

Section: \_\_\_\_\_

Name: \_\_\_\_\_

**AE 361 Applied Elasticity in Aerospace Engineering**

**Fall 2009**

**Midterm II**

**December 28, 2009 (5:30 pm – 7:30 pm)**

**You can use simple calculators as discussed in class.**

**Closed book exam. No notes. Formula sheet will be handed out in class.**

**Please show all your work.**

**Restate the problem in your solution sheet and draw a free body diagram!**

Problem 1: 20 points

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Problem 2: 40 points

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Problem 3: 40 points

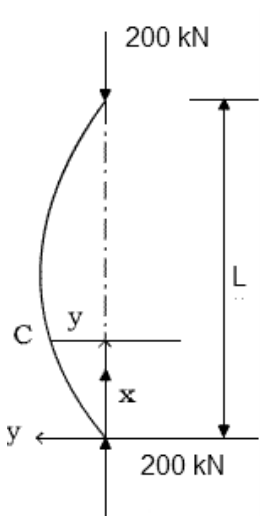
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Total : 100 points

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Problem 1.

A 2-m-long pin-ended column of rectangular cross section ( 12mm x 6 mm) is to be made of wood. Assuming  $E=13$  GPa, and using a factor of safety of 2.5, determine the minimum buckling load. Assume an Euler column.

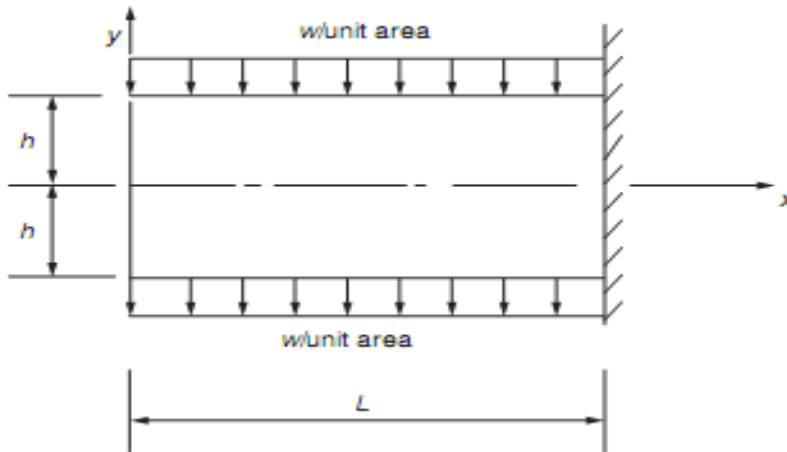


### Problem 2.

The cantilever beam shown in the Figure is in a state of plane strain and is rigidly supported at  $x=L$ . Examine the following stress function in relation to this problem:

$$\phi = \frac{w}{20h^3}(15h^2x^2y - 5x^2y^3 - 2h^2y^3 + y^5)$$

Show that the stresses acting on the boundaries satisfy the conditions except for a distributed direct stress at the free end of the beam which exerts no resultant force or bending moment.



### Problem 3.

A steel rod of diameter  $d = 50$  mm ( $S_y = 260$  MPa) supports an axial load  $P = 50R$  and vertical load  $R$  acting at the end of an  $0.8$ -m long arm. Determine the stresses at point A and draw a schematic of the stress state at point A. Given a factor of safety  $n = 2$ , compute the largest permissible value of  $R$  using the following criteria: (a) maximum shearing stress and (b) maximum energy of distortion.

