

MATLAB FOR PATTERN RECOGNITION

MIN 720 – Pattern Classification for Biomedical
Applications

05/04/2011



How Much Do We Know?

- Anybody who has never used MATLAB?



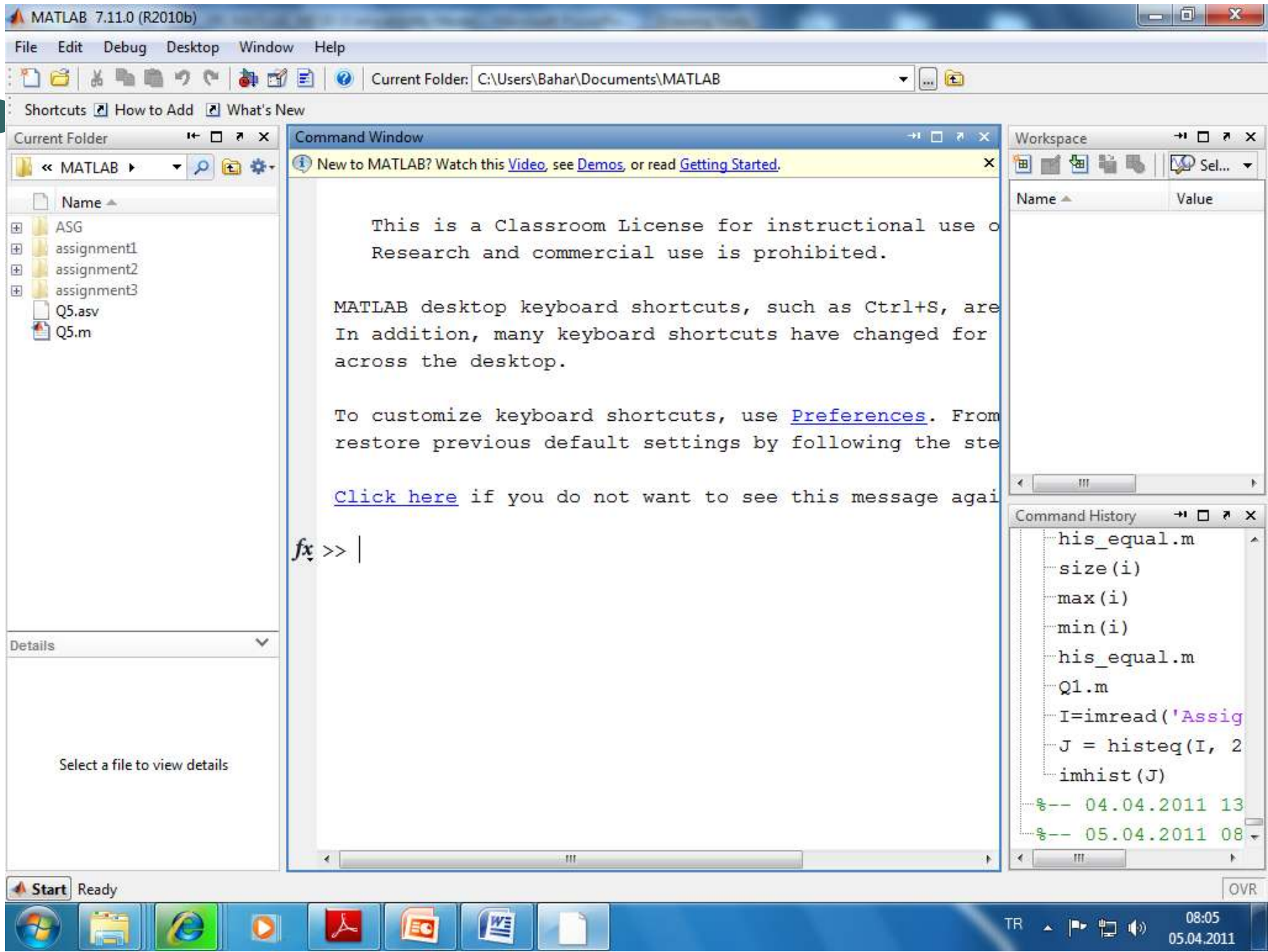
Outline

- An Introduction to MATLAB
- Generation of Random Data
- Basic Statistical Functions
- Parameter/Density Estimation Functions
- Classification/Clustering Functions
- MATLAB Toolboxes for Pattern Recognition



MATLAB Environment

- Workspace: Variables defined so far.
- Command History
- Command Window
- Editor
- Plot Window
- Current Directory: Start by setting the current directory to the directory that you are working. Generally, it is where your files are.
- Workspace Window





LOOKFOR & HELP

- LOOKFOR: Type 'lookfor smth' to learn the name of functions that are related to 'smth'.
- HELP: Type 'help function_name' to learn how that function works, its inputs and outputs.



