

# CENG 732 Computer Animation

Spring 2006-2007  
Week 7  
Natural Phenomena

## This week

- Modeling plants
  - L-System
- Modeling clouds
  - Volumetric Procedural Methods

## Modeling Plants

- Using fractals seems to be appropriate to model plants, because of observed self-similarity at various levels



- But how to define the fractal? What about the stochastic behavior?

## Animation

- In addition to rendering static plants we should also think about the motion to animate:
  - Motion due to environmental conditions such as wind
  - Plant growth

## L-System

- Introduced and developed in 1968 by the Hungarian theoretical biologist and botanist Aristid Lindenmayer
- Formal Grammar consisting of a set of production rules
- Famously used to model the growth processes of plant development
- Can be used to generate self-similar fractals
- A procedural technique to model objects

## D0L-System

- A deterministic and context-free L-System
  - Implies each non-terminal has a single grammar rule associated with it
  - And the left part of a grammar rule consists of a single non-terminal (i.e., no-context information)

## D0L-System Example

S → ABA  
A → XX  
B → TT

Production rules

S ← axiom

ABA  
XXTTXX

String sequence

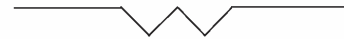
## Geometric Interpretation of L-Systems

- Geometric Replacement:
  - Replace each symbol with a geometric element

XXTTXX  
String

X : ——— T : 

Geometric replacement rules



Geometric interpretation

## Turtle Graphics

- Replace each symbol with a drawing command

Symbol	Turtle Graphic Interpretation
F	Move forward a distance $d$ while drawing a line. Its state will change from $(x, y, \alpha)$ to $(x + d \cdot \cos\alpha, y + d \cdot \sin\alpha, \alpha)$ .
f	Move forward a distance $d$ without drawing a line. Its state will change as above.
+	Turn left by an angle $\delta$ . Its state will change from $(x, y, \alpha)$ to $(x, y, \alpha + \delta)$ .
–	Turn right by an angle $\delta$ . Its state will change from $(x, y, \alpha)$ to $(x, y, \alpha - \delta)$ .

## Turtle Graphics

- Given the initial state of the cursor and the linear and rotational step sizes, a string can be used to draw a shape
- The state of the cursor at any point can be given by the current position and heading of the cursor

## Turtle Graphics



S → ABA  
A → FF  
B → TT  
T → -F++F-

Production rules

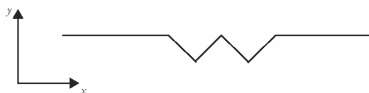
S ← axiom

ABA  
FFTTF  
FF-F++F--F++F--FF

Sequence of strings produced from the axiom

$d =$    
 $\delta = 45^\circ$   
reference direction:   
initial state: (10, 10, 0)

Initial conditions



Geometric interpretation

## Linearity Problem

- With only the four commands of draw/move/turn\_left/turn\_right one can only generate linear shapes.
- Bracketed L-systems are introduced to provide branching
- In the generation rules, a left branch indicates to push the current state on the stack and a right branch indicates a popping of the state from the stack and setting it as the current state.
- The stack structures provides unlimited branching

## Bracketed L-Systems

Symbol	Turtle Graphic Interpretation
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[	Push the current state of the turtle onto the stack
]	Pop the top of the state stack and make it the current state

$$\begin{aligned}
 S &\Rightarrow FAF \\
 A &\Rightarrow [+FBF] \\
 A &\Rightarrow F \\
 B &\Rightarrow [-FBF] \\
 B &\Rightarrow F
 \end{aligned}$$

Non-deterministic, context-free

## Examples

FFF

F[+FFF]F

F[+F[-FFF]F]F



## Stochastic L-systems

- To deal with non-determinism, one can assign probabilities to production rules

$$\begin{aligned}
 S_{1,0} &\Rightarrow FAF \\
 A_{0,8} &\Rightarrow [+FBF] \\
 A_{0,2} &\Rightarrow F \\
 B_{0,4} &\Rightarrow [-FBF] \\
 B_{0,6} &\Rightarrow F
 \end{aligned}$$

