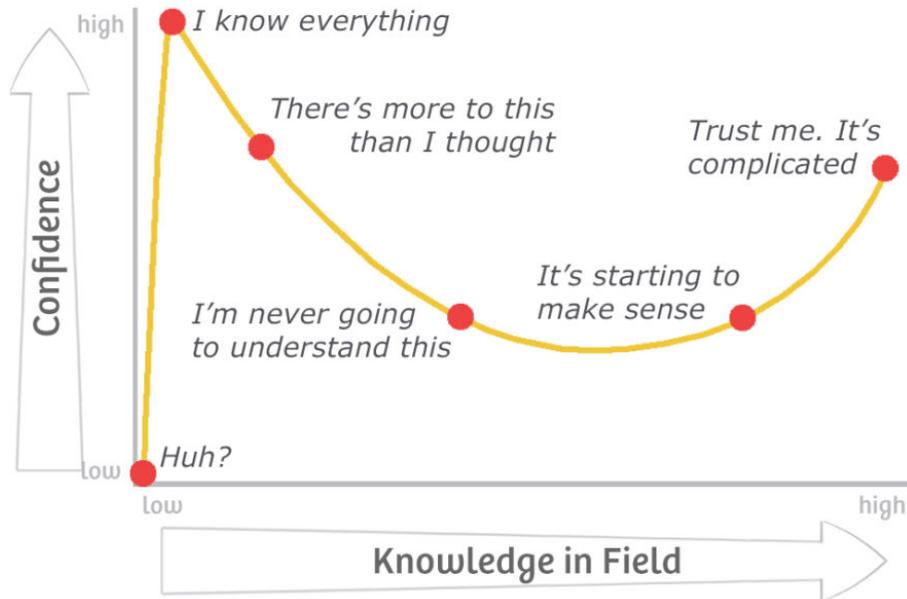
(b)

Dunning-Kruger Effect

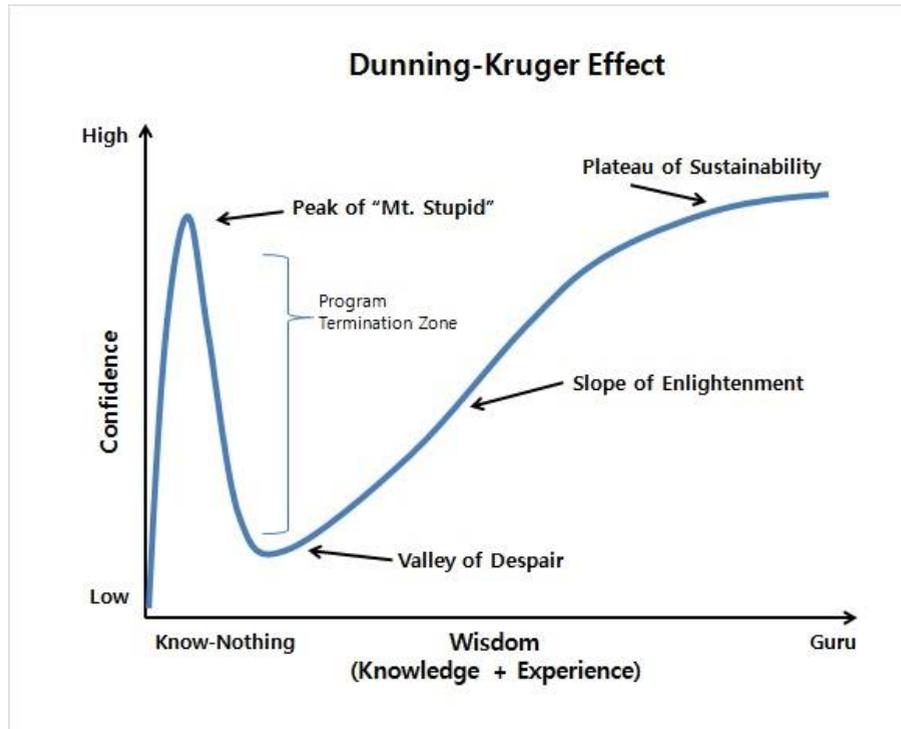
Dunning-Kruger Effect



Dunning-Kruger Effect



Dunning-Kruger Effect



Education in EEE

ODTÜ Elektrik size neler kattı?