Expressions

- Variables:
 - No need to make type declarations or dimension statements
 - When Matlab encounters a new variable name, it automatically creates the variable and allocates the appropriate amount of storage.

Example:

```
>> num_students = 25
```

Creates a 1-by-1 matrix named num_students and stores the value 25 in its single element



Expressions

- Cell:
 - A matrix which can store a separate variable (matrix with different dimensions, etc.) in each of its indices.
 - Useful for storing many matrices in a single structure in a compact manner.

Example:

```
a=cell(2,2);
```

```
a{1,1}=[2 4];
```

```
a{1,2}=[5 8; 8 9];
```




Expressions

- Structures:
 - Can store different attributes of an object in a single structure (like in Object Oriented Programming).

Example:

```
student.year = 3;
```

```
student.number=1556782;
```

Creates a structure and stores the declared attributes.



Functions

- Standard elementary mathematical functions; abs, sqrt, exp, sin ...
- For a list of elementary mathematical functions type
`>> help elfun`
- For a list of more advanced mathematical and matrix functions type
`>>help specfun`
`>>help elmat`
- Most of the functions are overloaded.



Vectors and Matrices

- **Scalar:** '5', pi ...
- **Vector:** Ordered list of numbers

Example: to represent a point in three dimensional space

```
>>p1=[1 3 4]
```

```
p1 = 1 3 4
```

```
>>p2=[1;3;4]
```

```
p2 = 1
```

```
     3
```

```
     4
```



Accessing a Vector

- Access to the elements of vectors

```
>>p1(1)
```

```
ans =
```

```
1
```



Creating Matrices

- **Matrices:**

```
>> a = [ 1 2 2 1 ]
```

```
a = 1 2 2 1
```

```
>> b = [1; 2; 2; 1]
```

```
b =
```

```
1
```

```
2
```

```
2
```

```
1
```

```
>> c = zeros(1,2);
```

```
c = 0 0
```

```
>> d = ones(1,3);
```

```
d = 1 1 1
```



Creating Matrices from Vectors

- It is possible to create matrices from row or column vectors, as long as all of the vectors being used to create the matrix have the same number of elements.
- Examples...



Accessing a Matrix

- Accessing element of a matrix

```
>>a=[2 4; 5 8];
```

```
>>a(1,:)
```

```
2 4
```

```
>>a(:,2)
```

```
5
```

```
8
```

- Accessing subset of a matrix

```
>>b=[1 2 3 ; 4 5 6; 7 8 9];
```

```
>>b(2:3,2:3)
```

```
5 6
```

```
8 9
```



Matrix Operations

- Matrix operations like, (for matrices “x” and “y”)
 - Determinant of a matrix ($\det(x)$)
 - Inverse of a matrix (x^{-1}) or $\text{inv}(x)$
 - Transpose of a matrix (x')
 - Element by element multiplication($x.*y$), division($x./y$)
 - Matrix multiplication($x*y$), division(x/y), summation($x+y$), subtraction($x-y$)
 - ... are defined in MATLAB.



Flow Control-IF

```
>> if a+b==5
    m=1;
elseif a+b==3
    m=2;
end
>>
```



Flow Control-Switch

```
>> switch (n)
  case 0
    M=0
  case 1
    M=1
  otherwise
    M=2
end
```



Loops

For/End

```
a = [ 0.8 0.1; 0.2 0.9 ; 0.4 0.6]
```

```
>> for i = 1:1:3  
    x(i,:) = a(i,:).*i  
end
```



While/End

- `a=3; ax=0`
- `while a==3`
- `ax=ax+2`
- `if ax>50`
- `a=4`
- `end`
- `end`
- Avoid using Loops in Matlab.



