

EE-362

Review of Electromechanical Energy Conversion

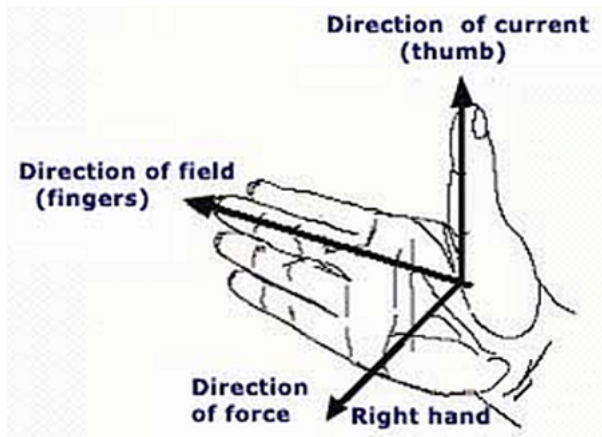
Ozan Keysan

keysan.me

Office: C-113 • Tel: 210 7586

Lorenz Force

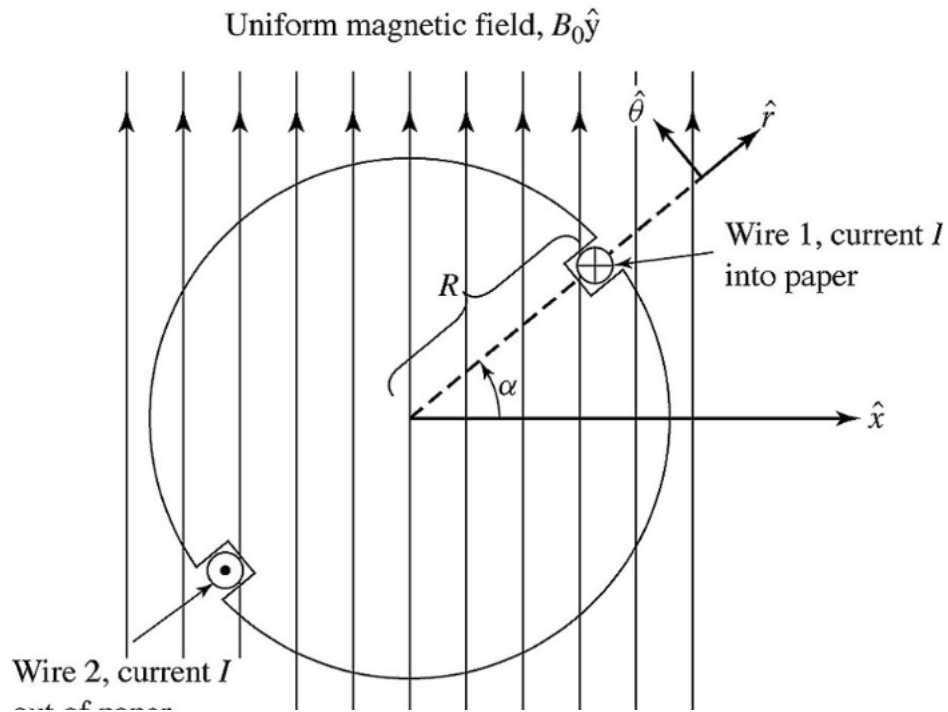
$$\vec{F} = \vec{J} \times \vec{B}$$



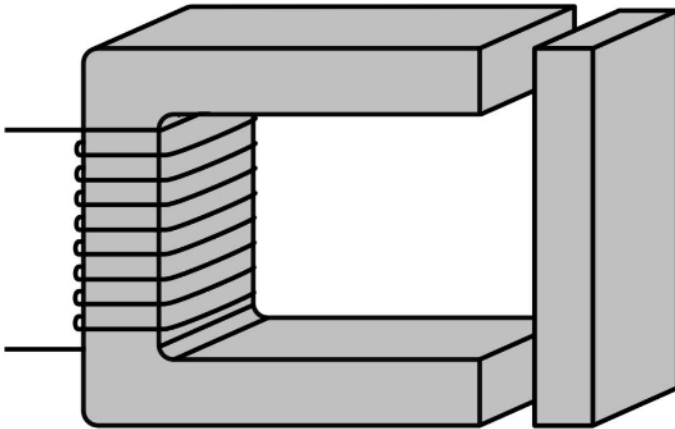
Lorenz Force Applications

- [Force Demo](#)
- [Homopolar Motor](#)
- [World's Simplest Electric Train](#)
- [Electromagnetic Aircraft Launcher](#)
- [Navy Railgun, Railgun-2](#)
- [Aselsan Tufan](#)
- [Aselsan Tufan-2](#)