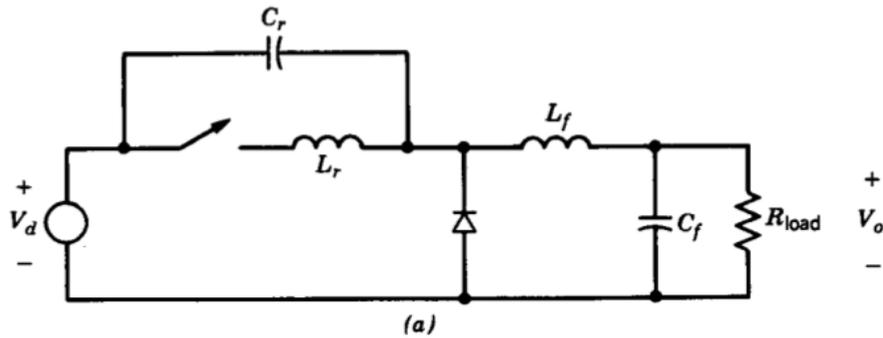
 Drawing

You can download this presentation from:
keysan.me/ee464

Extras

Alternative ZCS Converter

Mohan Section 9.5



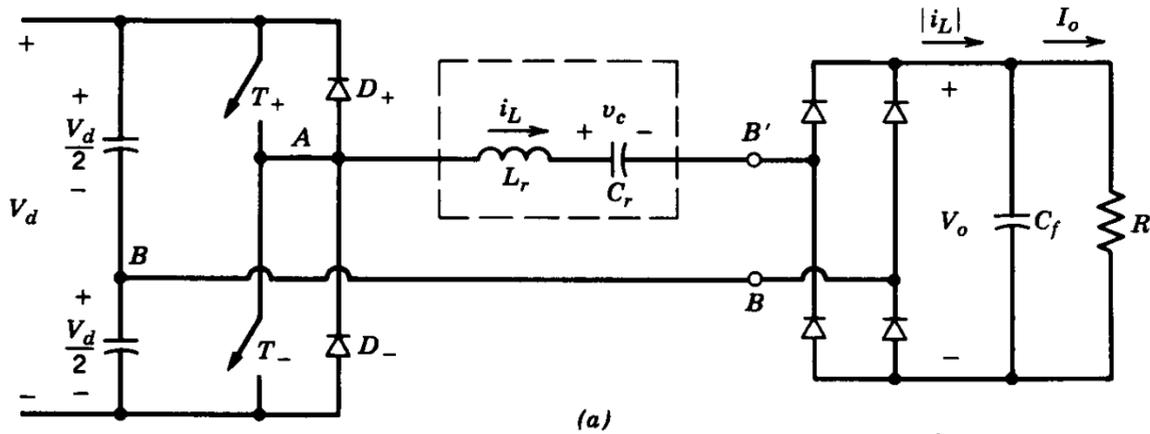
Series Resonant Converter

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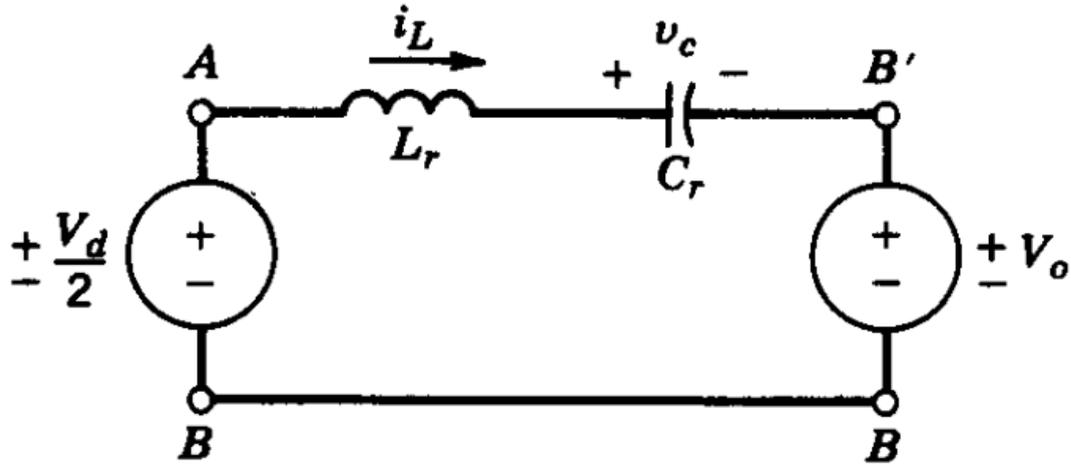
Series Resonant Converter

Series Resonant Converter

Simplified Equivalent Circuit

Series Resonant Converter

Simplified Equivalent Circuit