M-Files: Scripts And Functions

- **Scripts:** Do not accept input arguments or return output arguments. They operate on data in the workspace.
- **Functions:** can accept input arguments and return output arguments. Internal variables are local to the function.



Function Definition

- Name of the function and the file should be the same.

```
function[output1,output2]=example(input)
```



Graphical Representation

- Generally 'plot' is used for drawing graphics.

```
>>plot(x) ;
```

plots the columns of x versus their index.

Many options are provided for this function. 'stem' can also be used.

- "imagesc" is used to display an image or visualize a 2D matrix.

```
figure
```

```
imagesc(A)
```

```
colormap(gray)
```



Read & Write Files

- Load, Save, Saveas
- Textread
- ...
- There are many other functions for file operations. Check File I/O part in Mathwork's Help.



Generating Random Data

There are many functions for generating random samples from a desired distribution with the specified parameters.

➤ `random('name',a,b,c,...)` creates a matrix with the specified dimensions whose entries are samples drawn from the specified distribution.

```
>> x1 = random('unif',0,1,2,4)
```

```
0.8003    0.4218    0.7922    0.6557
```

```
0.1419    0.9157    0.9595    0.0357
```



Generating Random Data

- `normrnd(mu,sigma,m,n)` creates a $m \times n$ matrix whose entries are samples drawn from a normal distribution with specified parameters.

```
>> normrnd(50,10,2,5)
```

```
45.674  51.253  38.535  61.891  53.272
```

```
33.344  52.876  61.909  49.623  51.746
```

- `exprnd(mu,m,n)` creates a $m \times n$ matrix from an exponential distribution.

```
>>exprnd(30,2,3)
```

```
13.1593  12.4551  37.1646
```

```
6.0277  32.1909  32.2592
```



Generating Random Data

- `mvnrnd(mu,cov,n)` creates a $n \times d$ matrix whose indices are drawn from a d dimensional multivariate gaussian distribution.

```
>> mu=[5 10];
```

```
>> cov=[2 -1; -1 3];
```

```
>> mvnrnd(mu,cov,3)
```

```
6.7734 10.0164
```

```
2.7461 10.4947
```

```
2.9622 12.1099
```

There are also functions for random data generation of other common distributions.

● ● ● | Likelihood Evaluation Functions

➤ They calculate likelihood for a specific distribution in a given point.

➤ `normpdf(x,mu,sigma)`

```
>> normpdf(4,5,1)
```

```
0.2420
```

➤ `exp pdf(x,mu)`

```
>> exp pdf(10,20)
```

```
0.0303
```

➤ (`betapdf()`, `mvnpdf()`, etc.)



Basic Statistical Functions

- Functions for calculating the descriptive statistics of distributions.
- `mean(x)` returns the mean value of a 1D matrix.

```
>>x=[2 8 4];
```

```
>> mean(x)
```

```
4.6667
```

- `Std(x)` returns the standard deviation (with Bessel's correction (correction factor $n/(n-1)$))

```
std(x)
```

```
3.0551
```



Basic Statistical Functions

- `var(x)` returns the variance (with Bessel's correction)

```
>> var(x)  
9.3333
```

- `median(x)` returns the sample of the distribution which is in the middle rank when samples are ordered.

```
>> median(x)  
4
```



Basic Statistical Functions

- `cov(x)` returns the variance (with Bessel's correction)

```
>>x=[1 2 ;3 4];
```

```
>> cov(x)
```

```
    2    -1
```

```
   -1     3
```

- `mean2(x)` and `std2(x)` are functions for 2D case.

```
>>mean2(x)
```

```
    2.5000
```

```
>> std2(x)
```

```
    1.2910
```



Distance/Metric Functions

- `mahal(y,x)` returns the Mahalanobis distance of the data points(rows) of `y` to the distribution characterized by the samples(rows) of `x`.

```
>>x=[2 3; 4 7 ; 1 5];
```

```
>> y=[2 7];
```