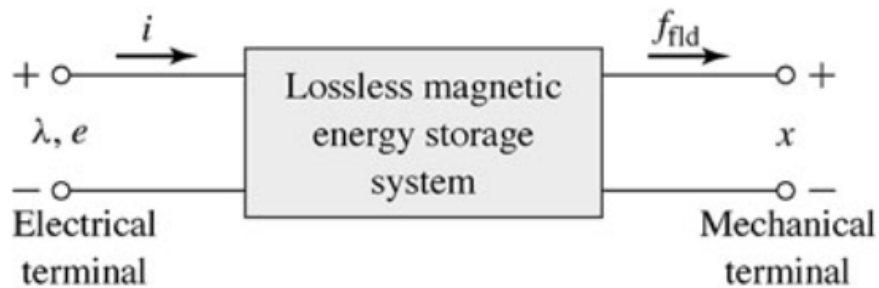
Determine the direction of rotation



What would happen in the device below?

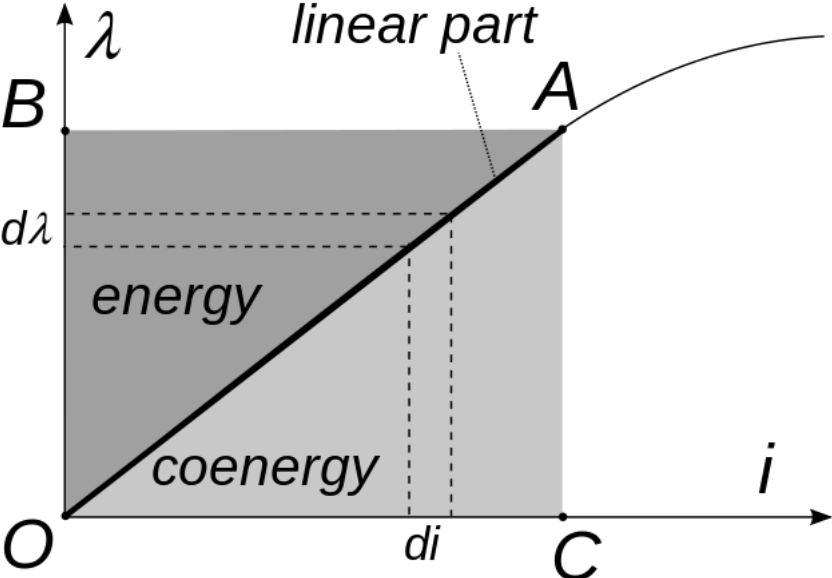


Link Between Electrical and Mechanical Systems



Electric Energy Input = Stored Magnetic Energy + Mechanical Work

Review: Magnetic Energy



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$$W_{stored} = \int_0^\lambda i(\lambda) d\lambda$$

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$$W_{stored} = \int_0^\lambda i(\lambda) d\lambda$$

or from B-H curve

$$W_{stored} = \int_{\text{volume}} \left(\int_0^B H dB \right)$$

Magnetic Energy

In Linear Systems:

Magnetic Energy

In Linear Systems:

Magnetic Energy = Magnetic Co-Energy

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Magnetic Energy + Magnetic Co-Energy = λi

Magnetic Energy

In Linear Systems:

Magnetic Energy = Magnetic Co-Energy

Magnetic Energy + Magnetic Co-Energy = λi

Thus (only in linear systems)

$$W(\text{magnetic}) = \frac{1}{2} \lambda i = \frac{1}{2} L i^2 = \frac{1}{2L} \lambda^2$$

Force from the Stored Energy



Force from the Stored Energy



Derivative of Energy w.r.t. position gives the force!