Series Resonant Converter

Continuous Conduction Mode with $\omega_s > \omega_0$

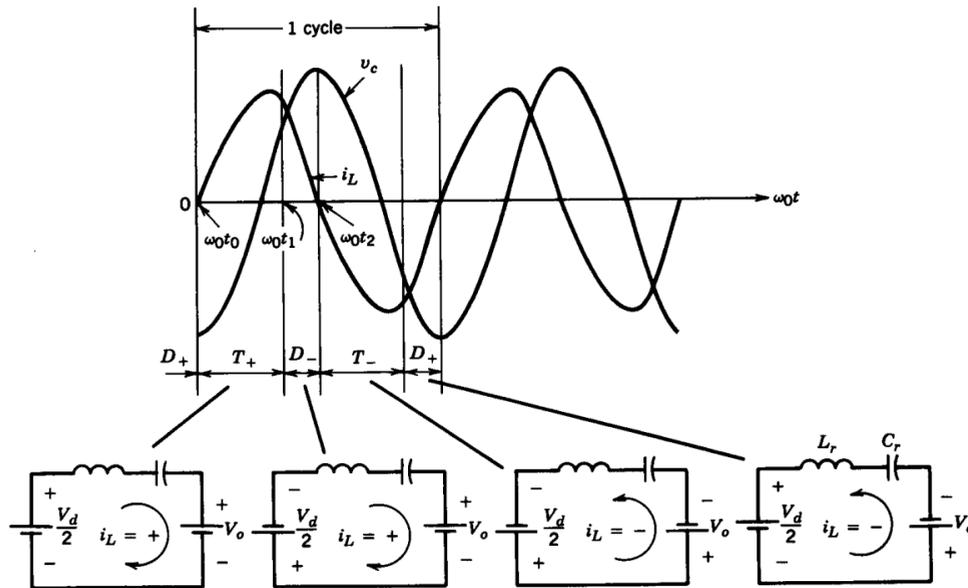


Figure 9-13 SLR dc-dc converter; continuous-conduction mode with $\omega_s > \omega_0$.

Series Resonant Converter

Continuous Conduction Mode with $\omega_s > \omega_0$

- i_L is approximately sinusoidal
- Switches turn on at zero voltage (no turn-on losses)
- but they turn-off at non-zero current (turn-off losses exist)

