

1. Calculate the following integrals:

(a)  $\int_0^1 dx x^{2.1}$

(b)  $\int_0^\pi d\theta \sin \theta$

(c)  $\int_0^\pi d\theta \sin^2 \theta$

(d)  $\int_0^\pi d\theta \tan \theta$

(e)  $\int_1^2 d\theta \frac{1}{x}$

(f)  $\int_0^3 dx e^{-x}$

(g)  $\int_0^3 dx x^2 e^{-x}$

(h)  $\int_0^\infty dx e^{-x^2}$

2. Calculate the derivatives of the following functions with respect to  $x$ . Also evaluate the value of this derivative at  $x = 1$

(a)  $x, x^{1.5}$

(b)  $\cos x, \sin x, \tan x$

(c)  $x^2 \tan x, \frac{1}{x} \sin x$

3. How many atoms are there in a person of 73  $kg$  if the composition (by mass) of human body is 65%  $O_2$ , 18.5%  $C_2$ , 9.5%  $H_2$ , 3.3%  $N_2$ , 1.5%  $Ca$ , 1%  $P$  and 0.35% other elements? (Hint: Ignore other elements)

4. The motion of a rocket burning its fuel at a constant rate while moving through empty interstellar space can be described by

$$x = u_{ex}t + u_{ex}\left(\frac{1}{b} - t\right) \ln(1 - bt)$$

where  $u_{ex}$  and  $b$  are constants ( $u_{ex}$  is the exhaust velocity of the gasses at the tail of the rocket and  $b$  is proportional to the rate of fuel consumption).

(a) Find a formula for the instantaneous velocity of the rocket

(b) Find a formula for the instantaneous acceleration.

(c) Suppose that a rocket with  $u_{ex} = 3.0 \times 10^3 \text{ m/s}$  and  $b = 7.5 \times 10^{-3} /s$  takes  $120 \text{ s}$  to burn all its fuel. What is the instantaneous velocity at  $t = 0 \text{ s}$ ? At  $t = 120 \text{ s}$

(c) What is the instantaneous acceleration at  $t = 0 \text{ s}$ ? At  $t = 120 \text{ s}$ ?