## Context Sensitive L-Systems

- You may provide a context for the left side of the grammar rule, to restrict the application of grammar rules to certain contexts

$$\begin{aligned}
 S &\Rightarrow FAT \\
 A > T &\Rightarrow [+FBF] \\
 A > F &\Rightarrow F \\
 B &\Rightarrow [-FAF] \\
 T &\Rightarrow F
 \end{aligned}$$

S  
FAT  
F[+FBF]F  
F[+F[-FAF]F]F

Production rules

String sequence

## Animating Plant Growth

- Changes in topology during growth
- Elongation of existing structures
- Elongation of structures may be animated by small linear step size and using rules such as  $F \rightarrow FF$
- Changes in topology is animated by the bracketing mechanism
  - However, we should not scan and render the final generated string left to right, the rendering should be done as we proceed

## Parametric L-Systems

- Symbols may have one or more parameters associated with them
  - We can specify different linear, angular step sizes

$$\begin{aligned}
 S &\Rightarrow A(0) \\
 A(t) &\Rightarrow A(t+0.01) \\
 A(t) : t >= 1.0 &\Rightarrow F
 \end{aligned}$$

$$A(t_0) < A(t_1) > A(t_2) : t_2 > t_1 \ \& \ t_1 > t_0 \Rightarrow A(t_1 + 0.01)$$

## Timed L-Systems

- A symbol has an initial age and terminal age associated with it. A global time tracks the animation time and local times associated with each symbol determines when the rules are used to generate the next symbol.

axiom: (A,0)

(A,3) => (S,0) [+ (B,0)] (S,0)

(B,2) => (S,0)

## Examples

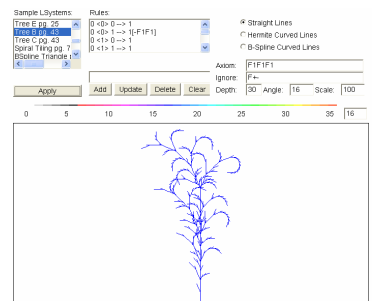


## Examples

- [L-System Movie 1](#)
- [L-System Movie 2](#)

## Example Applet

- [Applet](#)



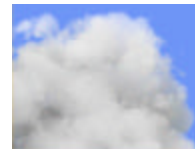
## Realistic Modeling of Clouds

- Most of the teaching material used in these slides (including the material in the book) is taken from David Ebert's work on cloud generation  
– <http://cobweb.ecn.purdue.edu/purpl/projects/astclouds/frames.html>



## Cloud Types

- Cumulus



- Cirrus



## Visual Characteristics of Clouds

- Clouds have volumetrically varying amorphous structure with detail at many different scales
- Cloud formation often results from swirling, bubbling, and turbulent processes
- Clouds have several illumination and shading characteristics

## Volumetric Cloud Modeling

- Two level hierarchy
  - Implicit volumes to represent the global structure of the cloud (the cloud macrostructure)
    - Modeled by implicit functions (such as spheres)
  - Procedural methods to define turbulent, noise characteristics at a smaller scale (the cloud microstructure)
    - Modeled by turbulent volume densities

## Volumetric Cloud Modeling

- The macro and micro models are combined to define a volumetric density function (*vdf*) over a 3D volumetric space
- The densities of the implicit volumes can be combined by using a cubic blending function and a weighted sum

$$F(r) = -\frac{4}{9} \cdot \frac{r^6}{R^6} + \frac{17}{9} \cdot \frac{r^4}{R^4} - \frac{22}{9} \cdot \frac{r^2}{R^2} + 1$$

$$D(p) = \sum_i w_i \cdot F(|p - q_i|)$$

## Volumetric Cloud Modeling

- To combine the densities from implicit primitives with the turbulence-based densities a user specified blend percentage can be used (60% to 80% gives good results).

## Videos

- [Cumulus forming](#)
- [Flying through a cloud](#)
- [Cirrus](#)
- [Rolling cloud scene](#)

## The Swell Software

- [How to build a cloud](#)