Series Resonant Converter

Continuous Conduction Mode with $\omega_0/2 < \omega_s < \omega_0$

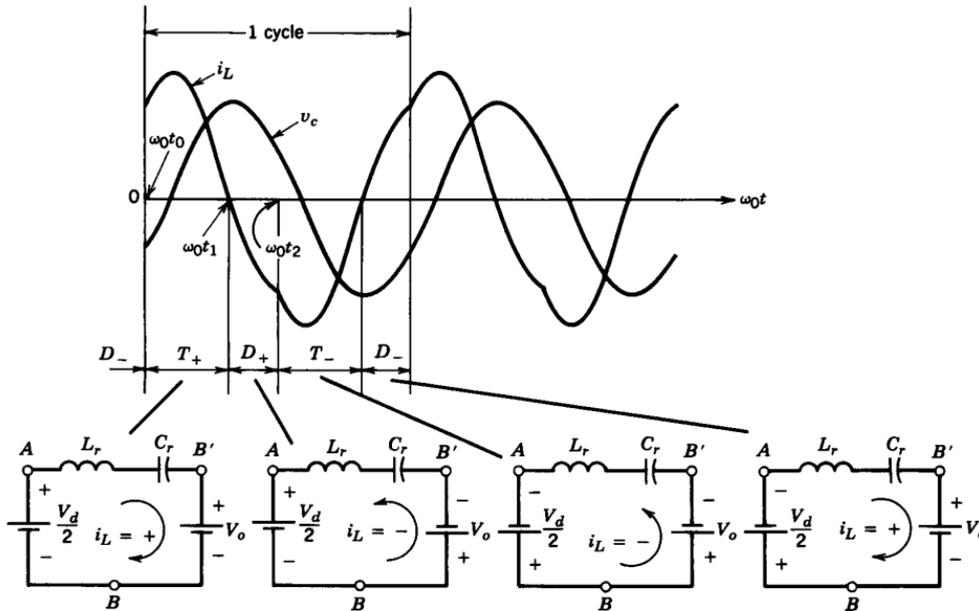


Figure 9-12 SLR dc-dc converter; continuous-conduction mode with $\frac{1}{2}\omega_0 < \omega_s < \omega_0$.

Series Resonant Converter

Continuous Conduction Mode with $\omega_0 / 2 < \omega_s < \omega_0$

- T+ conducts less than 180 degrees
- Switches turn on with finite voltage (turn-on losses exist)
- Switches turn-off with zero current (no turn-off losses)
- Turn-off occurs naturally, so thyristors can be used

Series Resonant Converter

Discontinuous Conduction Mode with $\omega_s < \omega_0/2$

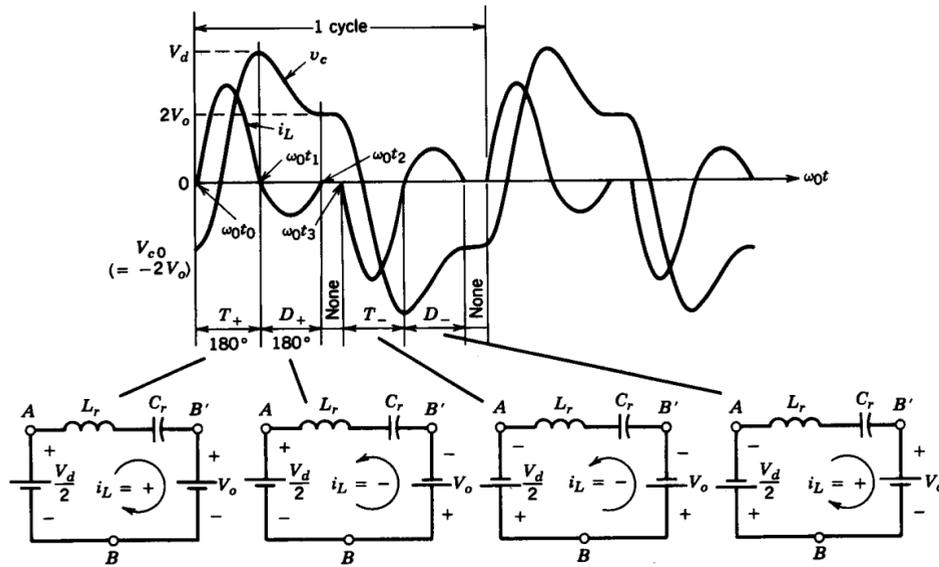


Figure 9-11 SLR dc-dc converter; discontinuous-conduction mode with $\omega_s < \frac{1}{2}\omega_0$.