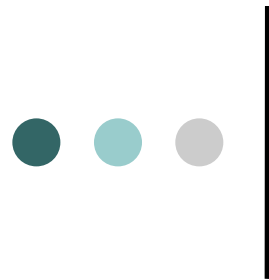
```
>> mahal(y,x)
```

```
2.3333
```

- `pdist(x)` returns the Euclidean distance between pairs of data(rows) points of `x`.

```
>> pdist(x)
```

```
4.4721    2.2361    3.6056
```

Distance/Metric Functions

- `pdist(x,distance)` can be used to find the distance between pairs of data of `x` with the specified distance metric.

```
>> pdist(x,'cityblock')  
    6    3    5
```

- `norm(x)` returns the norm of a matrix(or vector).

```
>> norm(x)  
10.0906
```



Parameter Estimation Functions

- `normfit(x)` returns the mean and standard deviation of the data that is assumed to be originated from normal distribution.

```
>> x=[3 2 6 4 7 3];
```

```
>> [mu_est,sig_est]=normfit(x)
```

```
mu_est =
```

```
4.1667
```

```
sig_est =
```

```
1.9408
```



Parameter Estimation Functions

- `expfit(x)` returns the mean of the data that is assumed to be originated from exponential distribution.

```
>>expfit(x)  
4.1667
```

- There are similar functions for other commonly used distributions. The confidence intervals(with adjustable confidence) may also be obtained for the estimates.



Parameter Estimation Functions

- `mle(x, 'distribution', 'dist')` returns the maximum likelihood (ML) estimate of the parameters that is assumed to be originated from the specified distribution by 'dist'.

```
>>mle(x,'distribution','normal')
```

```
4.1667  1.7717
```

```
>> mle(x,'distribution','gamma')
```

```
5.6322  0.7398
```

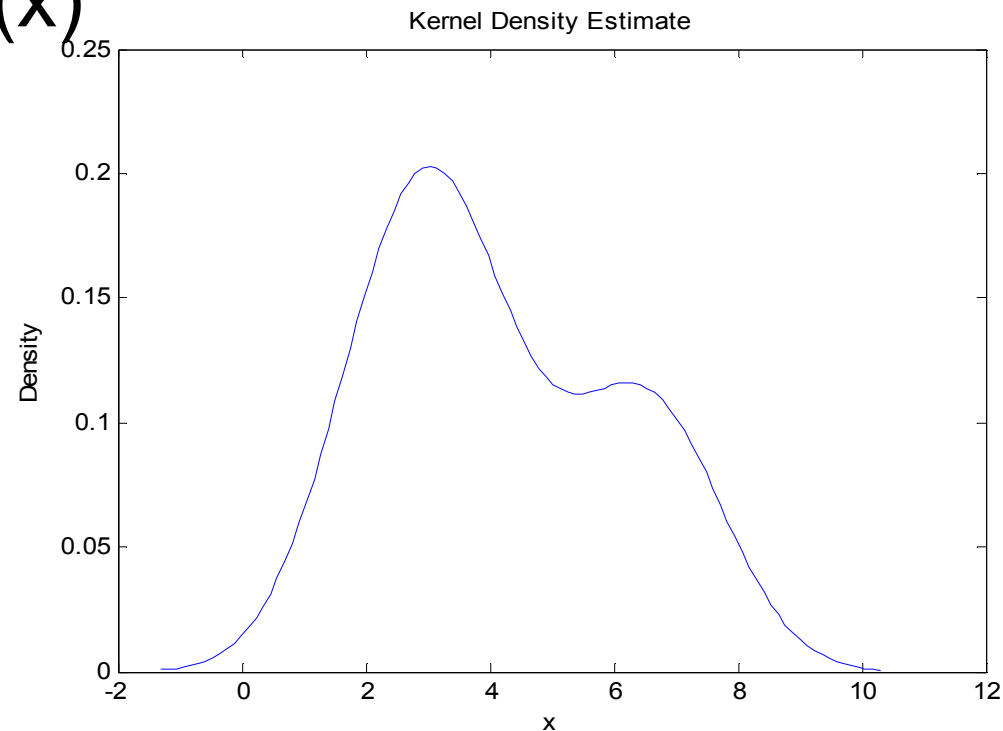
When it is used as `mle(x)`(with no distribution specification), normal distribution is assumed.