Force from Stored Energy

Take derivative of magnetic energy

Force from Stored Energy

Take derivative of magnetic energy

$$Force = - \frac{\partial W_{mag}(\lambda, x)}{\partial x} \Big|_{\lambda=constant}$$

Some useful reading:

- [MIT From Lasers to Motors](#)
- [Fitzgerald-Electromechanical Energy Conversion](#)

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For Linear Systems

$$Force = - \frac{\partial}{\partial x} \left(\frac{\lambda^2}{2L(x)} \right) = \frac{\lambda^2}{2L(x)^2} \left(\frac{dL(x)}{dx} \right)$$

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$$Force = \frac{1}{2} i^2 \frac{dL(x)}{dx}$$

Summary

Magnetic Circuit Tries

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- To minimize the reluctance ($L = N^2/R$)

Some Applications

Some Applications

How a speaker works?

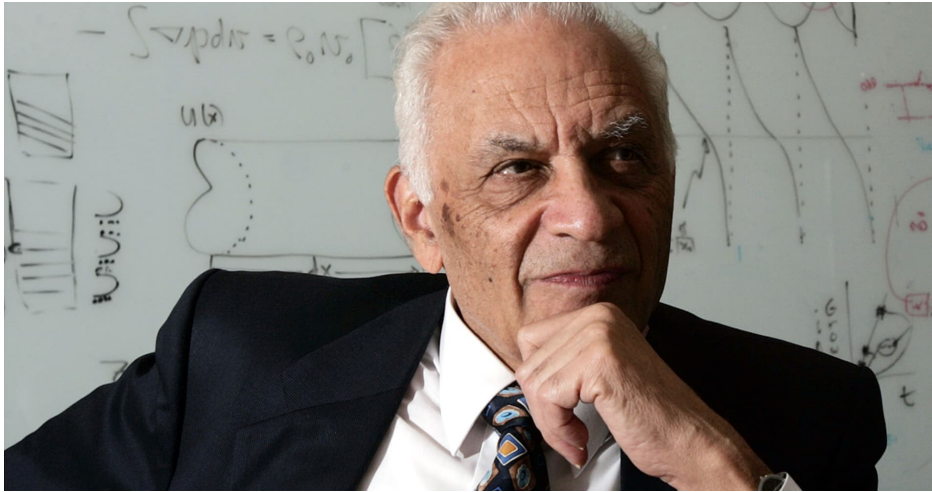


You can think it is just a basic solenoid, but it's more complex than that.

How Speakers Work

(Reading assignment)

Who is this guy?



Amar Bose

Founder of Bose Corp, MIT Professor, Electrical Engineering



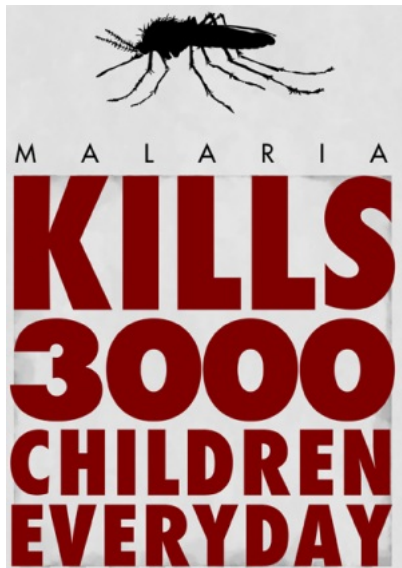
How Amar Bose used research to build better speakers

Now MIT owns the majority shares in Bose Corp.

Magnetism in Medicine:

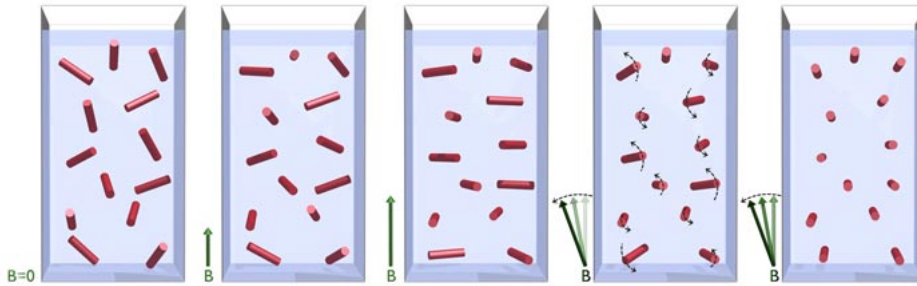
Magnetism in Medicine:

Malaria



Malaria vs Permeability

Diagnosis using Magnetic Alignment



[Physicists detect malaria using light and magnets](#)

[Magnets diagnose malaria in minutes](#)

Malaria Treatment



[Malaria's Magnetic Properties May Pull Treatments Forward](#)

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Mechanical Power & Energy:

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Rotational:

Mechanical Power & Energy:

$$\text{Linear Motion: } P = Fv = F \frac{dx}{dt} \text{ Watt}$$

$$\text{Rotational: } P = T\omega = T \frac{d\theta}{dt} \text{ Watt}$$

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Rotational Acceleration:

Linear Acceleration:

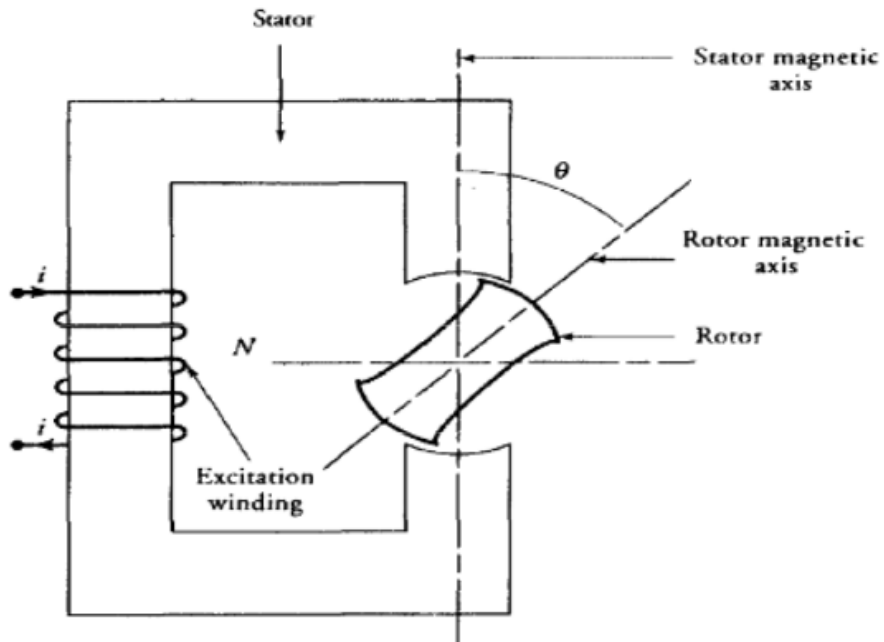
$$F = ma = m \frac{dv}{dt}$$

Rotational Acceleration:

$$T = J \frac{d\omega}{dt} \text{ Watt}$$

J: Rotational Inertia (kgm^2)

Can you guess the torque expression in this circuit?



Rotational Systems:

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Remember in linear systems:

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In rotational systems, just take the derivative wrt θ not x :

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[More information](#)

Rotational Systems:

Take the derivative wrt θ not x :

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Take the derivative wrt θ not x :

$$T = -\frac{1}{2} \Phi^2 \frac{dR(\theta)}{d\theta} \Big|_{\Phi=\text{constant}}$$

or alternatively

$$T = \frac{1}{2} I^2 \frac{dL(\theta)}{d\theta} \Big|_{i=\text{constant}}$$

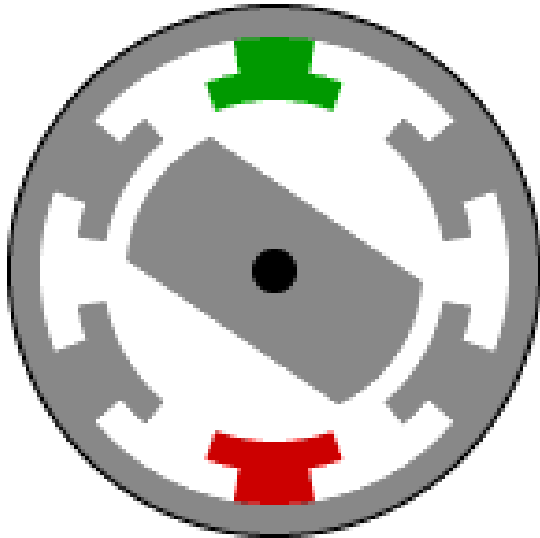
How can we achieve a constant rotation?