Series Resonant Converter

Discontinuous Conduction Mode with $\omega_s < \omega_0/2$

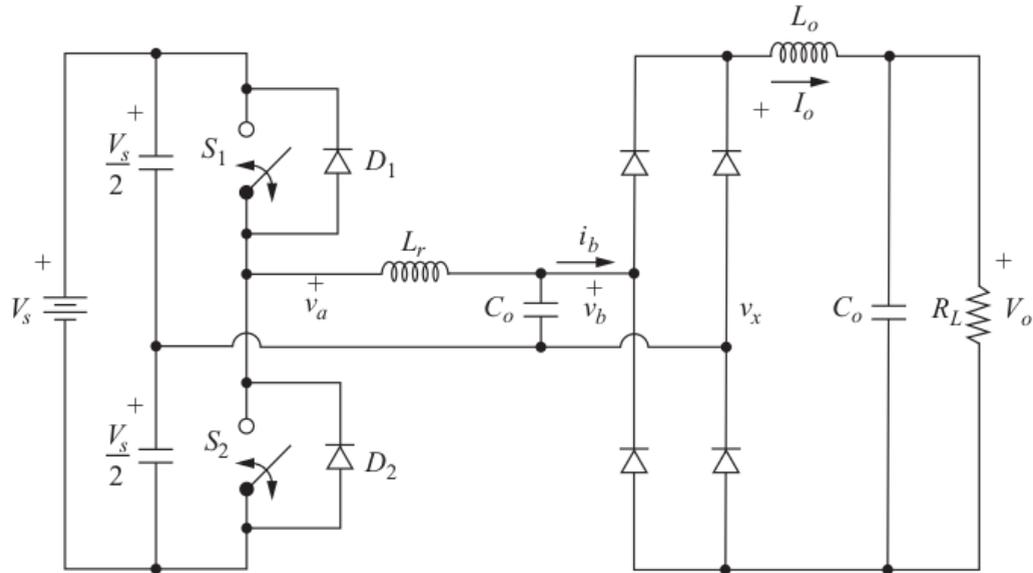
- i_L is zero for some time (discontinuous conduction)
- Switches turn on at zero current, with finite voltage
- Switches turn-off naturally with zero current (no turn-off losses)
- Thyristors can be used
- Disadvantage: Relatively large peak current in the circuit

Variations of the Resonant Converters

Parallel Resonant Converter

Variations of the Resonant Converters

Parallel Resonant Converter

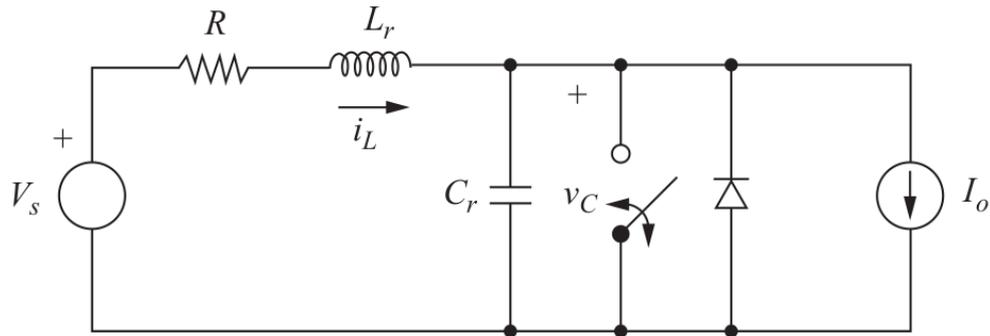


Variations of the Resonant Converters

Resonant DC Link Converter

Variations of the Resonant Converters

Resonant DC Link Converter



Variations of the Resonant Converters

3-Phase Resonant DC Link Converter

Variations of the Resonant Converters

3-Phase Resonant DC Link Converter