Density Estimation Functions

- `ksdensity(x)` returns the computed density estimate using a kernel smoothing method.

```
>> x=[3 2 6 4 7 3];
```

```
>> ksdensity(x)
```

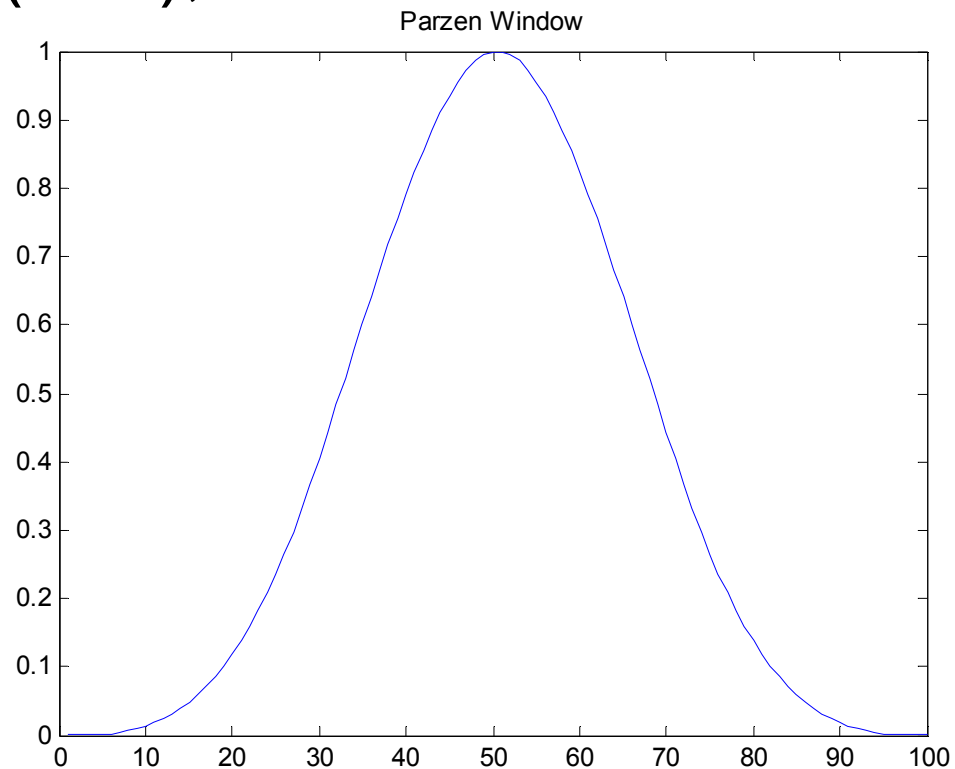


Density Estimation Functions

- `parzenwin(n)` forms a parzen window having `n` elements.

```
>>x=parzenwin(100);
```

```
>> plot(x)
```



● ● ● | Classification/Clustering Functions

- `knnclassify(sample, training, group)` classifies each data of the sample matrix using nearest neighbor rule which is supervised by the training data and its labeling.

```
>> x=normrnd(10,3,5,1) >> y=normrnd(13,3,5,1)
```

```
13.2850
```

```
11.8676
```

```
4.3780
```

```
12.1123
```

```
11.2845
```

```
8.5746
```

```
12.6869
```

```
12.2980
```

```
12.1929
```

```
13.3553
```

- ● ● | Classification/Clustering Functions

```
>> training=[x;y];
```

```
>> group=[ones(5,1); 2*ones(5,1)];
```

```
>> sample=normrnd(11,3,4,1)
```

```
11.9444
```

```
15.3305
```

```
9.9471
```

```
12.8697
```

```
>> knnclassify(sample, training, group)
```

```
[2; 2;1;1]
```


● ● ● | Classification/Clustering Functions

➤ `knnclassify(sample, training, group, k)`
classifies each data using k-nearest neighbor rule.

```
>>knnclassify(sample, training, group, 3)  
[2;1;2;1]
```

Note that classification result changes.

➤ `knnclassify(sample, training, group, k, distance)` performs classification using the specified distance metric (default is euclidean distance.).