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Single Phase Reluctance Motor

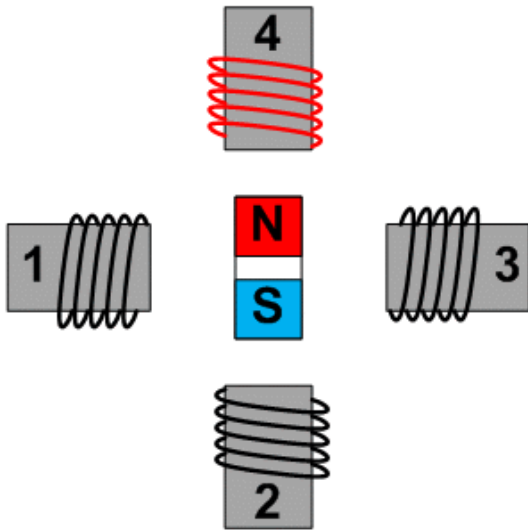
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Single Phase Reluctance Motor



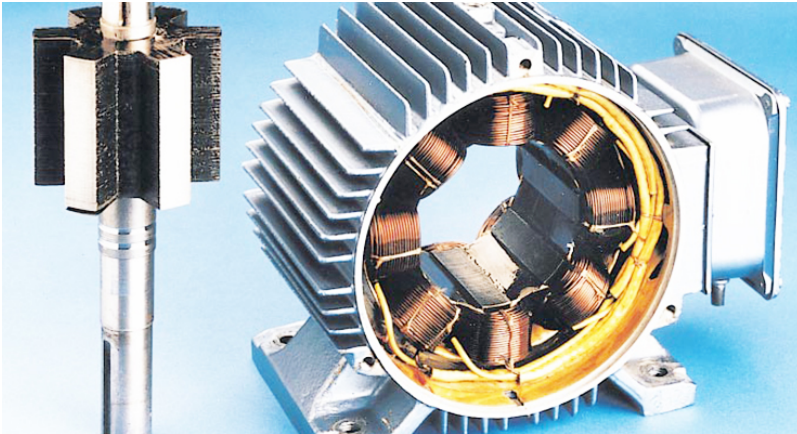
Single Phase Reluctance Motor

Single Phase Reluctance Motor



[Magnetic Flux](#), [Micro-stepping for higher accuracy](#).

Reluctance Motors



[More info](#)

Magnetorquer: How small satellites align themselves?



[Magnetorquer](#)

[CubeSat Magnetorquer](#)

Who is this guy?

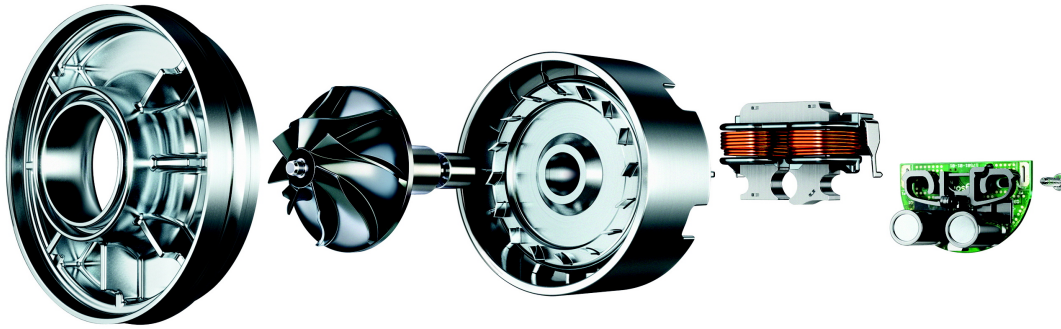


James Dyson



[Digital Motor](#), [Operating Principle](#), [Manufacturing](#)

Dyson uses Reluctance Motors



[Digital Motor](#), [Operating Principle](#), [Manufacturing](#)

Summary

Magnetic Circuit Tries

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Magnetic Circuit Tries

- To maximize the inductance, to minimize the reluctance ($L = N^2/R$)
- To decrease the magnetic energy (increase co-energy)

Rotational systems are similar to linear systems, but take the derivative of magnetic energy in terms of θ instead of x .

You can download this presentation from:
keysan.me/ee362