● ● ● | Classification/Clustering Functions

- `kmeans(x,k)` clusters the data into `k` classes using `k` means clustering algorithm.

```
>>kmeans(training,2)
    2;2;1;2;2;1;1;1; 1; 2
```

- `kmeans` function can also be used with other distance metrics(`kmeans(x,k,'distance','dist')`).

```
>> kmeans(training,2,'distance','cityblock')
    1;1;2;1;1; 2;2; 2; 2;1
```

● ● ● | Classification/Clustering Functions

➤ `classify(sample,training,group)` classifies the sample data into classes using the training dataset labeled with group. It performs discriminant analysis.

```
>> classify(sample,training,group)
      [2;2;1;2]
```

➤ The type of discriminant function to be used can be adjusted.

```
>> classify(sample,training,group,'quadratic')
      [2;1;2;2]
```

● ● ● | Classification/Clustering Functions

- The priors of the classes can be incorporated into classification.

```
>> prior=[0.1 0.9];
```

```
>> classify(sample,training,group,'quadratic',prior)
[2;2;2;2]
```

```
>> prior=[0.9 0.1];
```

```
>> classify(sample,training,group,'quadratic',prior)
[1;1;1;1]
```

- ❖ The choice of priors is critical.

● ● ● | Classification/Clustering Functions

- `clusterdata(x,cutoff)` clusters the data using a hierarchical cluster tree. `cutoff` is a parameter to adjust the number of clusters to be formed at the end ($0 < \text{cutoff} < 2$).

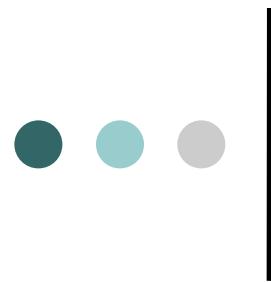
```
>> x=normrnd(20,2,5,1);
```

```
>> y=normrnd(30,2,5,1);
```

```
>> z=[x;y];
```

```
>> t=clusterdata(z,1)
```

```
[4;4;2;1;1;3;3;3;3;3]
```



Classification/Clustering Functions

```
>> t=clusterdata(z,1.2)  
[1;1;1;1;1;1;1;1;1;1]
```

- The distance metric to be used can be changed and the maximum number of clusters to be formed can be specified.

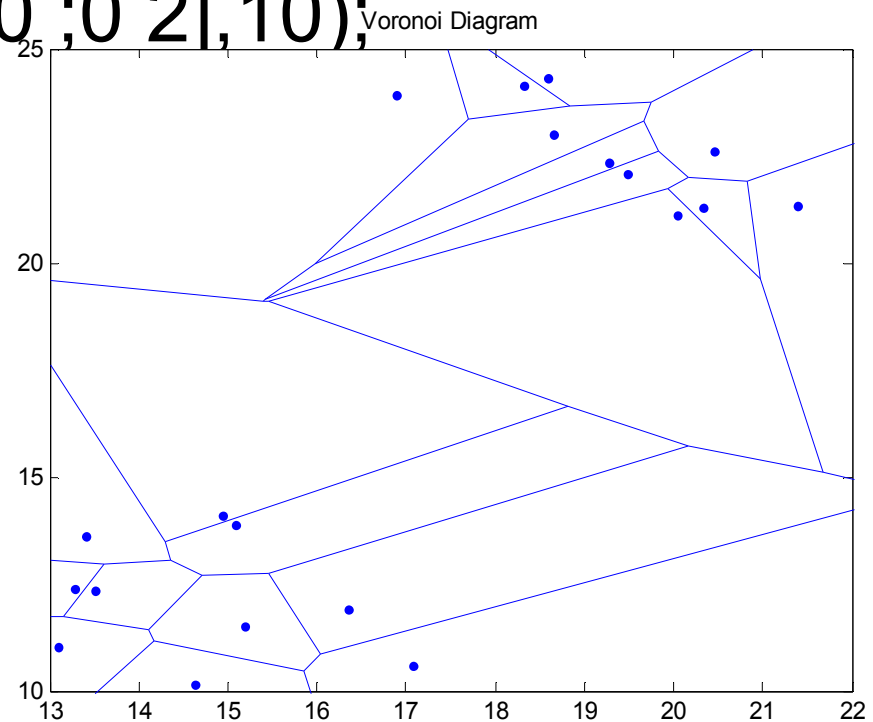
Classification/Clustering Functions

- `voronoi(x,y)` forms the voronoi diagram for the datasets `x` and `y`.

```
>> x=mvnrnd([20 ; 15],[2 0 ;0 2],10);
```

```
>> y=mvnrnd([23 ; 12],[2 0 ;0 2],10);
```

```
>> voronoi(x,y)
```

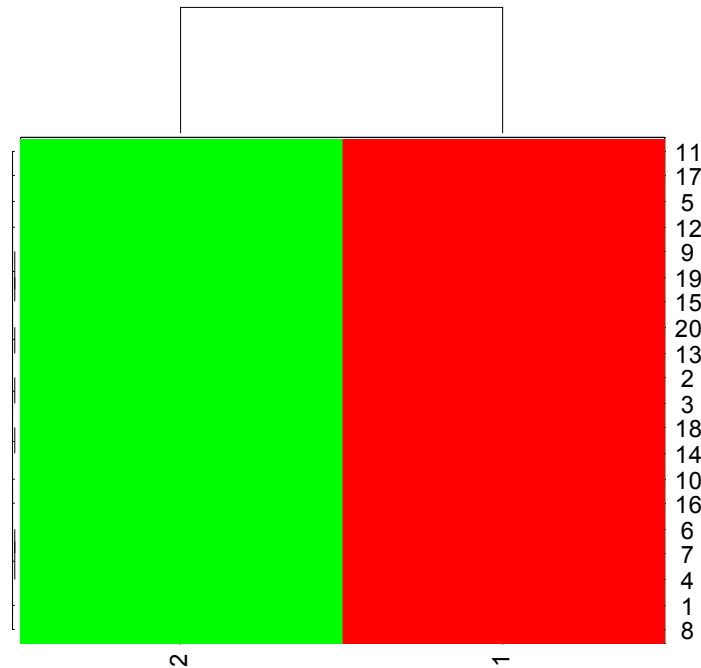


● ● ● | Classification/Clustering Functions

- `clustergram(x)` draws the dendrogram of the dataset `x`. The similar and distant datasets are visualized.

```
>> z=[x;y];
```

```
>> clustergram(z)
```



● ● ● | Dimension Reduction Functions

- `pcacov(v)` performs Principal Component Analysis (PCA) using the covariance matrix and returns the coefficient matrix.

```
>> v=[1 0.4 -0.2; 0.4 1.3 0.2; -0.2 0.2 0.8];
```

```
>> pcacov(v)
```

```
-0.5485    0.5811    0.6012
```

```
-0.8330   -0.3171   -0.4534
```

```
-0.0729   -0.7495    0.6580
```



Dimension Reduction Functions

- PCA can also be performed with `princomp(x)` directly from the data.

```
>>princomp(x)
```

```
0.6668    0.7453
```

```
0.7453   -0.6668
```



MATLAB Toolboxes

- A Toolbox is a collection of m-files developed to perform computation on a particular domain.

Ex: Animation toolbox (Developing scientific animations)

- Some toolboxes are present inside MATLAB but some are not embedded. They are available on the Internet.



MATLAB Toolboxes

- Neural Networks Toolbox:

Includes tools for designing, implementing, visualizing and simulating neural networks.

- Statistics Toolbox:

Provides tools for modeling and analyzing data, simulating systems, developing statistical algorithms, learning and teaching statistics.



MATLAB Toolboxes

- PRTools Toolbox:

Includes algorithms for data generation, training classifiers, features selection, density estimation, feature extraction, cluster analysis.

- Statistical Pattern Recognition Toolbox:

It provides users with procedures for discriminant functions, feature extraction, density estimation, support vector machines, visualization, regression, etc..



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- PRTools Toolbox:

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MATLAB Toolboxes

- Fuzzy Logic Toolbox
- Classification Toolbox
- Clustering Toolbox
- ClusterPack Toolbox
- GHSOM Toolbox
- HMM Toolbox
- HMMBOX Toolbox
- LPSVM Toolbox
- NSVM Toolbox



MATLAB Toolboxes

- PCNN Toolbox
- SDH Toolbox
- SOM Toolbox
- SSVM Toolbox
- SVM Toolbox
- SVM Classifier Toolbox
- Bioinformatics Toolbox



END

Thank you for listening.

Any Questions or
Comments ??